

**QCD AT A HIGH-ENERGY
 e^+e^- LINEAR COLLIDER**

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Representing

The QCD/ $\gamma\gamma$ Working Group

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Thanks to all the participants!

ECFA/DESY Workshop: Oxford

March 22 1999

MAIN QCD GOALS AT LINEAR COLLIDER

- **Precise test of QCD at highest energies**

In particular:

- **Precise determination of α_s :**

Event shape observables

- studied at PETRA, PEP, TRISTAN, SLC, LEP

$\sigma_{\bar{t}t}$ at and above threshold

- completely new domain!

- **Combining $\alpha_s(500)$, $\alpha_s(800)$ with low-energy meas.**

⇒ map out QCD ren. group trajectory

⇒ **constrain 'GUT scale'**

- limited currently by α_s uncertainty

- **Lower-energy running, eg. at Z^0 , very attractive:**

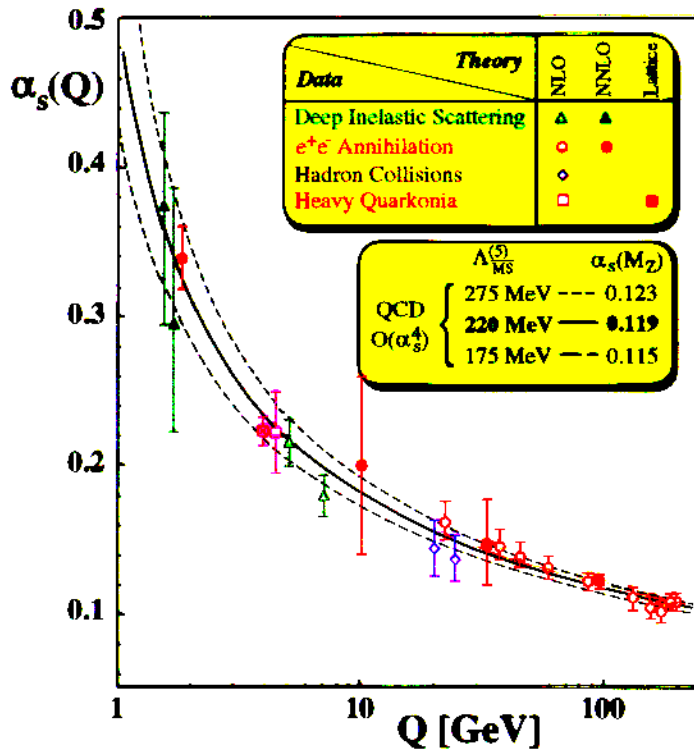
⇒ longer lever-arm in Q^2

⇒ α_s measurements with common systematics

- benefit needs to be quantified

Bethke
 Sept. 1998

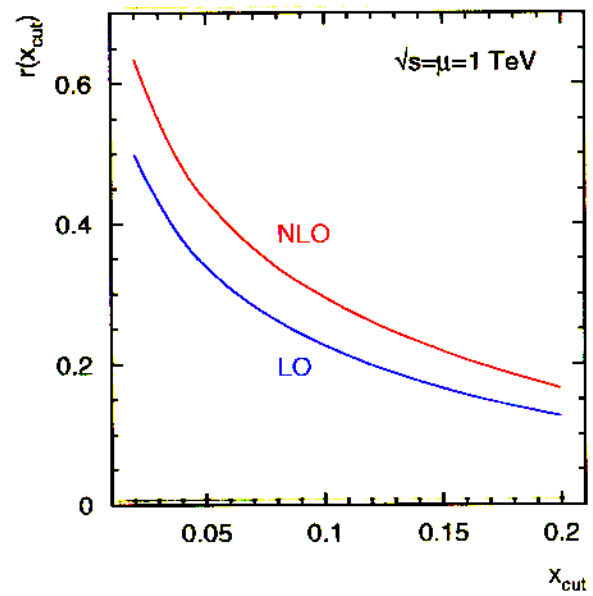
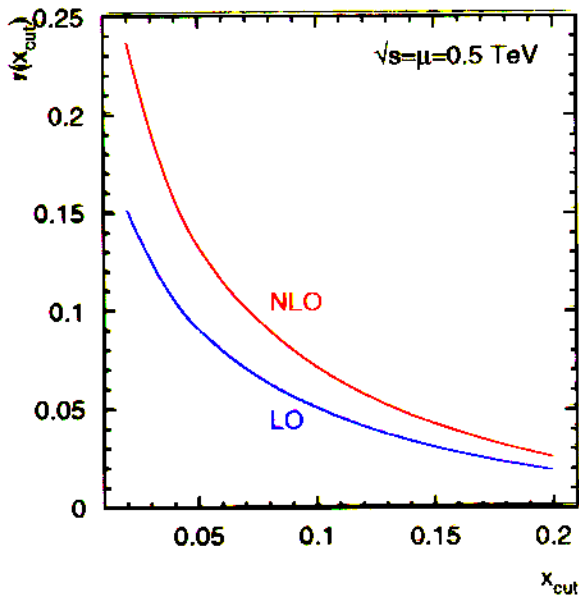
$$\alpha_s(M_Z) = 0.119 \pm 0.004$$



RECENT THEORETICAL DEVELOPMENTS

- $\sigma_{t\bar{t}}$ near threshold @ NNLO
(Beneke, Hoang, Teubner *et al.*)
important for $M_t + \alpha_s$ determination
- $e^+e^- \rightarrow 6$ jets @ LO (Moretti)
background to $t\bar{t}$, $Z^0(H^0 \rightarrow W^+W^-) \dots$
- $e^+e^- \rightarrow X b\bar{b} W^+W^-$, $X = H^0, Z^0, g$ @ LO (Moretti)
backgrounds to $t\bar{t} H^0$
- $e^+e^- \rightarrow q\bar{q}g, g \rightarrow b\bar{b}$ @ NNL (Miller, Seymour)
background to $Z^0 H^0, t\bar{t} \dots$
- b -quark forward-backward asymmetry @ 2 loops
(Seymour)
- $e^+e^- \rightarrow t\bar{t}g$ @ NLO (Brandenburg)

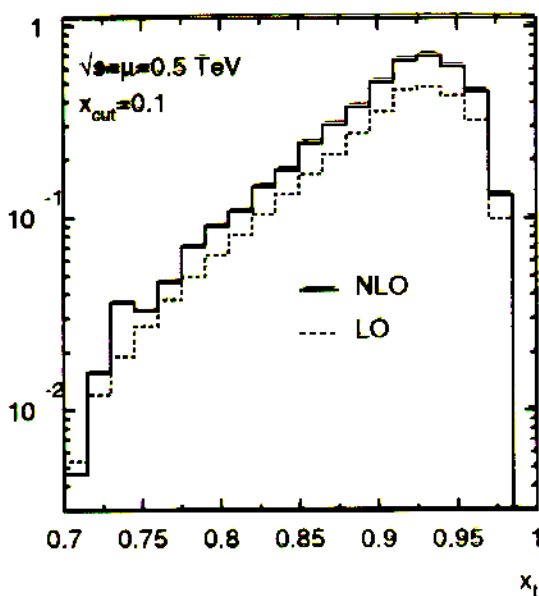
Results: Fraction $r(x_{\text{cut}})$



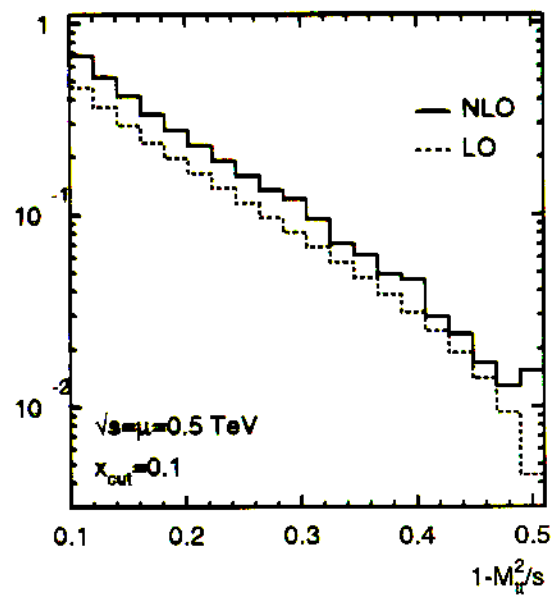
Results: Distributions

Top quark (scaled) energy $x_t \equiv 2E_t/\sqrt{s}$ and (scaled) "gluon energy" $x_g \equiv 1 - M_{t\bar{t}}^2/s$ distributions

$$\frac{1}{\sigma_{\text{tot}}} \frac{d\sigma(x_{\text{cut}}=0.1)}{dx_t}$$



$$\frac{1}{\sigma_{\text{tot}}} \frac{d\sigma(x_{\text{cut}}=0.1)}{d(1-M_{t\bar{t}}^2/s)}$$



LINEAR COLLIDER α_s MEASUREMENT

1. Event Shape Observables

- Studied at Snowmass 96 (Burrows *et al.*, SLAC-PUB-7371)

- This Workshop: O. Biebel

- Statistics:

50k $q\bar{q}$ events $\Rightarrow \Delta\alpha_s \leq 0.001$

- Detector systematics:

currently $\Delta\alpha_s \sim 0.002$

Excellent tracking + calorimetry $\Rightarrow \Delta\alpha_s \sim 0.001$

- Hadronisation uncertainties $\sim 1/Q$

At $Q = 500$ GeV $\Rightarrow \Delta\alpha_s < 0.001$

- Limiting precision:

Higher-order pQCD contributions: $\Delta\alpha_s \sim 0.006$

\Rightarrow NNLO calculation needed

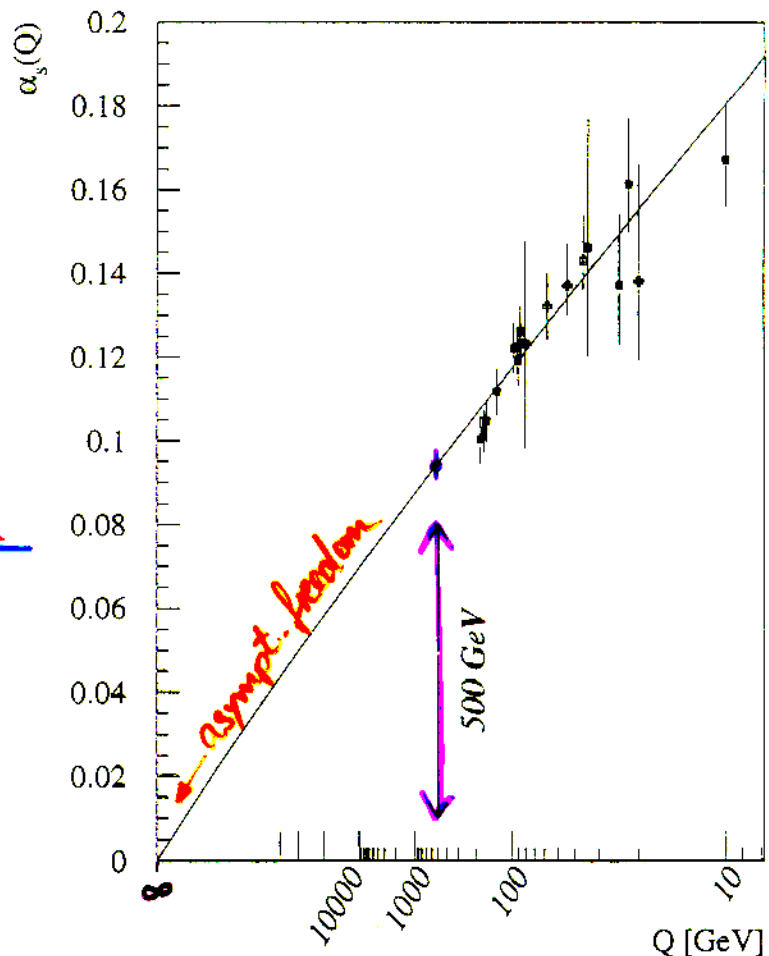
Conclusion

- QCD studies @ MC : significant test of QCD
 - ⊕ diminished hadronization effects
 - ⊕ net statistics limited
 - ⊕ ISR+BS+FSR : window to lower energies
 - ⊖ fight WW, ZZ, t \bar{t} background
 - ⊖ ISR+BS : dominating cross-section
 - ⊖ systematics (theory) limited
- Precision on α_s after ~ 1 yr at high lumi

$$\delta\alpha_s(500\text{ GeV}) \approx 0.0025$$

- Another big step towards

Asymptotic Freedom



LINEAR COLLIDER α_s MEASUREMENT

2. Top Quark Observables

- $\sigma_{t\bar{t}}$ near threshold

new NNLO calculations \Rightarrow (Peralta)

reduced correlation $\alpha_s \leftrightarrow M_t$ $\Delta\alpha_s = 0.002$

PRELIMINARY, NO THEORY UNCERTAINTY

- $\sigma_{t\bar{t}}$ above threshold (Bernreuther)

PRELIMINARY study of NLO calculations

$\sqrt{s} \approx 400$ GeV: $\Delta\alpha_s = 0.005$

(theory limiting)

$\sqrt{s} \geq 500$ GeV: $\Delta\alpha_s = 0.012$

(exp. syst. limiting)

- $e^+e^- \rightarrow t\bar{t}g$ (Brandenburg)

LINEAR COLLIDER α_s MEASUREMENT

3. Lower-energy running offers new possibilities:

- Z^0 decay widths: $\Gamma_Z^{had}/\Gamma_Z^{lept}$

calculated at NNLO

current precision, 16M Z^0 at LEP: $\Delta\alpha_s = 0.003$

100M $Z^0 \Rightarrow \Delta\alpha_s = 0.001$ (?)

- τ decay widths: $\Gamma_\tau^{had}/\Gamma_\tau^{lept}$

calculated at NNLO

current exp. precision, LEP+CLEO: $\Delta\alpha_s = 0.001$

theoretical uncertainties $\Rightarrow \Delta\alpha_s = 0.003$ (?)

OTHER IMPORTANT TOPICS

- **Limits on new coloured objects (eg. gluino)**
above threshold \Rightarrow modify $\alpha_s(Q)$
- **Limits on anomalous strong top-quark couplings**
 \Rightarrow modify gluon energy in $t\bar{t}g$ events
- **Measurement of Γ_t using $t\bar{t}g$ events**
 \Rightarrow Γ_t affects degree of soft-gluon coherence
- **Polarisation-based asymmetries in $q\bar{q}g$ events:**
$$\vec{P}_e \cdot \vec{k}_{q1} \times \vec{k}_{q2} \quad (\text{CP+ T-})$$
$$\vec{P}_e \cdot \vec{k}_q \times \vec{k}_{\bar{q}} \quad (\text{CP- T-})$$

 \Rightarrow Search for anomalous final-state interactions
- **Particle multiplicity in heavy- vs. light-quark jets**
 \Rightarrow add long lever-arm to current tests

All warrant updated simulations

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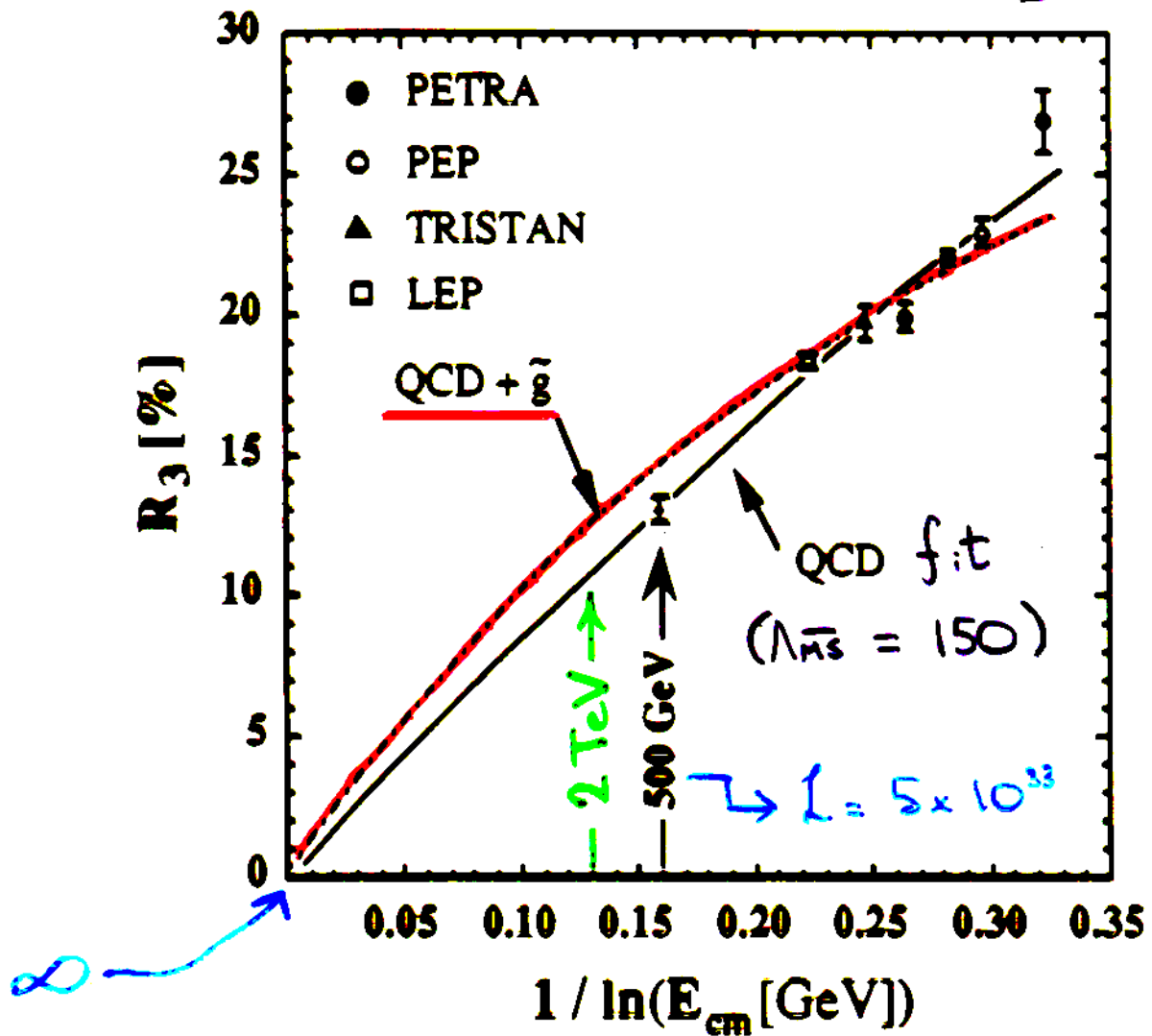


Fig. 4. Three-jet event production rates as a function of $1/\ln(E_{cm})$, measured with the JADE jet finder for a constant jet resolution of $y_{cut} = 0.08$.

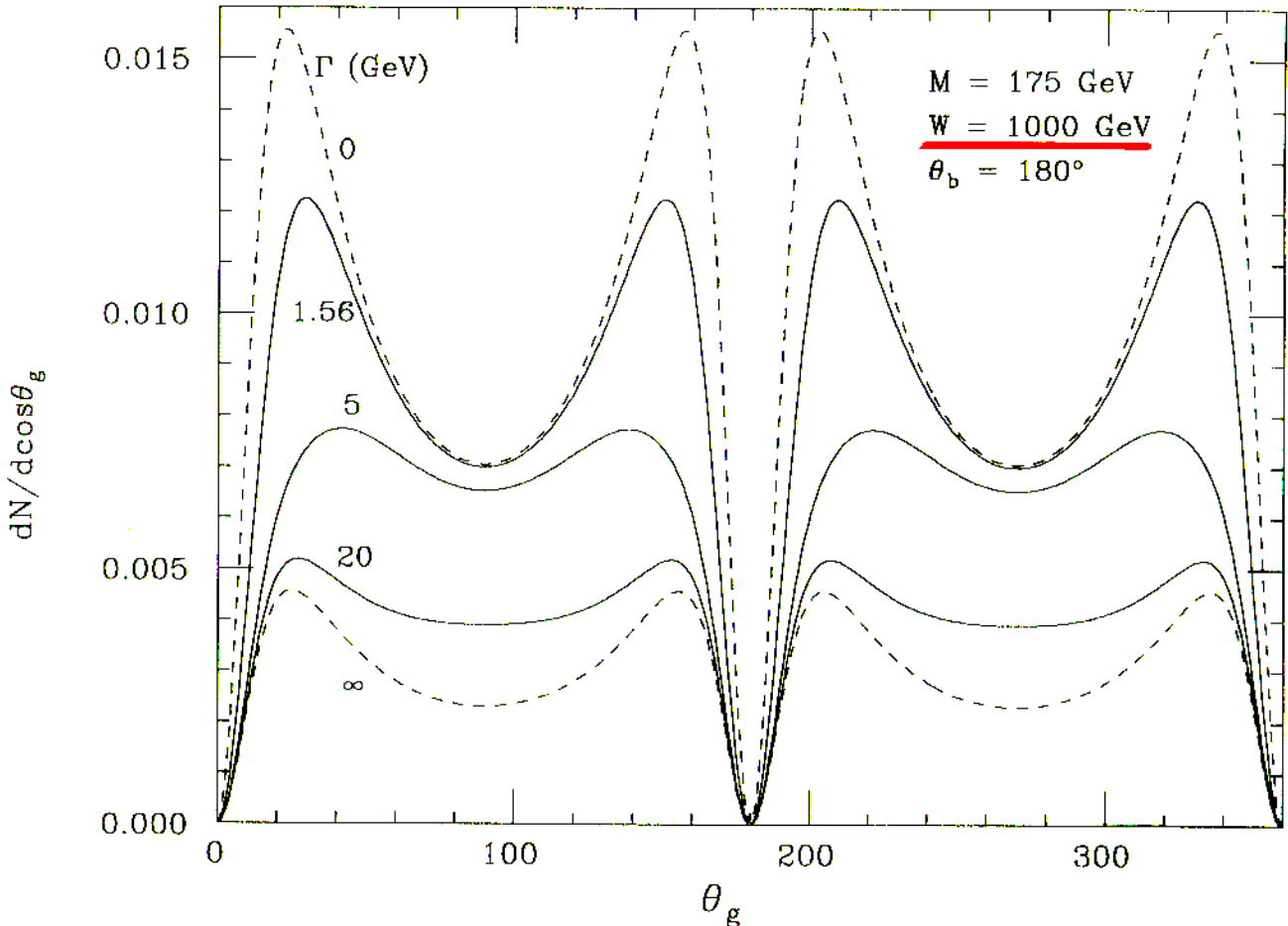
Light gluinos: $N_f \rightarrow N_f + 3N_{\tilde{g}}$

Precision (probably) limited by
 LOWER ENERGY DATA!

L. Orr et al.

Update: $m_t = 175 \text{ GeV}$

$$\Theta_b = 180^\circ$$



Emission Δ of 5 GeV gluons

Realistic simulation needed!

$$\Rightarrow \Delta\Gamma_t$$

EVENT SELECTION

- Multijet $q\bar{q}$ events bgd. to $t\bar{t}$, W^+W^- , $Z^0 H^0$, ...
- Separation of $q\bar{q} / t\bar{t} / W^+W^- / Z^0 Z^0 / \dots$ not trivial
- For QCD studies: $q\bar{q} /$ the rest
 $t\bar{t} /$ the rest
- Hawaii 93: kinematic cuts \Rightarrow 83% pure $q\bar{q}$ sample,
but with large bias
- Snowmass 96: eliminate W^+W^- events with right-handed e^- beam
 $P_c = +90\% \Rightarrow$ 87% pure $q\bar{q}$ sample
with zero bias
- To do:
effect of highly efficient b-tag on $q\bar{q} / t\bar{t}$ separation

SUMMARY

- **'QCD events' \Rightarrow background to new physics**
ultimately need to measure and understand them
- **Good progress: several new pQCD calculations**
- **Key QCD meas. exploit high energy + lumi:**
Precise α_s and $\alpha_s(Q^2)$
 \Rightarrow Test QCD at highest Q^2
 \Rightarrow Constrain QCD RGE trajectory + GUT scale
- **Low energy running attractive**
- **Strong overlap of interest with Top Group**
- **Several important measurements deserve modern simulations**