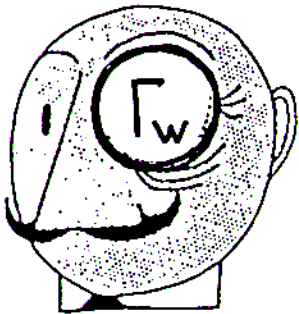


①

2nd ECFA/DESY Study on
Physics and Detectors for a
Linear Electron - Positron Collider

Oxford 20-23rd March, 1999

EW WG



Γ_w as seen through
the eyes of photons
near W^+W^- threshold

V. A. Khoze, LNF



Motivation :

- Encouraged by G. Wilson's talk at Frascati on threshold measurement of M_w ($\Delta M_w \approx 6 \text{ MeV}$) ("theoretical-noise-free")
- Is the LC (experimental) community well aware that the pattern of soft photon radiation allows to probe the time delay $\Delta t \sim \frac{1}{\Gamma_w}$ between the W decays ?

Conventional Γ_W methods

- THRESHOLD SCAN @ 161 GeV

G. Wilson's talk
FRASCATI 9/11/98

- DIRECT KINEMATIC RECONSTRUCTION

$q\bar{q}q\bar{q}$, $q\bar{q}l\nu$ channels

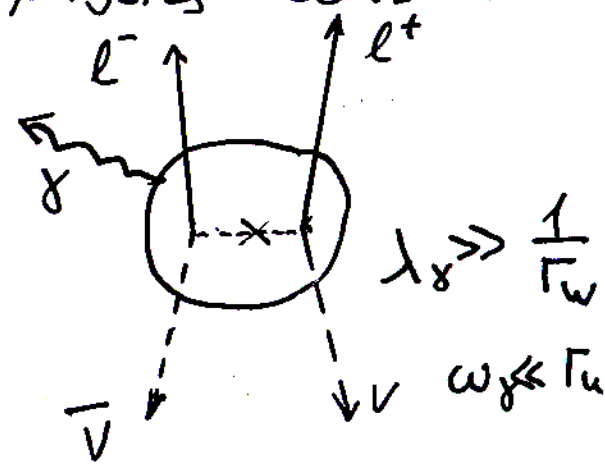
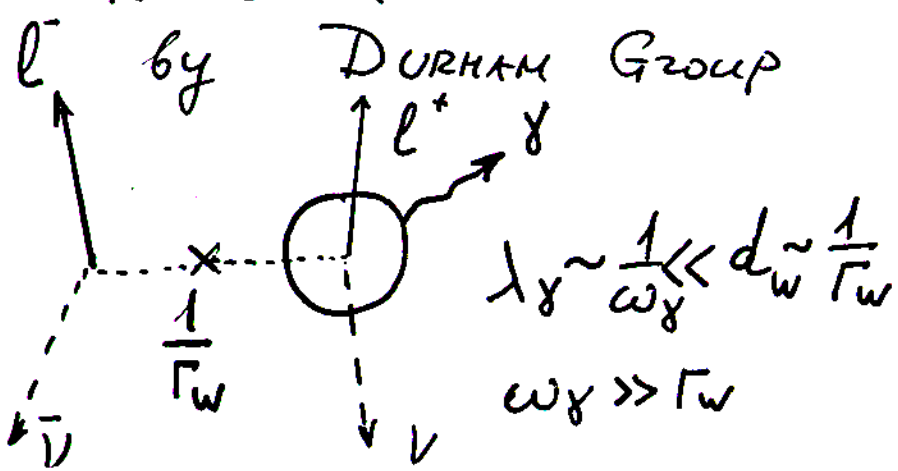
NOT WITHOUT THEIR OWN PROBLEMS
(beam-induced effects, QCD/EW corrections)

- 'INDIRECT' MEASUREMENTS in $P\bar{P}$ (PP) COLLIDERS

Old idea to exploit the Bremsstrahlung Radiation Pattern to measure the TIME DELAY in nuclear reactions
(R.M. Eisberg, D.R. Yennie, D.H. Wilkinson, N.P. 18 (1960) 338-345)

L. Stodolsky

Resurrected in the W-physics context by DURHAM Group



Has been on the market for years...⁽⁶⁾

KOS (1992), D'KOS (1993)
T. Sjöstrand, VAK (1994) QCD context

Nuclear Physics B403 (1993) 65-100
North-Holland

NUCLEAR
PHYSICS B

May have been a standard tool in the
world of high energy physics ($\Gamma_t, \Gamma_q, \Gamma_e \dots$)

Properties of soft radiation near $t\bar{t}$ and W^+W^- threshold

Yu.L. Dokshitzer

Department of Theoretical Physics, University of Lund, Sölvegatan 14A, S-22362 Lund, Sweden

V.A. Khoze

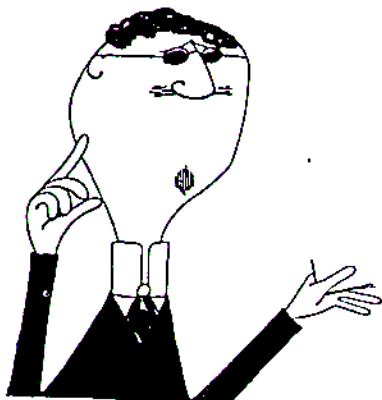
Department of Physics, University of Durham, Durham DH1 3LE, UK

Lynne H. Orr

Department of Physics, University of California, Davis, CA 95616, USA

W.J. Stirling

Departments of Physics and Mathematical Sciences, University of Durham, Durham DH1 3LE, UK



Physics Letters B 213 (1993) 171-179
North-Holland

PHYSICS LETTERS B

Soft photons in W^+W^- production at LEP200

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Lynne H. Orr¹

Department of Physics, University of California, Davis, CA 95616, USA

and

W.J. Stirling

The current
market price is
still unclear

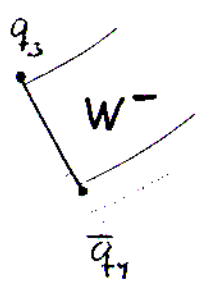
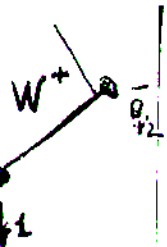


Could LC become a committed buyer?

SPACE-TIME HISTORY

EXAMPLE : QED RADIATION

IN $W^+ W^- \rightarrow q_1 \bar{q}_2 \bar{q}_4 q_3 (e^+ \nu e^- \bar{\nu})$

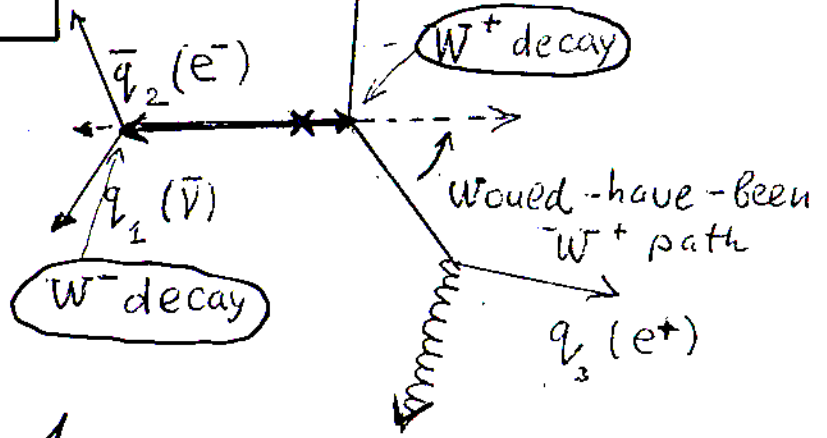


$W = 170 \text{ GeV}$
 $\beta_W \approx 0.34$
 $t_1 \approx 0.02 \text{ fm}$
 $t_2 \approx 0.08 \text{ fm}$
 $\tau_{\text{prod}} \sim \frac{1}{W} \ll \frac{1}{\Gamma_W}$

$$dN \sim \frac{d^3x}{\pi} \frac{d\omega_\gamma}{\omega_\gamma} \frac{d\Omega}{4\pi} \left[R_{\text{ind}} + 2 \text{Re} \langle e^{i\omega_\gamma(t_1-t_2)} \rangle \cdot \mathcal{J}(\nu) \right]$$

$$\langle e^{i\omega_\gamma(t_1-t_2)} \rangle_{1,2} = \frac{\Gamma_W^2}{\Gamma_W^2 + \omega_\gamma^2} = \chi(\omega)$$

D'KOS 1993

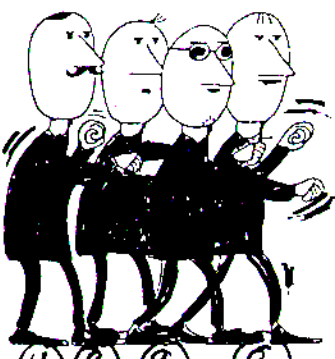


• at $\omega_\gamma \Delta t \sim \omega_\gamma / \Gamma_W \gg 1$
 INTERFERENCE VANISHES
 RESULT OF AVERAGING
 OVER THE INSTANCES OF
 THE DECAYS

$$\lambda \ll \Delta x_W \sim d_W$$



(coherence gets lost)



ONLY FAIRLY SOFT EMISSION
 FEELS THE JOINT ACTION
 OF THE ALL CHARGES

$$\omega_\gamma < \Gamma_W$$

(Coherence remains UNDISTURBED)



W width as a Bremsstrahlung Filter

Through the eyes of a photon

$$e^- e^+ \rightarrow W^+ W^- \rightarrow f_1 \bar{f}_2 \quad f_3 \bar{f}_4 + \gamma$$

$$l^- \bar{\nu}_e \quad l^+ \nu_e + \gamma$$

• $\omega_\gamma \ll \Gamma_W$

$(l^- \bar{\nu}_e)$ and $(l^+ \nu_e)$ appear almost instantaneously and radiate almost coherently as if produced in the same vertex

• $\omega_\gamma \gg \Gamma_W$

$(l^- \bar{\nu}_e)$ and $(l^+ \nu_e)$ appear at very different times t_1, t_2 after $W^+ W^-$ production

$$\tau_p \sim \frac{1}{M_W} \ll \Delta t = |t_1 - t_2| \sim \frac{1}{\Gamma_W}$$

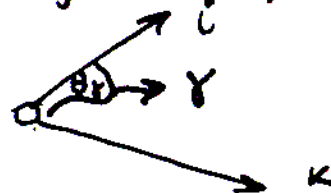
l^- and l^+ radiate photons INDEPENDENTLY

$$\omega_\gamma \frac{dN^{(\alpha\beta)}}{d\omega_\gamma} = \frac{\cancel{2}}{\pi} \frac{dR}{4\pi} \left[(1 - \chi(\omega_\gamma)) R_{ind}^{(\alpha\beta)} + \chi(\omega_\gamma) R_{coh}^{(\alpha\beta)} \right]$$

$(\alpha\beta) = (ll), (le), (ee)$

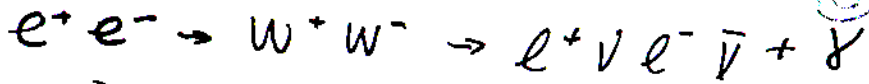
$$\chi(\omega_\gamma) = \frac{\Gamma_W^2}{\Gamma_W^2 + \omega_\gamma^2}$$

• ω_γ / Γ_W dependence vanishes for emission close to the direction of one of the primary charged particles



$$\theta_\gamma \sim \theta_{ik}$$

ISR can be easily taken into account (ISR-FSR interference can be explicit)



$\int_0^{2\pi} d\phi \omega_\gamma \left(\frac{dN}{d\omega_\gamma d\Omega} \right)$

No ISR

Yu.L. Dokshitzer et al. / Properties of soft radiation

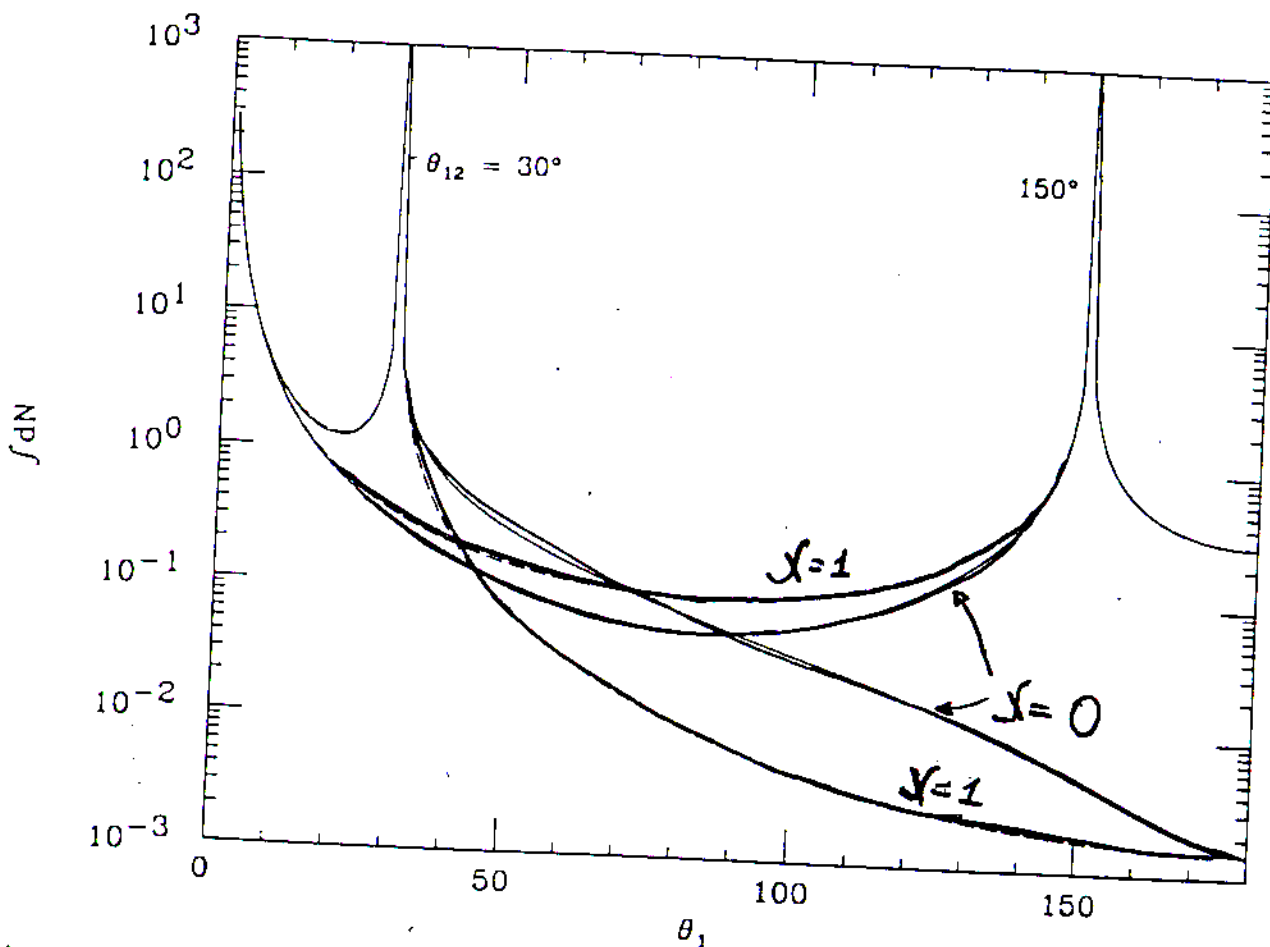
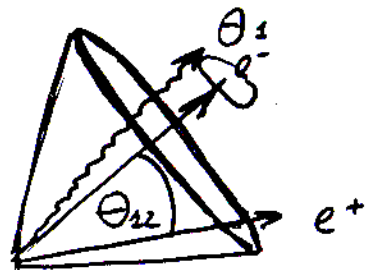


Fig. 4. Analog of fig. 3 for the $W^+ W^-$ case: angular ordering effects in the soft photon distribution in $\gamma\gamma \rightarrow W^+ W^- \rightarrow \ell^+ \ell^- \nu \bar{\nu}$, for $\theta_{12} = 30^\circ$ and 150° . $\int dN \equiv \omega(dN/d\omega d\cos\theta)$ as in fig. 3. Solid lines: $\chi = 0$; dashed lines: $\chi = 1$. (The $\gamma\gamma \rightarrow W^+ W^-$ case is equivalent to the $e^+ e^- \rightarrow W^+ W^-$ case with no initial state radiation.)

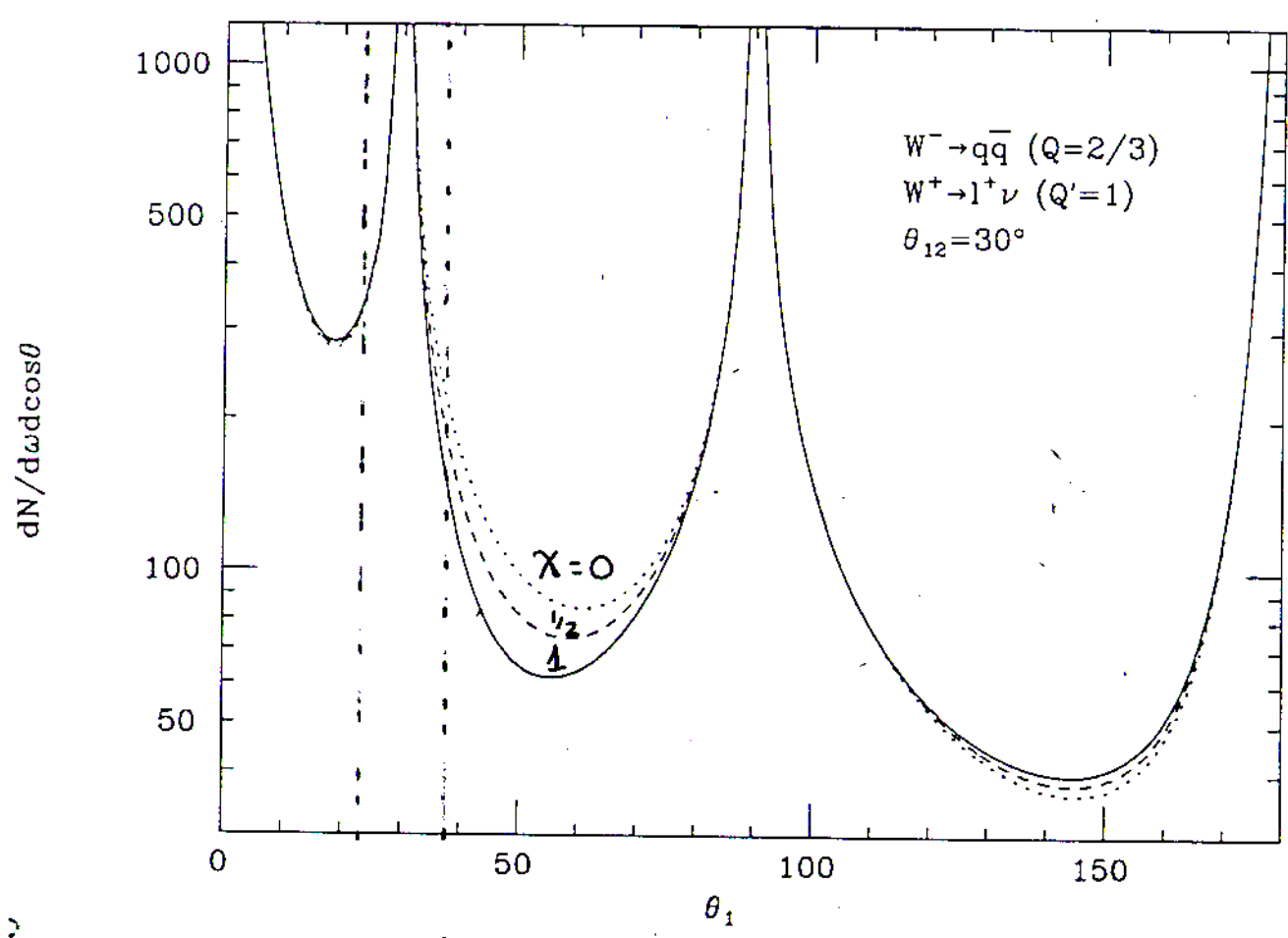
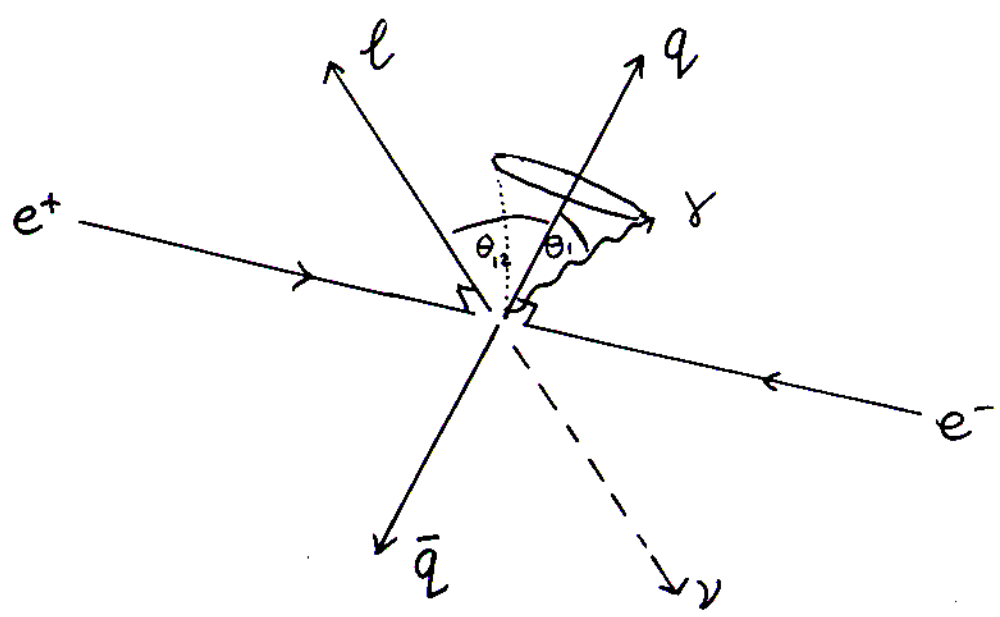
$\chi = \frac{\Gamma_w^2}{\Gamma_w^2 + \omega_\gamma^2}$



$\chi = 0$ (no QED interconnection)

$\chi = 1$ (Instantaneous interconnection)

- Normalization at small θ_1 , cuts $\theta_{12} > \theta_{cut} \Rightarrow \theta_1 > \theta_0$



excitation cross-section

$$\chi = \frac{\Gamma_W^2}{\omega_\gamma^2 + \Gamma_W^2}$$

- To achieve a higher event rate there is a great demand for (at least one) hadronically decaying W
- Subject to additional experimental problems

price to pay - limited statistics
NEED TO UTILIZE ALL EVENTS

$\int d\Omega_x$



$$\omega \frac{dN^{(\alpha\beta)}}{d\omega} = \frac{\alpha}{\pi} [R_{\text{ind}}^{(\alpha\beta)} + 2\chi(\omega)F^{(\alpha\beta)}(\theta_{12})],$$

where $(\alpha\beta) = (ll), (ql), (qq)$. The important point is that the first, χ -independent term does not depend or depend on θ_{12} . At $\theta_{12} > \theta_{\text{crit}}$ radiation is enhanced.
 $\theta_{12} < \theta_{\text{crit}}$ (suppressed)

ql, qq - $\theta_{\text{crit}} \approx 47.4^\circ$ (q and \bar{q} -jets not discriminated)
ll - $\theta_{\text{crit}} \approx 74.7^\circ$

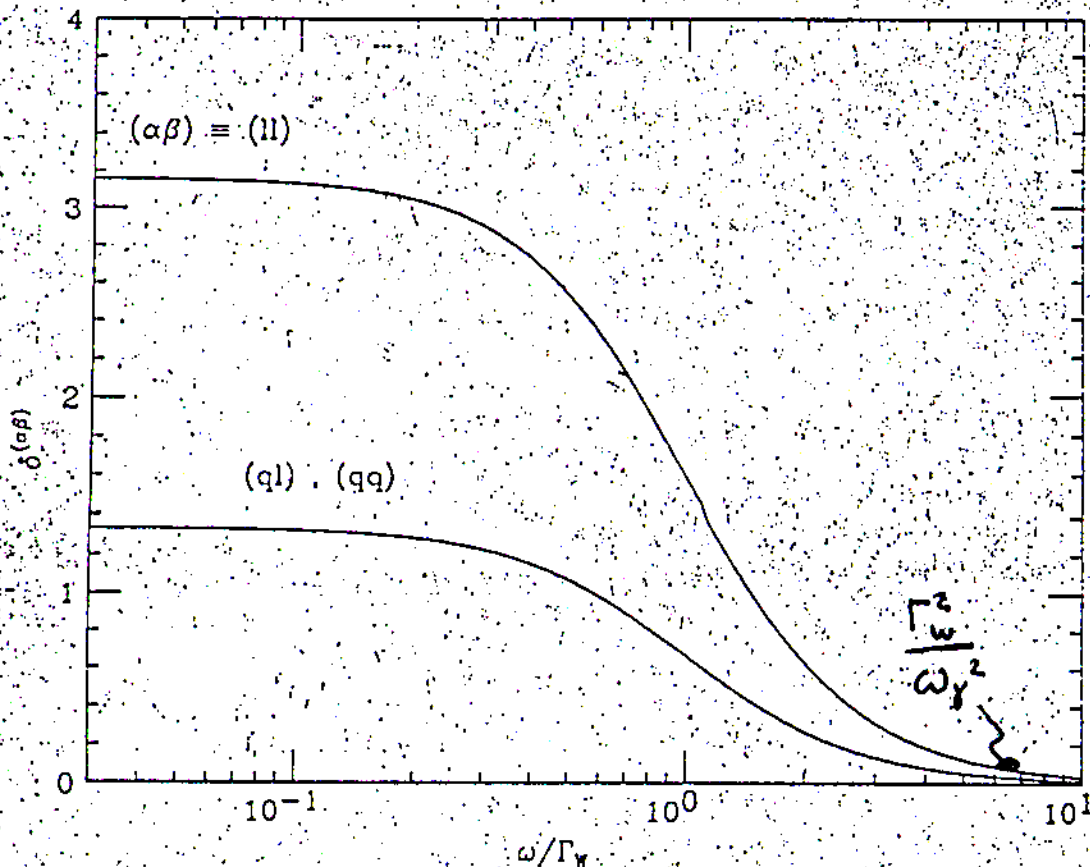
$$\delta^{(ll)} = \frac{1}{1 + \cos \theta_{\text{crit}}} \int_{\theta_{\text{crit}}}^{\pi} \omega \frac{dN^{(ll)}}{d\omega} \sin \theta_{12} d\theta_{12} - \frac{1}{1 - \cos \theta_{\text{crit}}} \int_0^{\theta_{\text{crit}}} \omega \frac{dN^{(ll)}}{d\omega} \sin \theta_{12} d\theta_{12},$$

$$\delta^{(ql,qq)} = \frac{1}{1 - \cos \theta_{\text{crit}}} \int_{\theta_{\text{crit}}}^{\pi/2} \omega \frac{dN^{(ql,qq)}}{d\omega} \sin \theta_{12} d\theta_{12} - \frac{1}{\cos \theta_{\text{crit}}} \int_0^{\theta_{\text{crit}}} \omega \frac{dN^{(ql,qq)}}{d\omega} \sin \theta_{12} d\theta_{12},$$

then the χ independent term in (17) cancels and we are left with

$$\delta^{(ll)} = \frac{\alpha \cdot 4\chi(\omega)}{\pi (1 + \cos \theta_{\text{crit}})} = \frac{\alpha}{\pi} 3.164\chi(\omega),$$

ISR cancels



$\delta^{(\alpha\beta)}$ in units of $\frac{\alpha}{\pi}$

assuming $\mathcal{L} = 10^{34}$ and 10^7 s year

→ $\int \mathcal{L} = 100 \text{ fb}^{-1}$

→ $10^6 W^+W^-$ (possibly more)

- optimal \sqrt{s} , using polarized beams
 (~ 1.5) much more flexibility in \sqrt{s} as compared to threshold scan (~ 3)

- BRP is less sensitive to beam-induced effects

$WW \rightarrow$	'BR'	
$l\nu l\nu$	10.5%	gold-plate
$q\bar{q}l\nu$	44%	$\mu^+\mu^-$ events
$q\bar{q}q\bar{q}$	45.5%	

- $q\bar{q}$ - 'indirect' photons from hadron decays
 (but practically insensitive to the event geometry)
 QCD interconnection

Not very severe requirements on

$\frac{\Delta\theta_x}{\theta_x} > \frac{\Delta E_x}{E_x}$, primary lepton/quark directions

Experimental partners are WANTED

NON-EXPERT ROUGH ESTIMATES

$$\int \mathcal{L} = 100 \text{ fb}^{-1} \rightarrow N_{WW} \sim 10^6$$

$$N_0^\gamma = \frac{\alpha}{\pi} N_{WW} \sim 2.5 \text{ k}$$

$$(N_0^\gamma)^{(ee)} \sim 250 \quad (N_0^\gamma)^{(qe)} \sim 1 \text{ k} \quad (N_0^\gamma)^{(qq)} \sim 1 \text{ k}$$

- Optimal \sqrt{s} + polarization ~ 5
- fully hadronic decays $?$
- Optimised FS characteristics $?$ (to be studied)
- Higher $\int \mathcal{L}$ $?$

$$(\omega)_{\min} \sim 300 \text{ MeV}$$

Efficiencies, cuts - need systematic (MC) studies $\sim (50-75\%) ?$

Possible strategy

- keep away from the 'main stream' directions (beams, final leptons, jets) $\theta_{\text{cut}} \sim 10-20^\circ$
- separate events with $\theta_{12} > \theta_{\text{cut}}$ and $\theta_{12} < \theta_{\text{cut}}$
- study the difference in a few ω_γ -intervals

If $\omega_0 < \omega_\gamma < \omega_{\text{mix}} \Rightarrow \Gamma_W$

$$f_{(ee)} \sim 3.5 \cdot 10^{-4} \ln \left(1 + \frac{\Gamma_W^2}{\omega_0^2} \right)$$

$$f_{(qe)} \sim 6 \cdot 10^{-4} \ln \left(1 + \frac{\Gamma_W^2}{\omega_0^2} \right)$$

Concluding Remarks

- Soft photon BRP in WW production near threshold is a sensitive tool to probe Γ_W .
FSR, IRS/FSR
- By no means, being obviously statistically competitive for precise determining the W width.
may appear to be only a complementary approach (though with a different systematics)
- Further studies are worth pursuing.
On the theoretical side: validity of approximations ($\beta_W^2 \ll 1 \dots$), optimized configurations, energies...
On the experimental side: detector capabilities, dedicated electromagnetic calorimeter, optimized event rates...
[A. Chopovsky + VAK]



Recall: TRADITIONAL STRATEGIES ARE NOT WITHOUT THEIR OWN CAVEATS