

Looking for extra-dimensions  
at the weak-scale  
experimental search for  
Kaluza-Klein states signatures  
at the  $e^+e^-$  linear colliders

ECFA-DESY

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Marc Besançon  
(DAPNIA/SPP/CEA Saclay)

## Some motivations

Exciting piece of superstrings physics !

- string dualities  $\rightarrow$  string scale  $M$  not at  $M_{Planck}$ 
  - Witten  $\rightarrow M$  arbitrary parameter**
  - Lykken  $\rightarrow M$  in the TeV region ?**
- superstrings leaves in 10-d space time
- possibility of "opening"  $\delta$  extra-dimensions at the TeV scale

See also Antoniadis 90' (string compactification)

→  $\delta$  extra-dimensions → Kaluza Klein states

Kaluza-Klein unification of gravity and e.m.  
1921 1926 in 5 dimensions

assume the ground state of general relativity is

$M^4 \times S^1$   
4d Minkowski circle

generalization: complex quantum field  $\phi(x)$  depends  
not only on the 4d-spacetime coordinates  $X(x_0 \dots x_3)$   
but also the  $\delta$  extra dimension  $Y(y_1 \dots y_\delta)$

periodicity of  $\phi(x)$  under  $y_i \rightarrow y_i + 2\pi R$  →

$$\phi(x) = \sum_{n_1=-\infty}^{+\infty} \sum_{n_2=-\infty}^{+\infty} \dots \sum_{n_\delta=-\infty}^{+\infty} \phi^{(n)}(x) e^{i \frac{n \cdot y}{R}}$$

$$n_i \in \mathbb{Z}$$

the "4d" fields  $\phi^{(n)}(x)$  are the Kaluza Klein  
modes (or excitations)

$$m_n^2 = m_0^2 + \frac{n^2}{R^2} \quad p = \frac{n}{R}$$

momenta appearing as masses for states that are  
massless from the higher dimensional point of view

# Impact of extra-dimensions on phenomenology

- grand unification at TeV scales

Dienes Dudas Egergetta

- millimeter ranges forces (SUSY)

$$d=2 \rightarrow \frac{1}{r^4} (< \text{mm})$$

$$\vdots$$
$$d=6 \rightarrow \frac{1}{r^8} (< \text{fm})$$

see also

Antoniadis Dimopoulos  
Dvali

Antoniadis Arkani-Hamed

Dimopoulos Dvali

{ Antoniadis Dudas Sagnotti  
Antoniadis Quiros  
Dudas Grojean

- excitations of KK states at colliders

Antoniadis Benakli  
Quiros

→ Giudice Rattazzi Wells

Mirabelli Perelstein

Peskin

Han Lykken Zhang

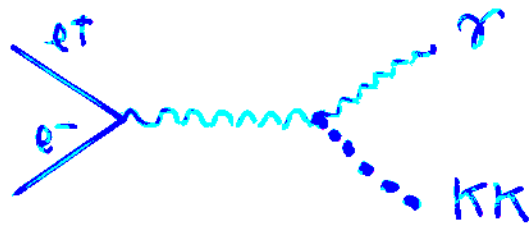
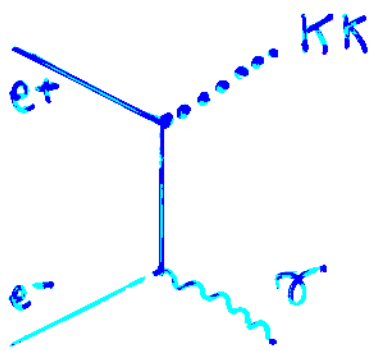
Hewett

# A piece of phenomenology at $e^+e^-$

- resonant production of KK gauge bosons if accessible in mass

if not  $\Rightarrow$  effective 4 $\ell$  interaction  
look for deviations from the SM

- production of single KK boson



KK  $\equiv$  SU(2)  $\times$  U(1) gauge bosons (neutral)  
higgs  
graviton

lifetime (from hep-ph/9811350)

$$\tau(G_{KK} \rightarrow \gamma\gamma) \sim 6 \cdot 10^9 \text{ yr} \left( \frac{100 \text{ TeV}}{m_{KK}} \right)^3$$

ex:

$$\sim \tau(G_{KK} \rightarrow f\bar{f})$$

## KK graviton emission in the extra-dimension

$e^+e^- \rightarrow \gamma$  graviton, from hep-ph/9811291

**WITHOUT ISR:**

$$\frac{d\sigma}{dx_\gamma d\cos\theta} = \frac{\alpha}{64} \frac{2\pi^{\frac{\delta}{2}}}{\Gamma(\frac{\delta}{2})} \left(\frac{\sqrt{s}}{M}\right)^{\delta+2} \frac{1}{s} f(x_\gamma, \cos\theta)$$

with  $x_\gamma = \frac{2E_\gamma}{\sqrt{s}}$  and assuming  $\sum_{k_T} = R^\delta \int d^\delta m$   
where  $M^{\delta+2} R^\delta = (4\pi G_N)^{-1}$

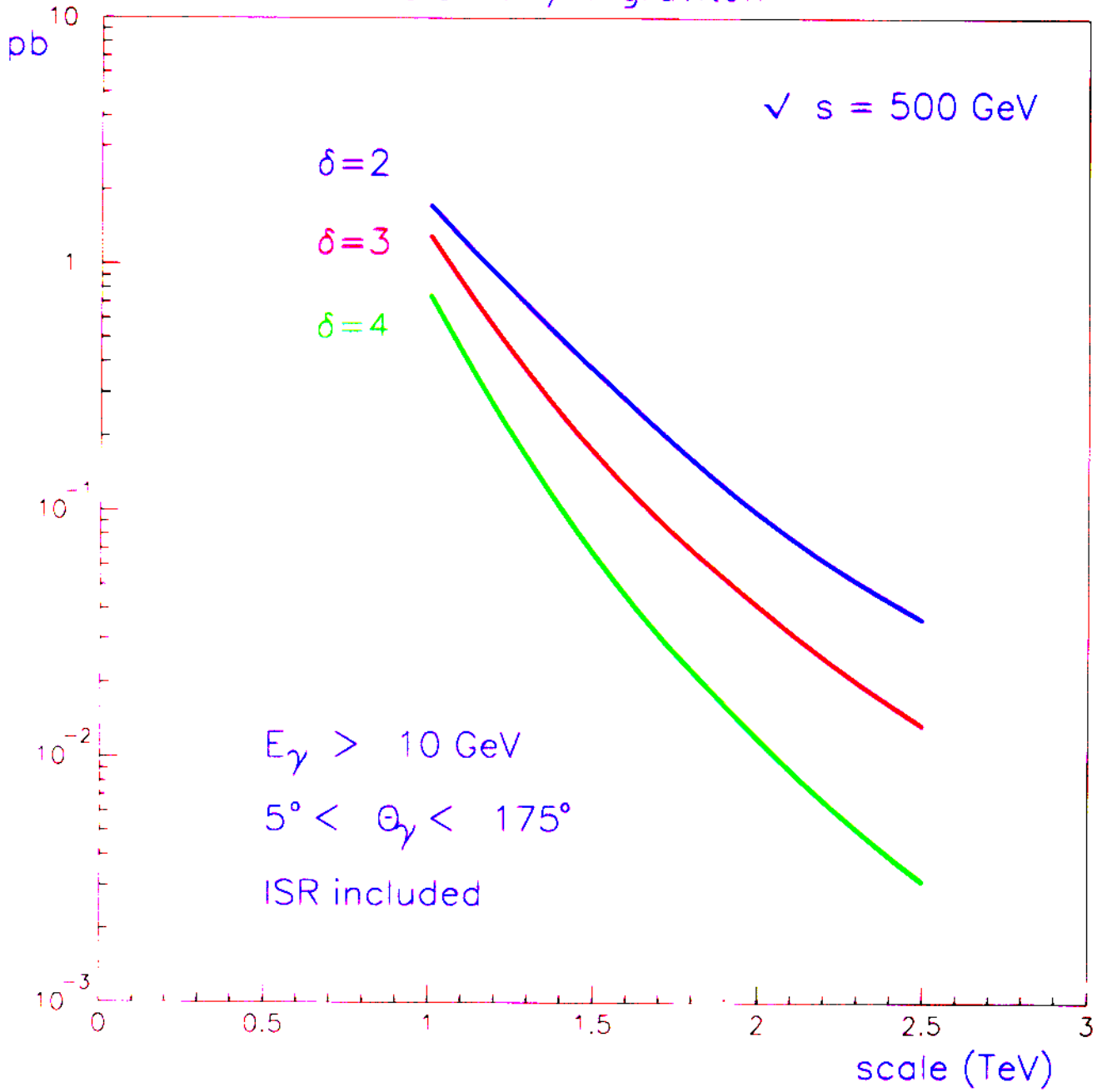
M = scale and  $\delta$  = number of extra-dimensions  
divergence for  $x_\gamma \rightarrow 0$  and  $\cos^2\theta \rightarrow 1$

1st task: add ISR  $\rightarrow$

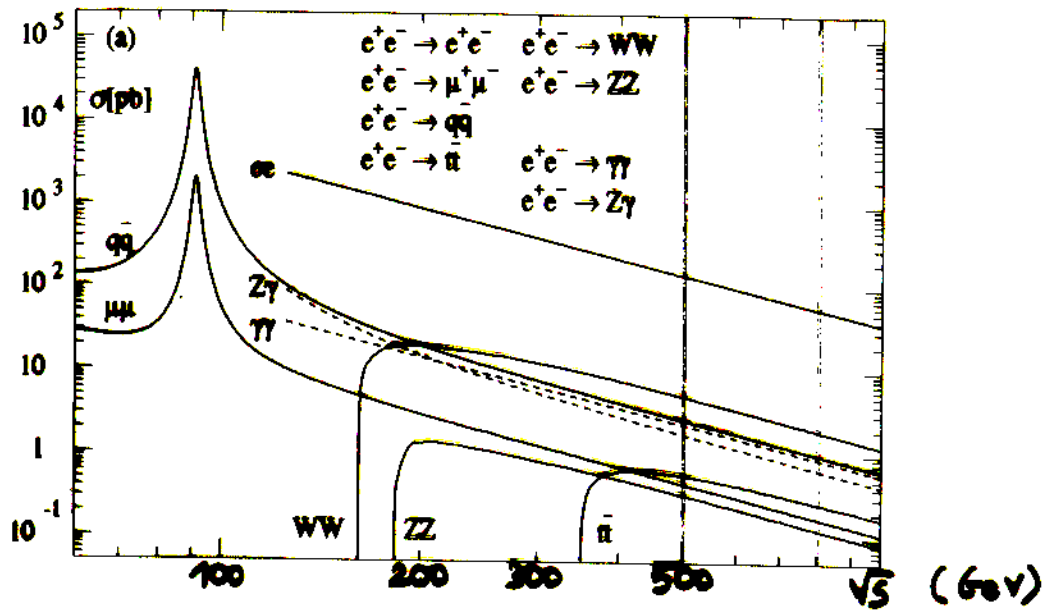
lowering of Xsection up to 10% or more !

look for signature  $(\gamma)_{ISR} \gamma \cancel{E}$

$e^+e^- \rightarrow \gamma + \text{graviton}$



# Background from SM processes



## PYTHIA 5.7

$\sigma (e^+e^- \rightarrow Z\gamma)$	8.2 pb	includes $\nu\bar{\nu}\gamma$
$\sigma (e^+e^- \rightarrow ZZ)$	0.55 pb	
$\sigma (e^+e^- \rightarrow WW)$	7.7 pb	
$\sigma (e^+e^- \rightarrow W\ell\nu)$	5.3 pb	
$\sigma (e^+e^- \rightarrow Z\ell\ell)$	7.4 pb	
$\sigma (e^+e^- [\text{2}\gamma \text{ processes}])$	3.6 nb	
$\sigma (e^+e^- \rightarrow \gamma\gamma (\gamma))$	8.02 pb	←
$\sigma (e^+e^- \rightarrow e^+e^- (\gamma))$	3.9 nb	←

# SMEARING

- electromagnetic resolution  $\frac{10\%}{\sqrt{E}}$
- hadronic resolution  $\frac{50\%}{\sqrt{E}}$
- electron identification 90 %

# SMEARING

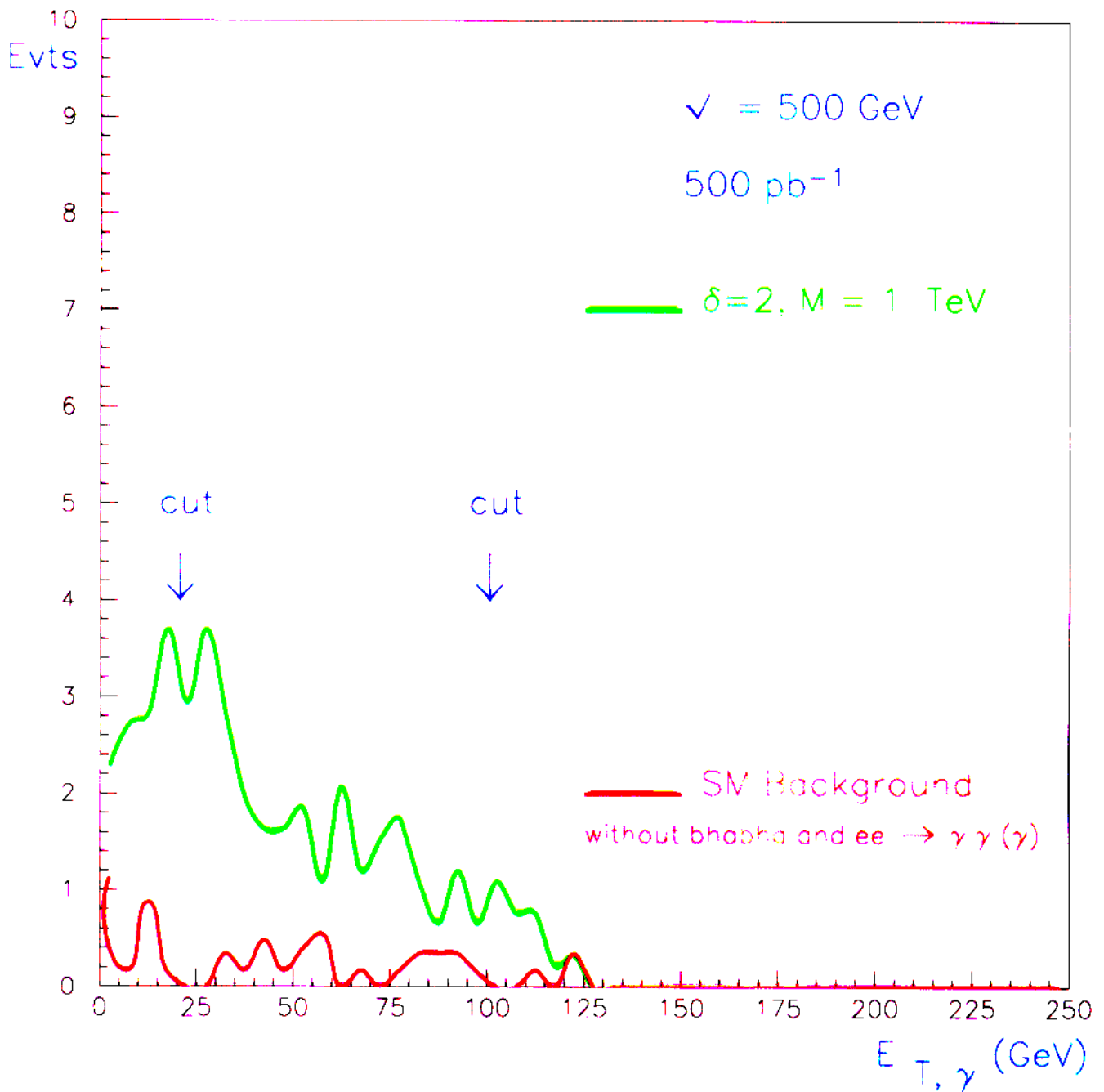
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## SELECTION

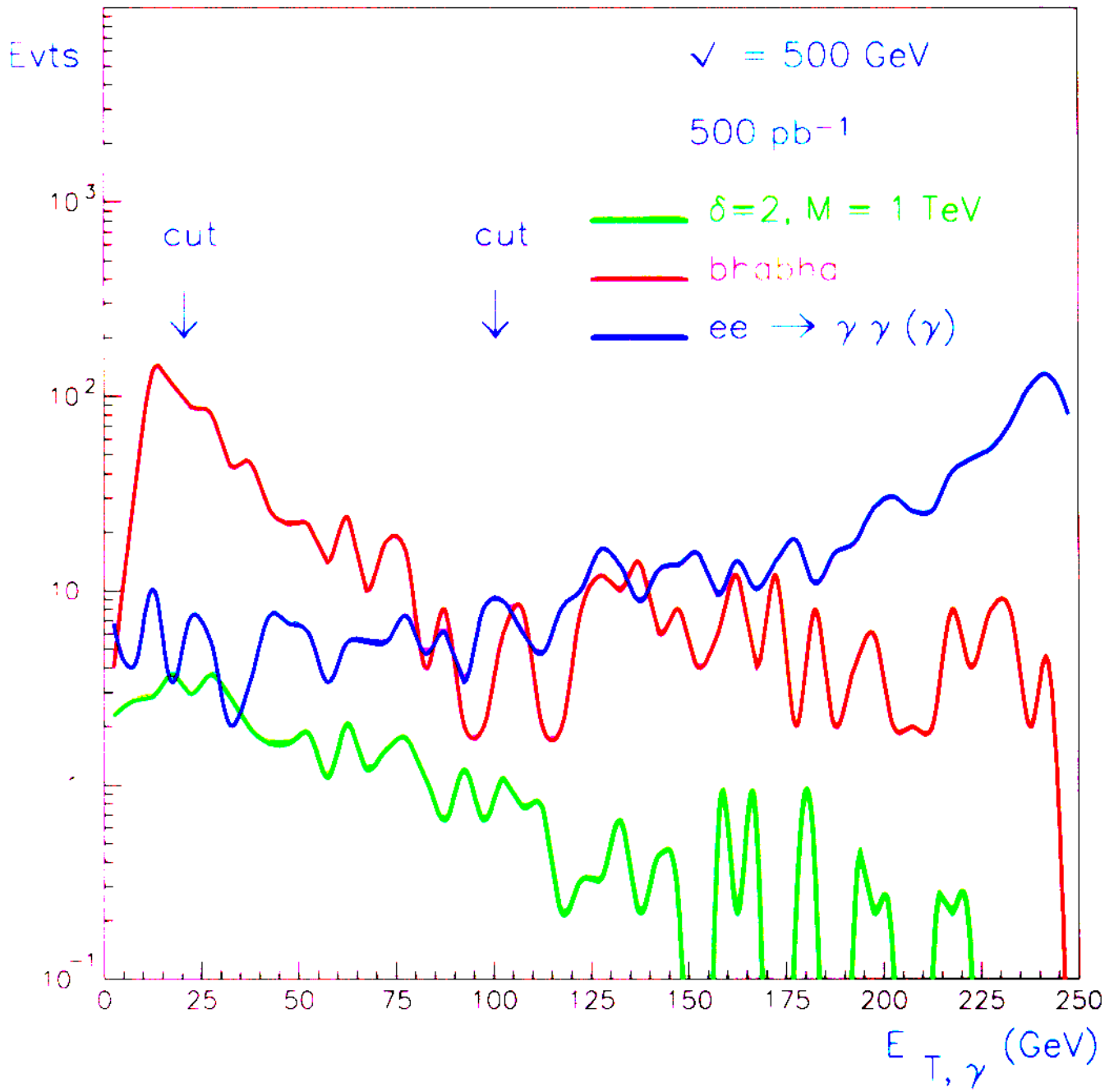
- 2  $\gamma$ 's in  $[10^\circ, 170^\circ]$  and nothing else
- Energy leading  $\gamma > 10$  GeV
- Energy of next to leading  $\gamma > 5$  GeV

Look at  $E_T$  of the leading  $\gamma$

$$e^+e^- \rightarrow \gamma + \text{graviton}$$



$e^+e^- \rightarrow \gamma + \text{graviton}$



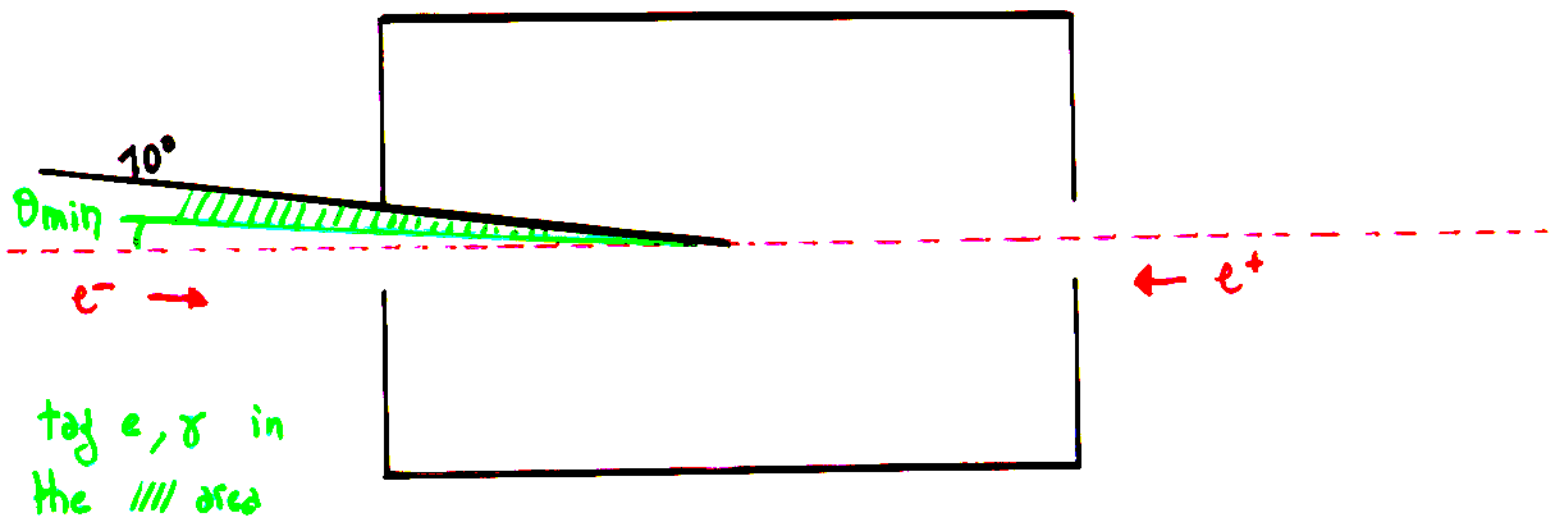
## SELECTION (continued)

The situation may not be hopeless

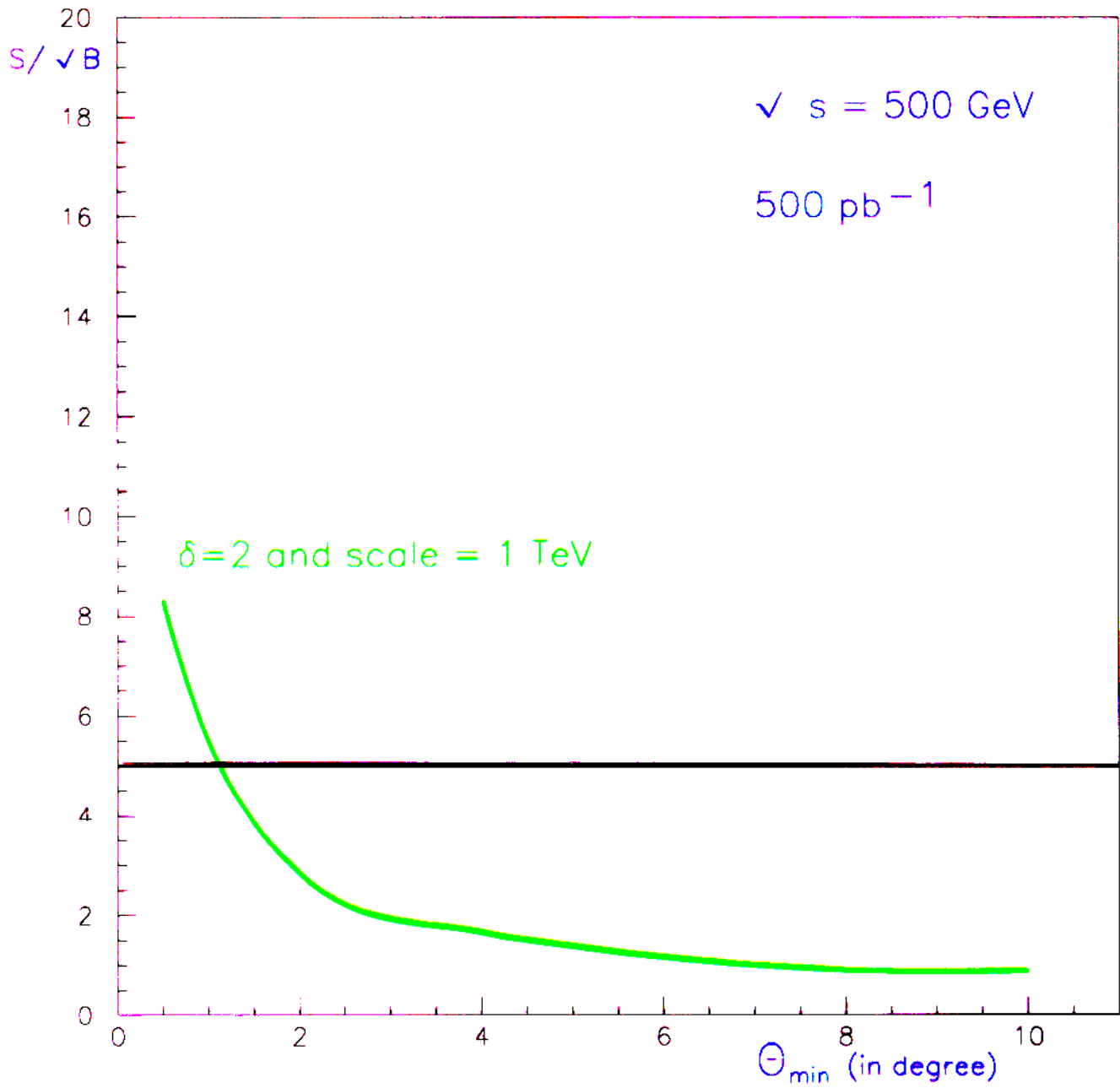
- $20 \text{ GeV} < E_T \text{ of leading } \gamma < 100 \text{ GeV}$
- $10 \text{ GeV} < E_{\text{missing}} < 150 \text{ GeV}$
- no electron tagged in  $[\theta_{\text{min}}, 10^\circ]$
- $\sum E_\gamma \text{ in } [10^\circ, 170^\circ] + \sum E_\gamma \text{ in } [\theta_{\text{min}}, 10^\circ] < 150 \text{ GeV}$

Tagging and measurement of electron and  $\gamma$  below  $10^\circ$  down to  $\theta_{\text{min}}$  required

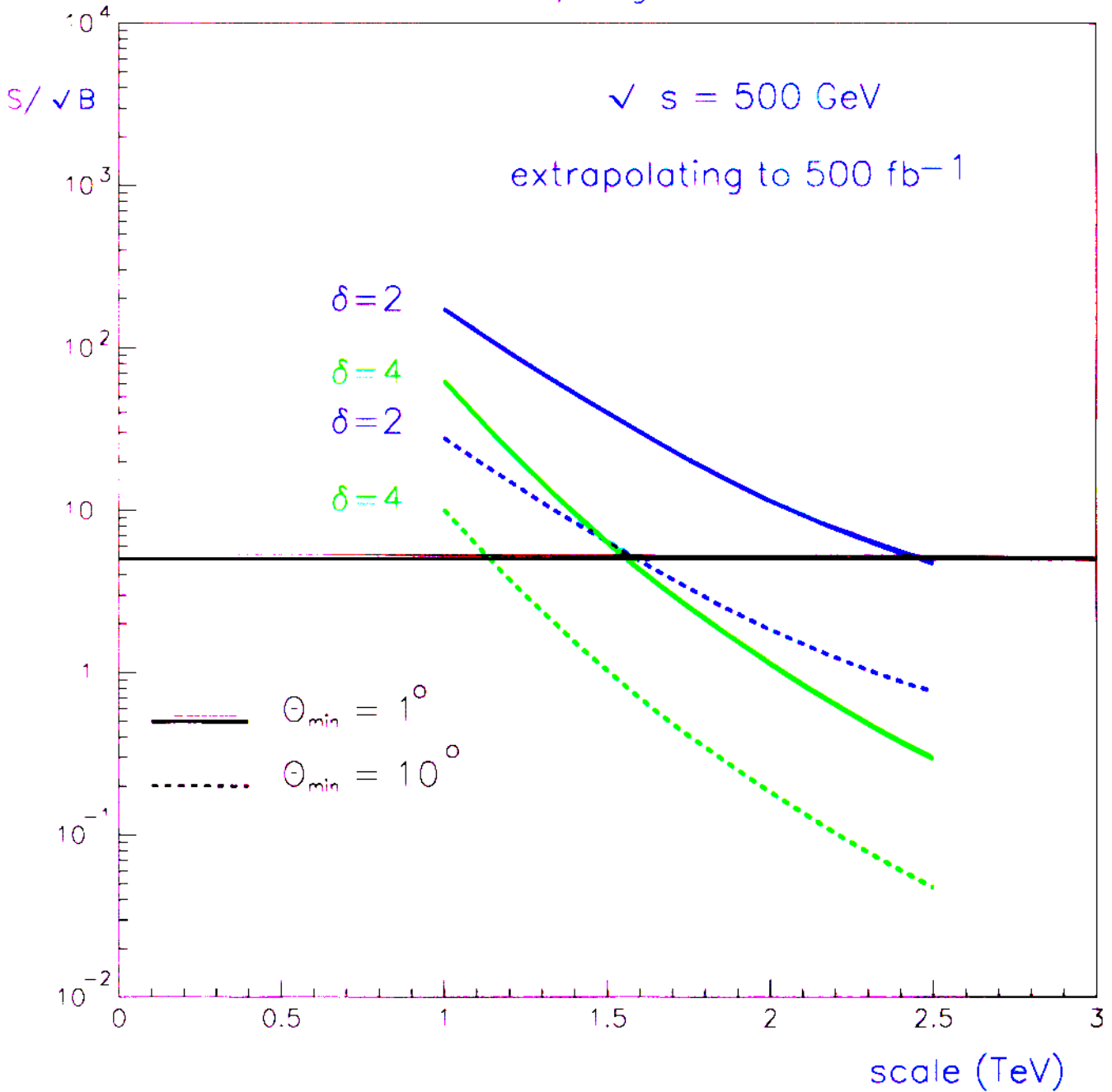
Try  $\theta_{\text{min}} = 0.5^\circ 1^\circ 1.5^\circ 2^\circ 4^\circ 5^\circ$  and  $10^\circ$



$$e^+e^- \rightarrow \gamma + \text{graviton}$$



$e^+e^- \rightarrow \gamma + \text{graviton}$



## Conclusions

- The search for Kaluza-Klein states at present/future colliders is an exciting piece of (experimental) string physics !
- At the  $e^+e^-$  collider the search for  $e^+e^- \rightarrow \gamma$  graviton seems a promising way to look for extra-dimensions at the TeV scale
- Xsections have been calculated  
**inclusion of ISR  $\rightarrow$  Xsections are 10% -15% lower**
- From the present Monte Carlo study this signal can be extracted from the  $\nu\bar{\nu}\gamma(\gamma)$  background as well as, **provided that one can tag  $e$  and  $\gamma$  below  $10^\circ$ ,** bhabha and  $e^+e^- \rightarrow (\gamma)\gamma\gamma$  backgrounds
- **For example tagging  $e$  and  $\gamma$  down to  $1^\circ$  allows for an efficient veto which in turn allows to explore the 2.5 TeV string scale domain for 2 extra-dimensions at the linear collider after  $500 \text{ fb}^{-1}$**
- Additionnal direct search for Kaluza-Klein states signatures can be provided by the search for  $e^+e^- \rightarrow Z$  graviton where the SU(2) gauge boson Z decays as usual into quarks or leptons giving 2 jets or 2 leptons + missing energy  
**help from theoreticians in the calculation of Xsection welcome !**