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# HIGGS self couplings

with the collaboration of:

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- \* Introduction
- \* The simplest case.
- \* Conclusion(s) ?

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## Testing Higgs Self-couplings at $e^+e^-$ Linear Colliders

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### Abstract

To establish the Higgs mechanism *sui generis* experimentally, the self-energy potential of the Higgs field must be reconstructed. This task requires the measurement of the trilinear and quadrilinear self-couplings, as predicted, for instance, in the Standard Model or in supersymmetric theories. The couplings can be probed in multiple Higgs production at high-luminosity  $e^+e^-$  linear colliders. Complementing earlier studies to develop a coherent picture of the trilinear couplings, we have analyzed the production of pairs of neutral Higgs bosons in all relevant channels of double Higgs-strahlung, associated multiple Higgs production and  $WW/ZZ$  fusion to Higgs pairs.

# Measuring the Trilinear Couplings of MSSM Neutral Higgs Bosons at High-Energy $e^+e^-$ Colliders

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## Abstract

We present a detailed analysis of multiple production of the lightest  $CP$ -even Higgs boson ( $h$ ) of the Minimal Supersymmetric Standard Model (MSSM) at high-energy  $e^+e^-$  colliders. We consider the production of the heavier  $CP$ -even Higgs boson ( $H$ ) via Higgs-strahlung  $e^+e^- \rightarrow ZH$ , in association with the  $CP$ -odd Higgs

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# Measuring Trilinear Higgs Couplings in the MSSM

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## Abstract

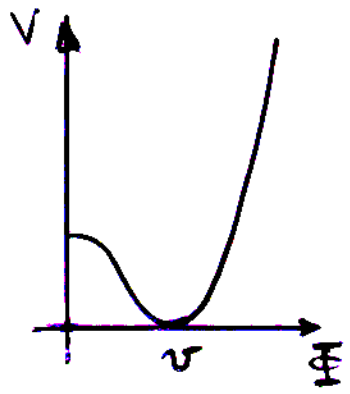
Trilinear couplings of the neutral  $CP$ -even Higgs bosons in the Minimal Supersymmetric Standard Model (MSSM) can be measured through the multiple production of the lightest  $CP$ -even Higgs boson ( $h$ ) at high-energy  $e^+e^-$  colliders. This includes the production of the heavier  $CP$ -even Higgs boson ( $H$ ) via  $e^+e^- \rightarrow ZH$ , in association with the  $CP$ -odd Higgs boson ( $A$ ) in  $e^+e^- \rightarrow AH$ , or via  $e^+e^- \rightarrow \nu_i \nu_j H$ , with  $H$  subsequently decaying through  $H \rightarrow hh$ . These processes can enable one to measure the trilinear Higgs couplings  $\lambda_{Hhh}$  and  $\lambda_{hhh}$ , which can be used to theoretically reconstruct the Higgs potential. We delineate the regions of the MSSM parameter space in which these trilinear Higgs couplings could be measured.

# Introduction

Higgs potential has to be tested  
(ultimate proof of the nature of H)



SM example



$$V(H) = \lambda (H^\dagger H - v^2)^2$$

↑ quartic coupling

with  $v = 174 \text{ GeV}$

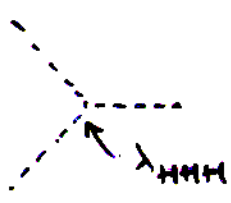
Thus

Higgs mass

$$M_H^2 = 4\lambda v^2$$

trilinear self coupling

$$\lambda_{HHH} = 6\sqrt{2}\lambda v = 3M_H^2 / \sqrt{2}v$$



quartic linear self coupling

$$\lambda_{HHHH} = 6\lambda = 3M_H^2 / 2v^2$$



MSSM case

much more complicated!

- 4 different  $\lambda$ s in the potential
- All trilinear couplings exist!

$$\lambda_{\bar{L}L\bar{L}}, \lambda_{\bar{L}RH}, \lambda_{\bar{L}HH}, \lambda_{HHH}, \lambda_{\bar{L}AA}, \lambda_{HAA}$$

$$\lambda_{\bar{L}H^+H^-}, \lambda_{HH^+H^-}$$

functions of  $\alpha, \beta$

★ It's very important (fundamental) to measure these trilinear couplings.

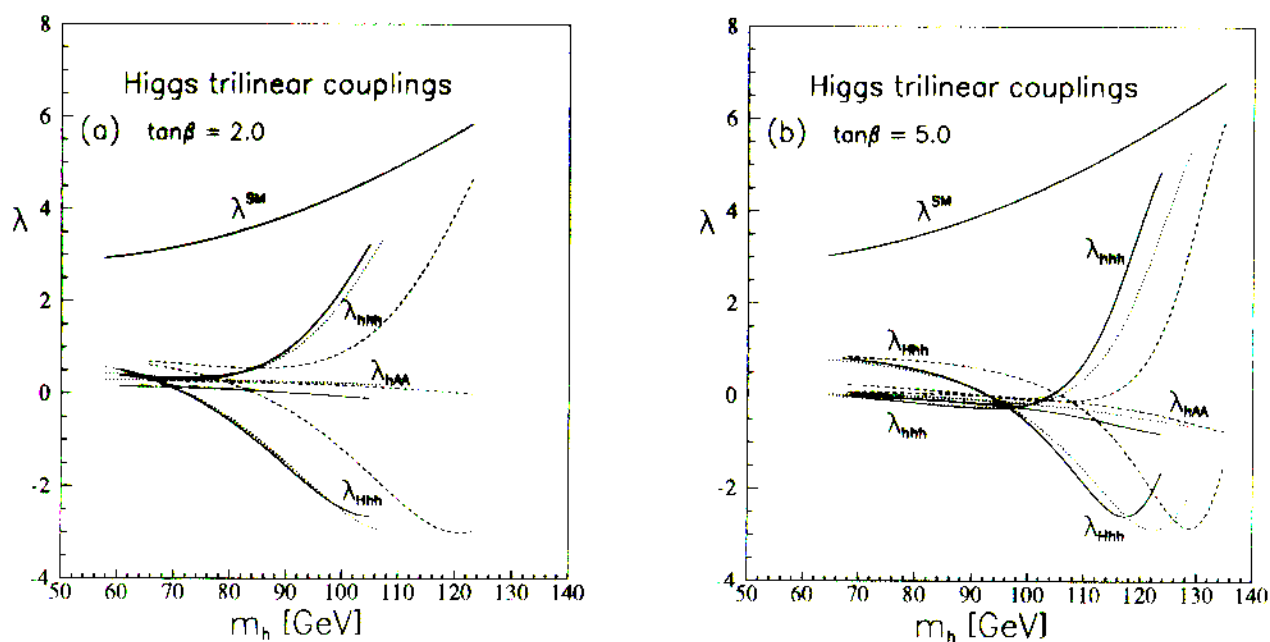


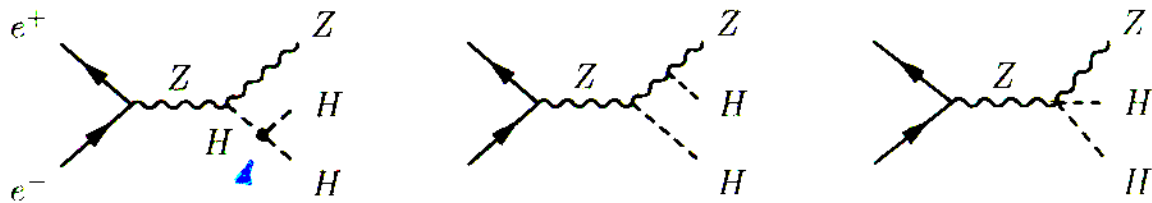
Figure 1: Trilinear Higgs couplings  $\lambda_{Hhh}$ ,  $\lambda_{hhh}$  and  $\lambda_{hAA}$  as functions of  $m_h$  for two values of  $\tan\beta$ : (a)  $\tan\beta = 2.0$ . (b)  $\tan\beta = 5.0$ . Each coupling is shown for three cases of the mixing parameters: no mixing ( $A = 0$ ,  $\mu = 0$ , solid), mixing with  $A = 1$  TeV and  $\mu = -1$  TeV (dotted), as well as  $A = 1$  TeV and  $\mu = 1$  TeV (dashed).

from Osland / Pandita

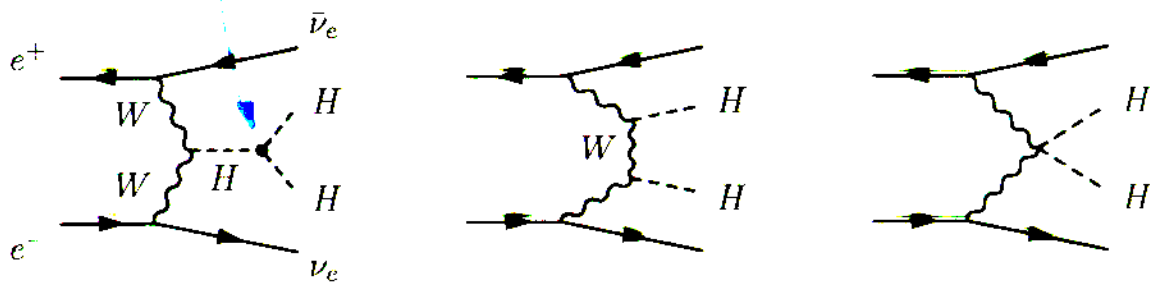
# The simplest case

SM!

double Higgs-strahlung:  $e^+e^- \rightarrow ZHH$



WW double-Higgs fusion:  $e^+e^- \rightarrow \bar{\nu}_e \nu_e HH$



ZHH important for  $\sqrt{s} \leq 500 \text{ GeV}$   
 fusion dominant for  $\sqrt{s} > 500 \text{ GeV}$

X-sections for  $M_H = 110 \text{ GeV}$

ZHH @  $\sqrt{s} = 500 \text{ GeV}$  :  $\sim 0.2 \text{ fb}$

fusion @  $\sqrt{s} = 1 \text{ TeV}$  :  $\sim 0.1 \text{ fb}$

ZHH feasibility study @  $\sqrt{s} = 500 \text{ GeV}$

with  $M_H = 100 \text{ GeV}$

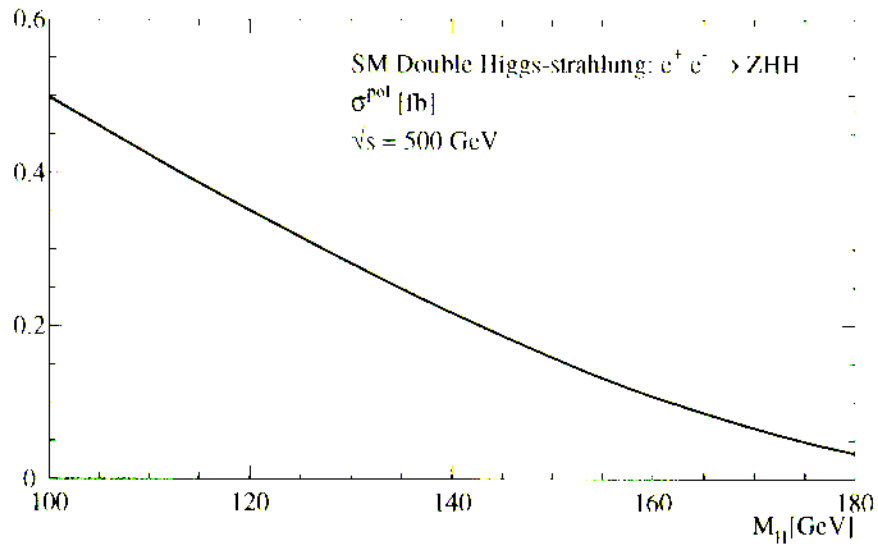


Figure 1: The cross section for double Higgs strahlung in the SM at the collider energy  $\sqrt{s} = 500$  GeV. The electron-positron beams are taken oppositely polarized.

↑ important.

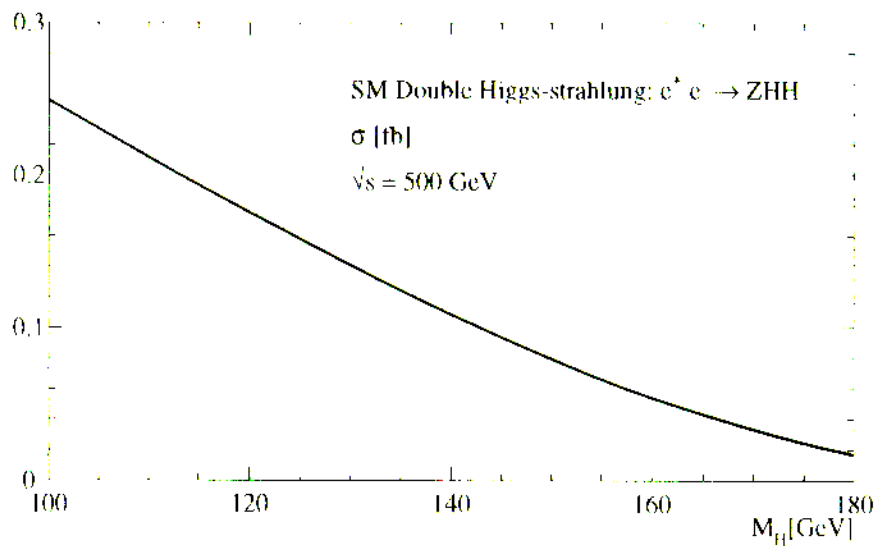


Figure 2: The cross section for double Higgs strahlung in the SM at the collider energy  $\sqrt{s} = 500$  GeV. The electron-positron beams are unpolarized.

SM,  $\sqrt{s} = 500$ ,  $M_H = 100$ ,  $HZ$  channel

Signal:

x-section: 0.25 fb

signature: 1Z and 2H

(GRACE)

6 jets, kin. fits, btag)

background(s)

			x-section
"2 fermion"	$q\bar{q}(x)$ including $t\bar{t}$ !	↑	8200 fb
"4 fermion"	$W^+W^-$	↑ (PYTHIA) ↓	4700 fb
	$Z^0Z^0$		550 fb
	$Z\ell\bar{\ell}/W\nu$		12700 fb
	$HZ$		70 fb
"6 fermion"	$WWZ$	) (GRACE)	20 fb
	$ZZZ$		0.53 fb

most difficult background:  $Zb\bar{b}b\bar{b}$ !  $\geq 0.02$  fb  
reducible only thru kin. fits!

generator level study!

simple sequential analysis.

P. Lutz

Summary:

	Initial	cut #1	cut #2	cut #3	cut #4
Signal	0.175	0.172	0.169	0.129	0.014
$q\bar{q}(x)$	8200	164	110	38	-
WW	7700	1740	154	8	-
ZZ	550	148	20	5	-
W $\nu$ /Z $\nu$	12700	2	2	-	-
HZ	70	33	4	2	-
ZZZ	0.53				
WWZ	20				
Total b $\nu$ gd	$\sim 29$ pb	$\sim 2$ pb	$< 300$ fb	$\sim ?$	$?$
s/b	$< 10^{-6}$	$\approx 10^{-4}$	$\sim 8 \cdot 10^{-4}$	$?$	$?$

8-10% efficiency.

caveat: 1) statistics not enough

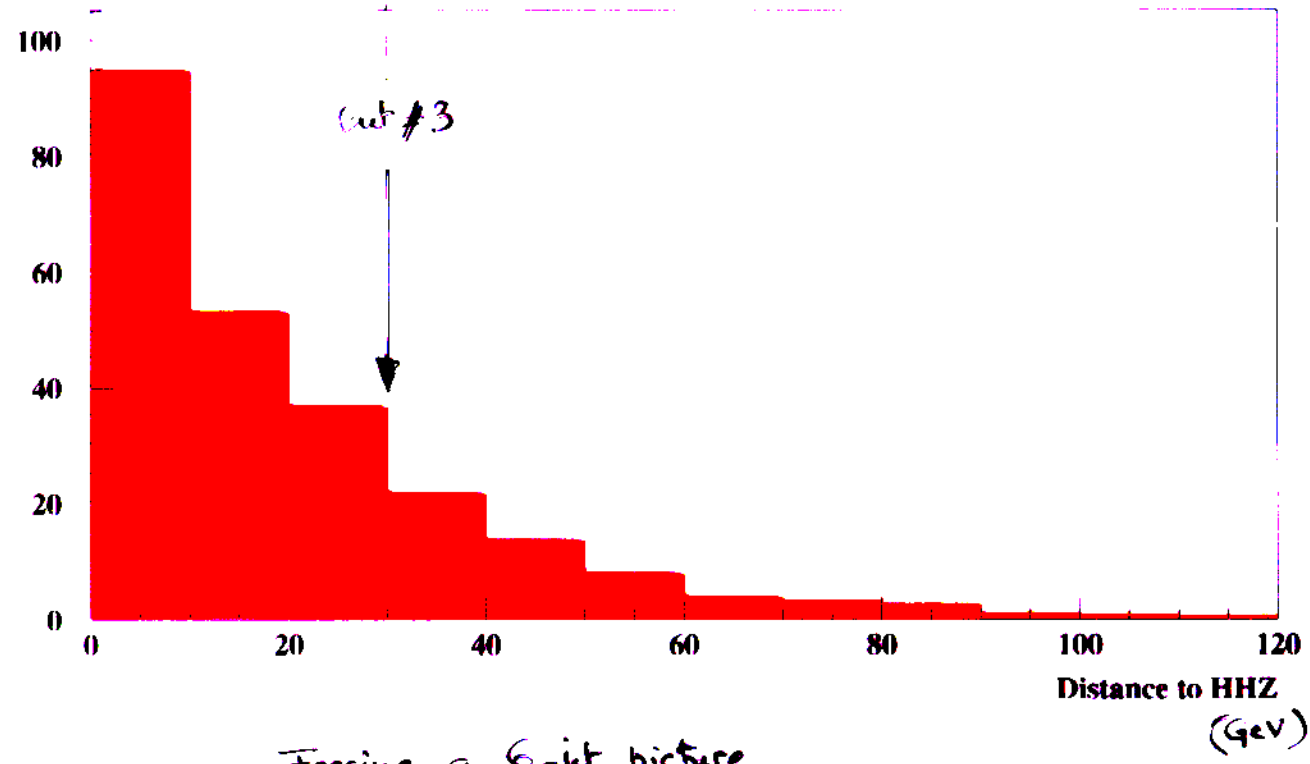
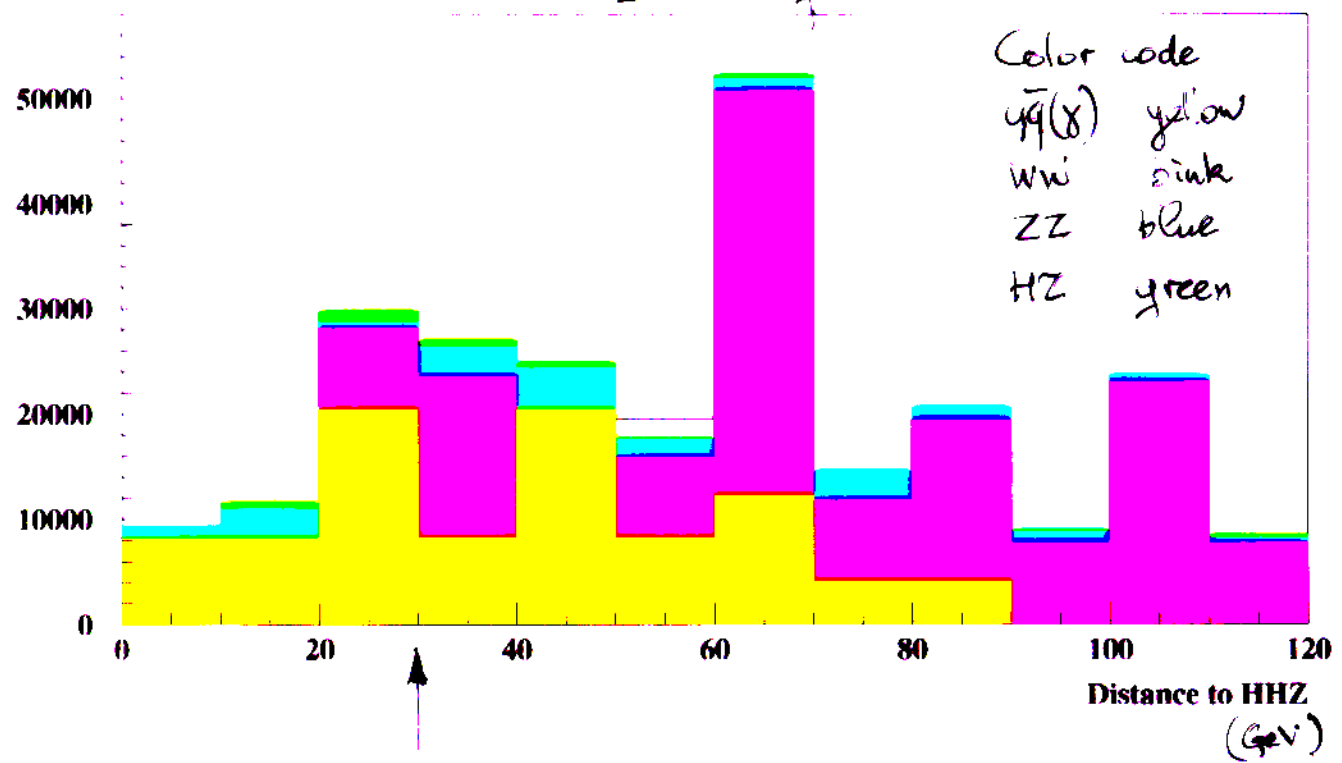
2) major backgrounds (WWZ and ZZZ) not generated yet!

1) and 2) will be covered before SITGES!

Together with an overall optimisation of this set of cuts  
No hope for a SGV/SIMDET/BRAHMS simulation...

### TESLA - HHZ analysis - $\sqrt{s} = 500$ GeV

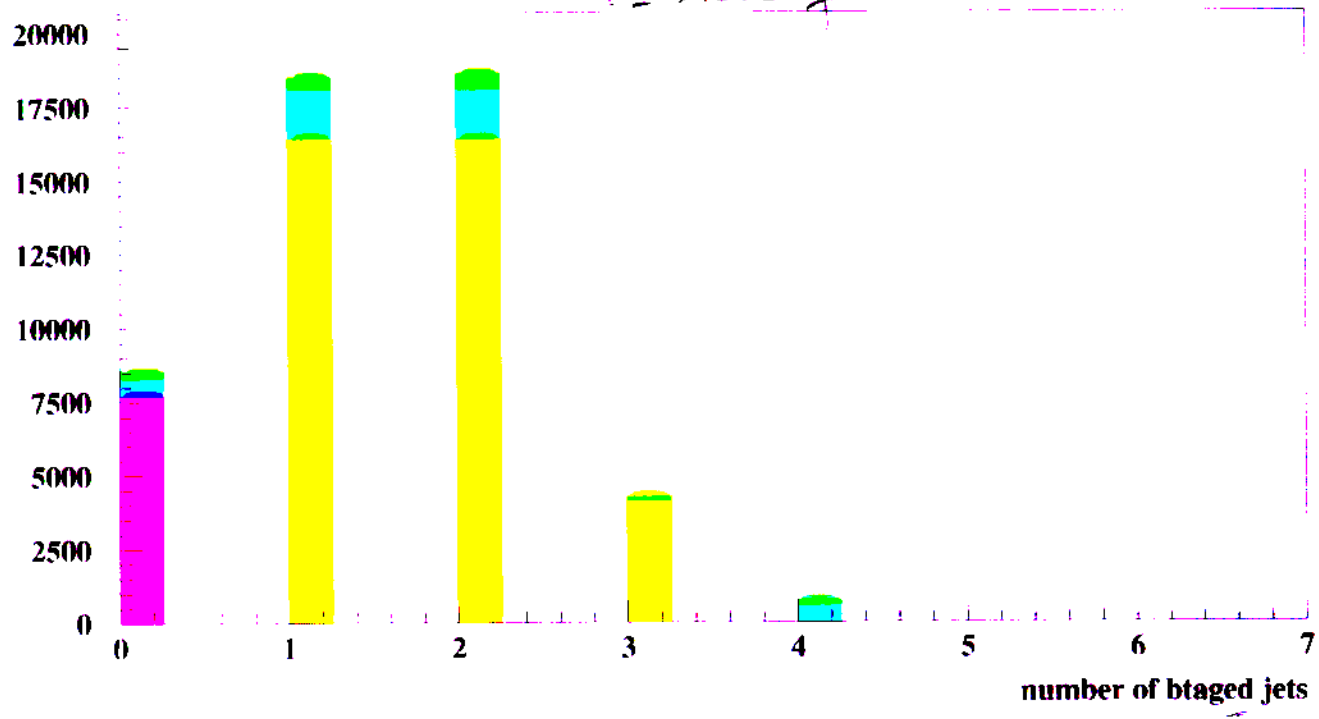
$L = 1000 \text{ fb}^{-1}$



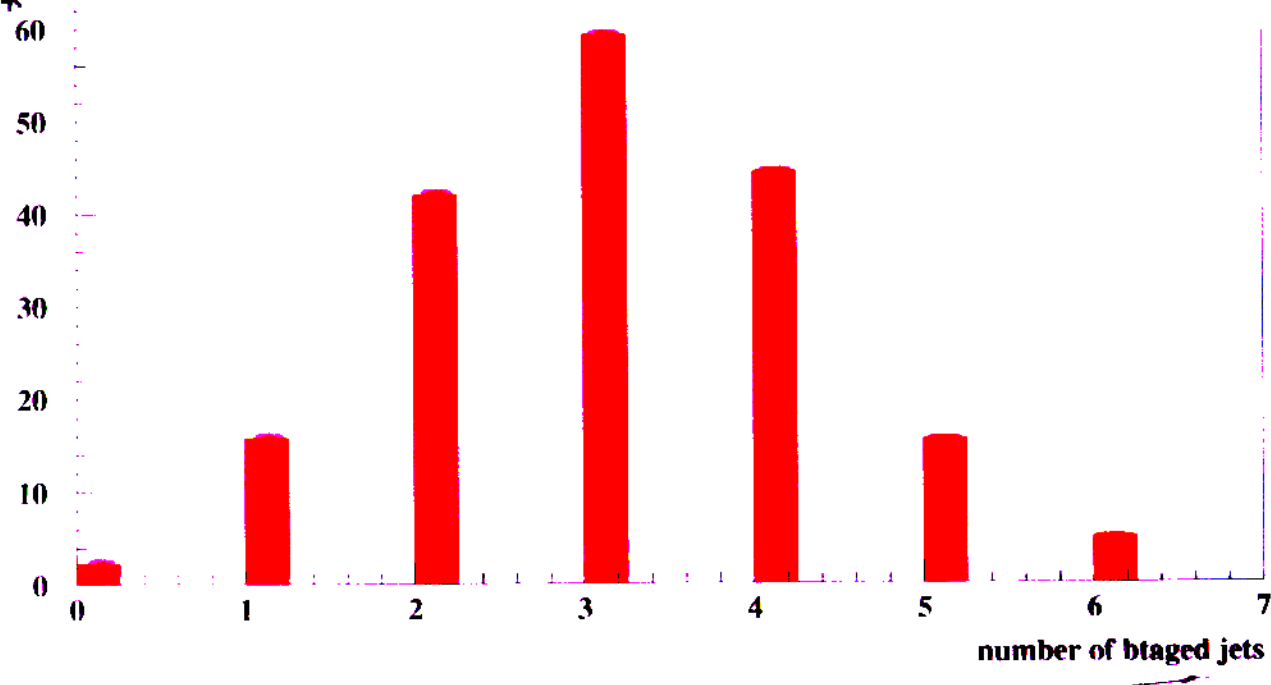
Forcing a 6-jet picture  
 15 bijets, 15 triplets of bijets  
 compute the min. (euclidian) distance to  
 (100., 100., 91.2)

### TESLA - HHZ analysis - $\sqrt{s} = 500$ GeV

$\sigma = 1000 \text{ fb}^{-1}$

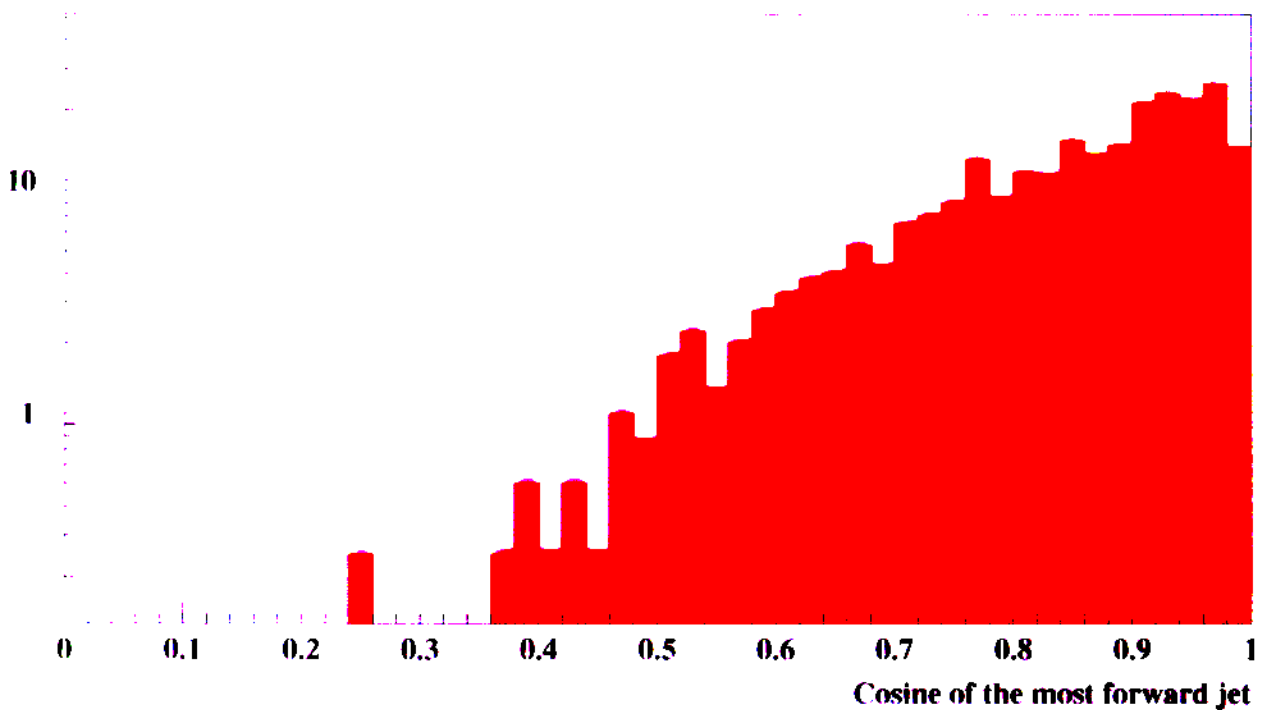
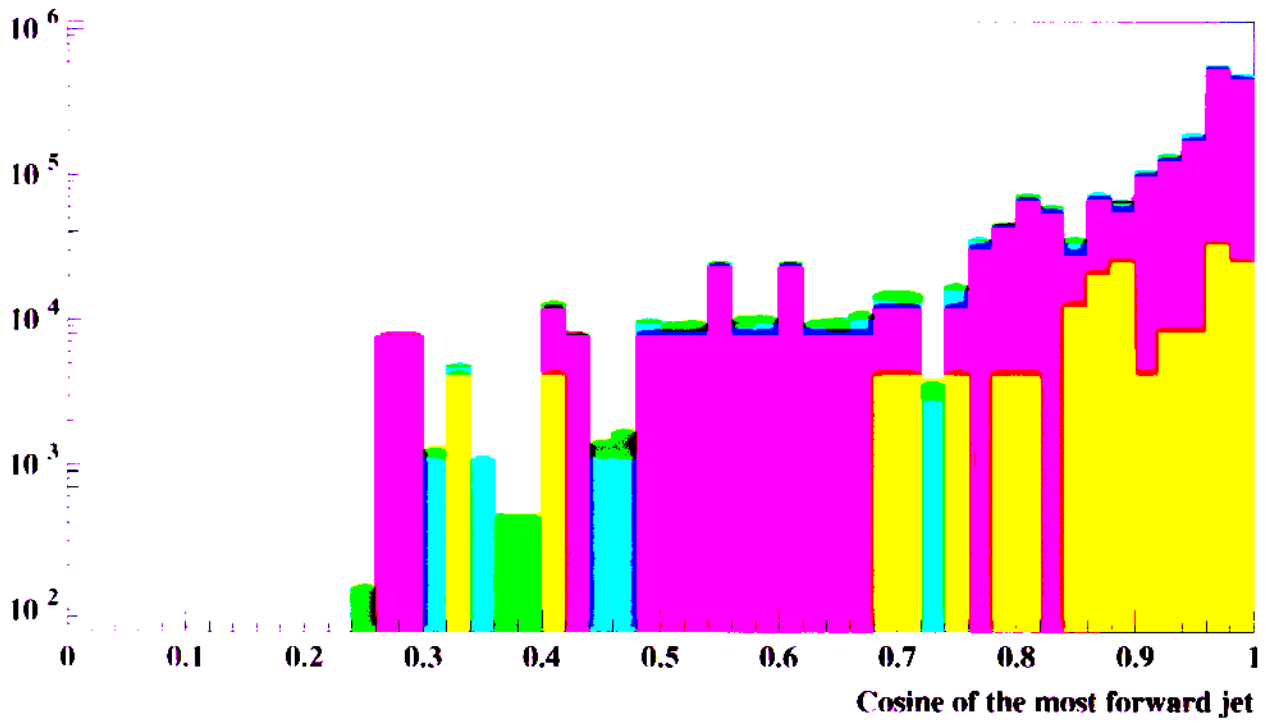


0.7\*



cut #4 : selecting a high number of b-jets.

## TESLA - HHZ analysis - $\sqrt{s} = 500$ GeV



We need :

- a very good forward acceptance
- a very good forward btag!

vertex detector coverage up to  
cos  $\sim .94$

# Conclusions

- It seems feasible to
  - \* claim evidence for (SM)  $HHZ$  events  
↳  $q\bar{q}$
  - \* measure the cross-section (errors?)
  - \* deduce a value for  $\lambda_{HHH}$  (precision?)  
↳  $\lesssim 20\%$

- under a (few) mandatory conditions.

\* ~ low  $\sqrt{s}$ , but very high luminosity!

$$\rightarrow \left\{ \begin{array}{l} \mathcal{L} \geq 500 \text{ fb}^{-1} \quad (\text{SM}) \\ \mathcal{L} \sim 1000 \text{ fb}^{-1} \quad (\text{MSSM}) \end{array} \right.$$

\* with a detector with a good forward accept.

→  $\left. \begin{array}{l} \text{jet reconstruction down to } < 10^\circ \\ \text{tagging capability down to } < 20^\circ \end{array} \right\}$

Challenging, but ~~it~~ is rewarding!