

ECFA / DESY Linear Collider Workshop
20-23 March 1999

Top Quark WG

Plenary Review

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+ Gonzalo Merino (IFAE)

Plan:

0. Thanks to everybody who contributed!
1. What is top?
2. Threshold Studies
3. top in the continuum
4. Sitges and beyond
5. G. Merino: Simulation of $e^+e^- \rightarrow t\bar{t}H$

1. What is top?

- the heaviest known particle plays a special role in EWSB

→ $\Delta m_t \stackrel{!}{\lesssim} 200 \text{ MeV} \implies \frac{\Delta M_H}{M_H} \lesssim 17\%$

→ test of EWSB

→ $\frac{\Delta m_t}{m_t} \sim 1\%$ (several % for b)

$\lambda_t^2 \stackrel{!}{\sim} 0.5$ ($\lambda_b^2 \sim 4 \cdot 10^{-4}$)

top as the key to Physics beyond the SM that links masses + mixings, $q + l$?!

- the only free quark: $\Gamma_t \sim 1.5 \text{ GeV}$ decays before hadron. $\gg \Lambda_{\text{QCD}}$

→ "clean" QCD @ high scales

→ + spin physics!

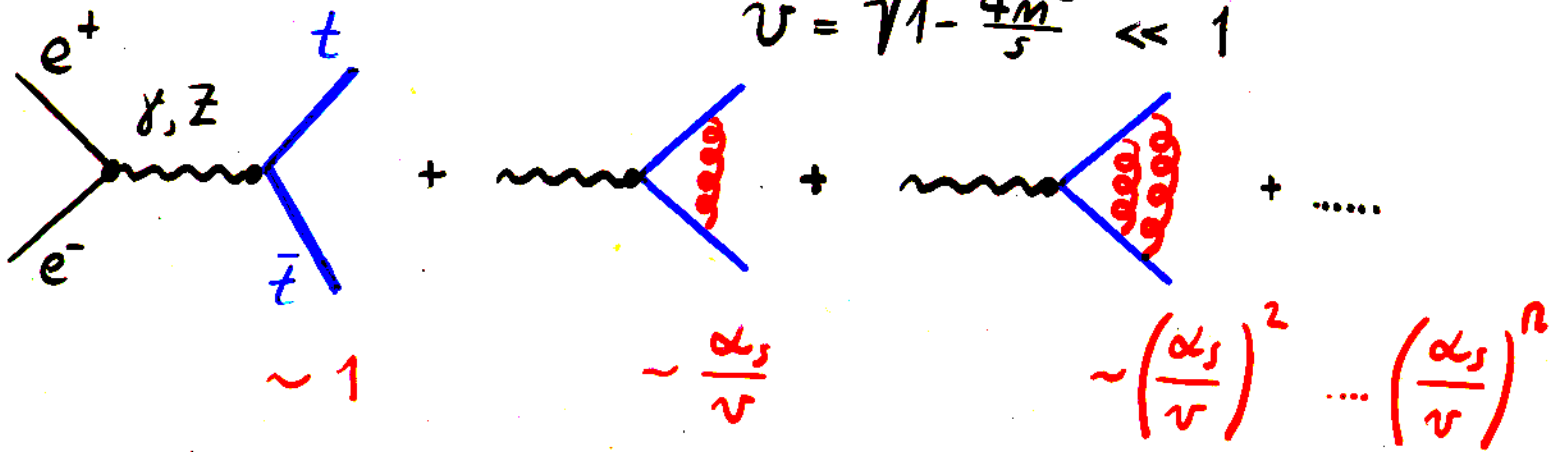
- anything else? non SM coupling? $\dots \rightarrow \alpha_s$

→ better check it ...

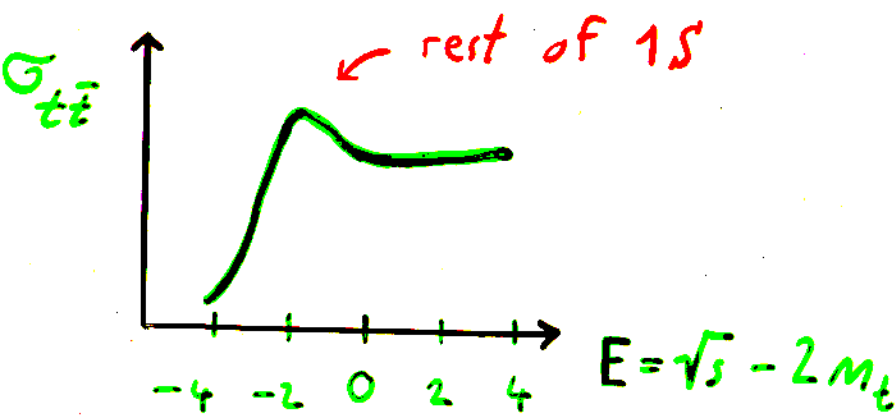
2. Threshold Studies

allow for the most precise determination: $\sqrt{s} \approx 2m_t \rightarrow m_t$

$$v = \sqrt{1 - \frac{4m_t^2}{s}} \ll 1$$



Strong coulombic interaction near threshold \rightarrow ~~resonances~~

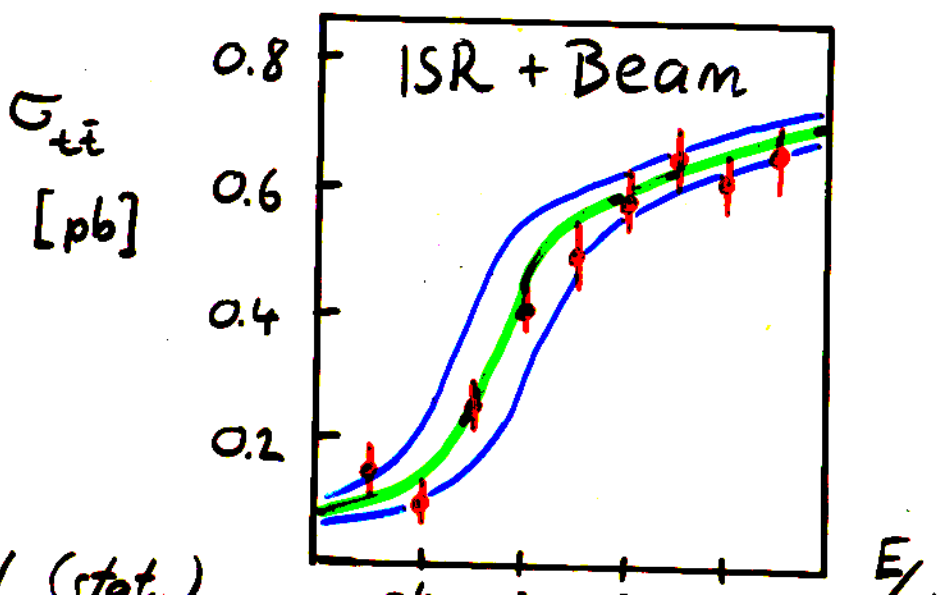


Γ_t smears them out

Still: fit steep rise of $\sigma_{t\bar{t}}$ to measure m_t :

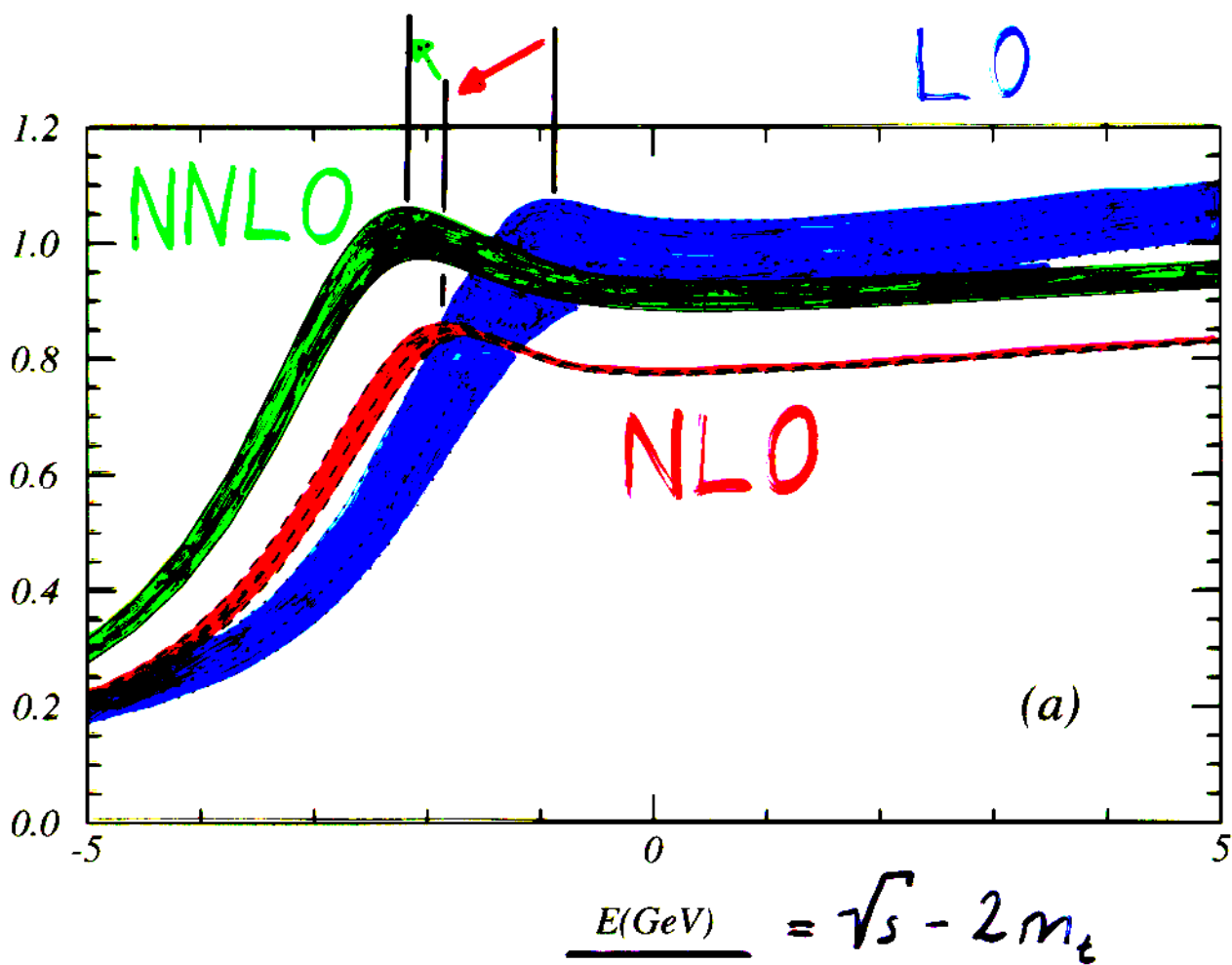
9-point fit with data:
theory

$m_t \pm 400 \text{ MeV}$
 $\rightarrow \Delta m_t \sim 120 \text{ MeV (stat)}$



$$\frac{\sigma(e^+e^- \rightarrow t\bar{t})}{\sigma(e^+e^- \rightarrow \mu^+\mu^-)} \text{ in fixed}$$

L, NL, NNLO order +
scale dependence

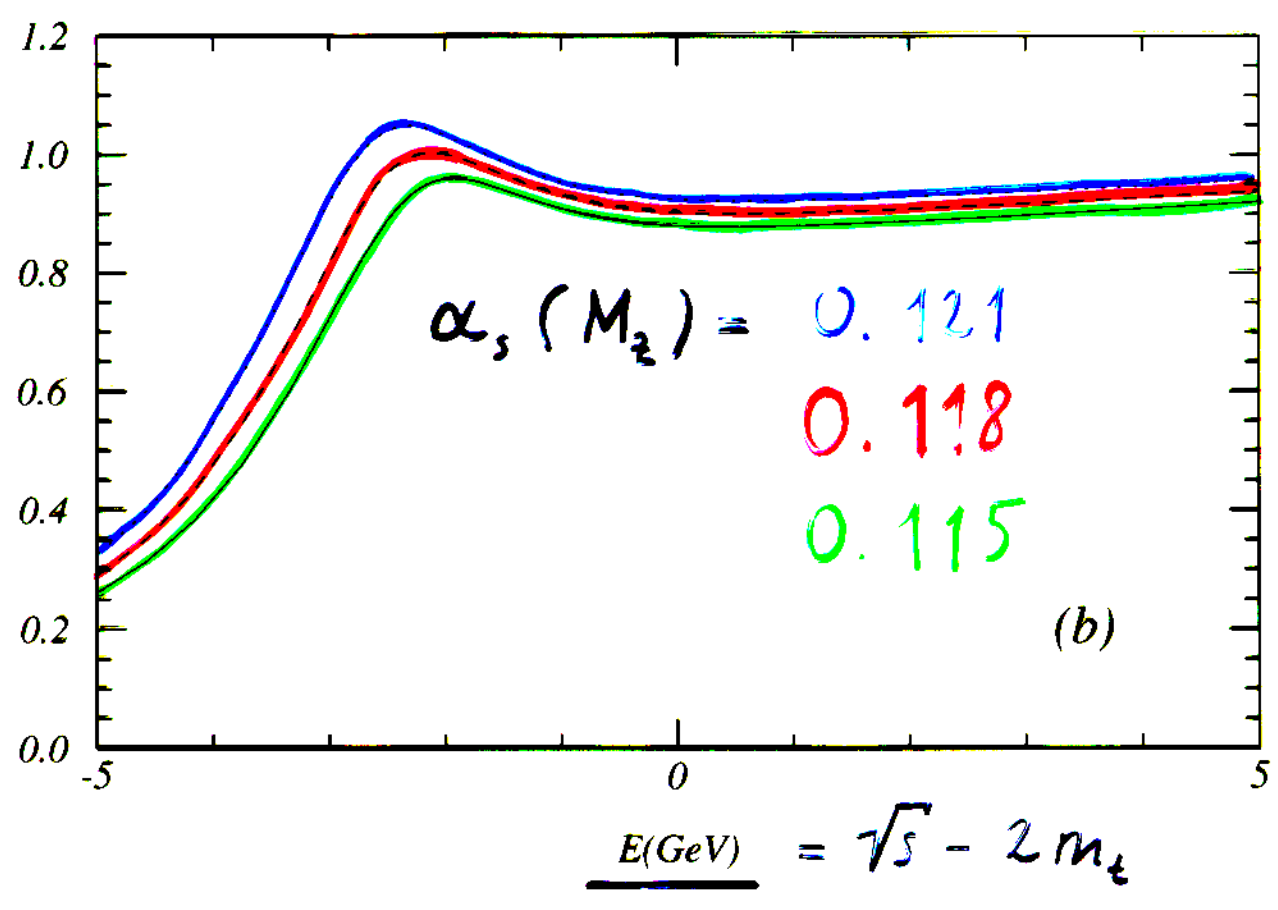


Hoang,
TT

scale $\mu_{\text{soft}} = 50 / 75 / 100 \text{ GeV}$

$$\frac{\sigma(e^+e^- \rightarrow t\bar{t})}{\sigma(e^+e^- \rightarrow \mu^+\mu^-)} \quad \text{in NNLO}$$

Hoang,
TT



In the past:

Fit σ_{tot} , $\frac{d\sigma}{dp_t}$ (A_{FB}) to get

m_t , α_s (Γ_t) with very high
120 MeV 0.003 5% ← accuracy.

Recently ('98 → '99, situation at Orsay, Lund):

NNLO ($O(\alpha_s^2, \alpha_s v, v^2)$) corrections are large!

Hoang, TT
Melnikov, Yelkovsky
Yakovlev
Beneke, Signer, Smirnov

large theoretical uncertainties ?

(normalization, "1S peak") the problem plot →

Δm_t (theory) = ? what to do?

$\Delta \alpha_s$ (theory) = ? Think again:

What is m_t ?

Here: m_t^{pole} ... but

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Now we know :

- m^{pole} is NOT an observable.

Only defined up to $\mathcal{O}(\Lambda_{\text{QCD}})$
(despite large Γ_t)

- But: $E_{\text{static}} = 2m + E_{\text{binding}}$ is as a physical observable unambiguous.
(but m_{xyz} and $V_{xyz}(\tau)$ are xyz scheme dependent)

And: The leading $\overline{\text{IR}}$ Renormalons cancel in

$$2 \cdot \text{[Diagram 1]} + \text{[Diagram 2]} = 0$$

The diagram shows two terms. The first term is a horizontal line with a semi-circular arc of red circles above it. The second term is a wavy line entering from the left and splitting into two lines that meet at a vertex, with a semi-circular arc of red circles to the right of the vertex.

Beneke
Hoang et al.

- Therefore: use a suitable Short Distance Mass which is free from IR ambiguities and cures the large NNLO (NLO) corrections!

● Two recent proposals:

▶ $1S$ mass : ~ position of the $1S$ peak
(for stable quarks) Hoang et. al.

▶ PS mass : $m^{PS}(\mu_f) = m^{pole} - \delta m(\mu_f)$ Beneke

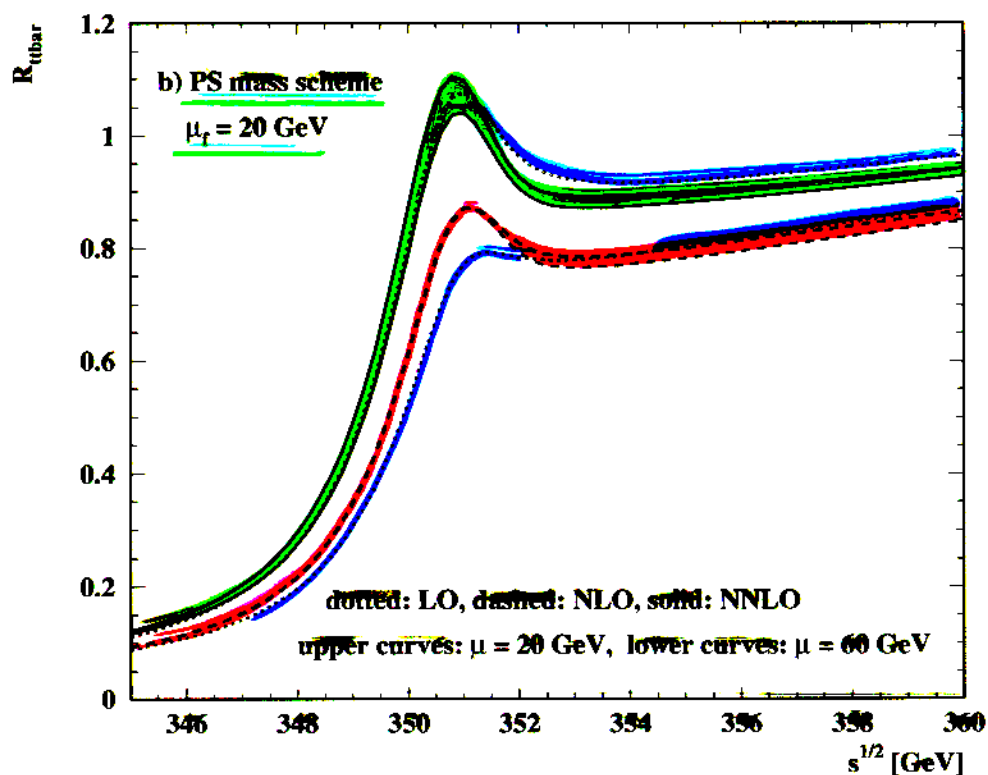
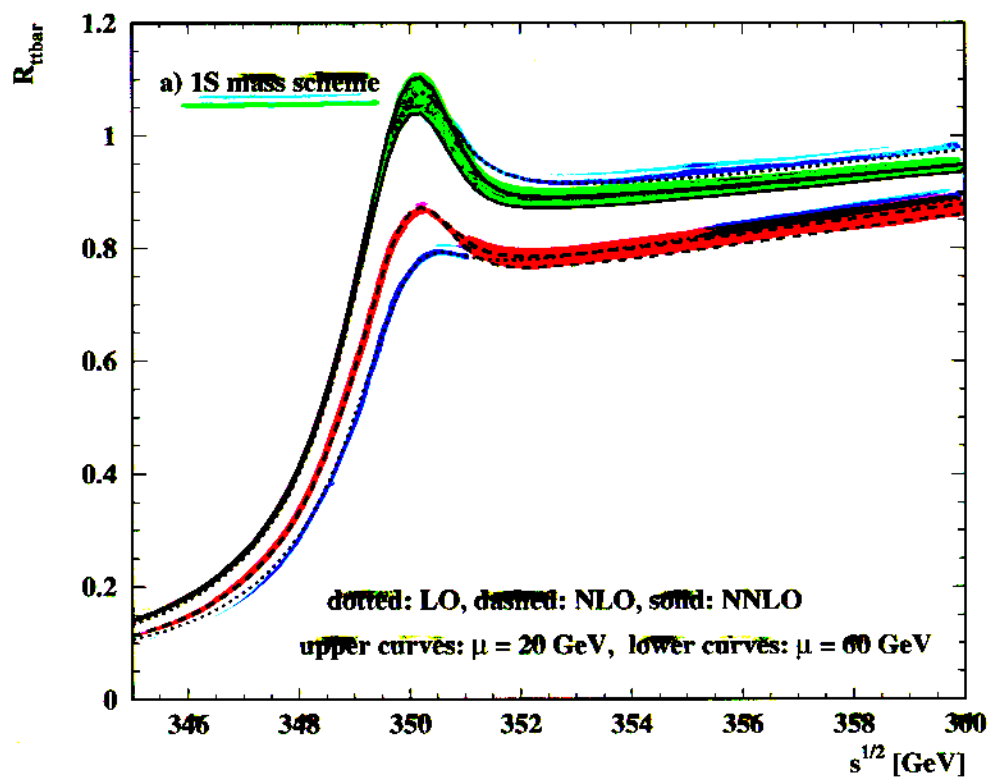
$$\delta m(\mu_f) = -\frac{1}{2} \int_{|\vec{q}| < \mu_f} \frac{d^3 q}{(2\pi)^3} \tilde{V}(q)$$

subtract the IR-part due to the potential.

Results are quite similar: the solution \rightarrow plot

Both can, as short distance masses, be reliably transformed to $m_{\overline{MS}}$ (or maybe used directly in other cases ?)

No strong 1S peak shifts from
LO \rightarrow NLO \rightarrow NNLO



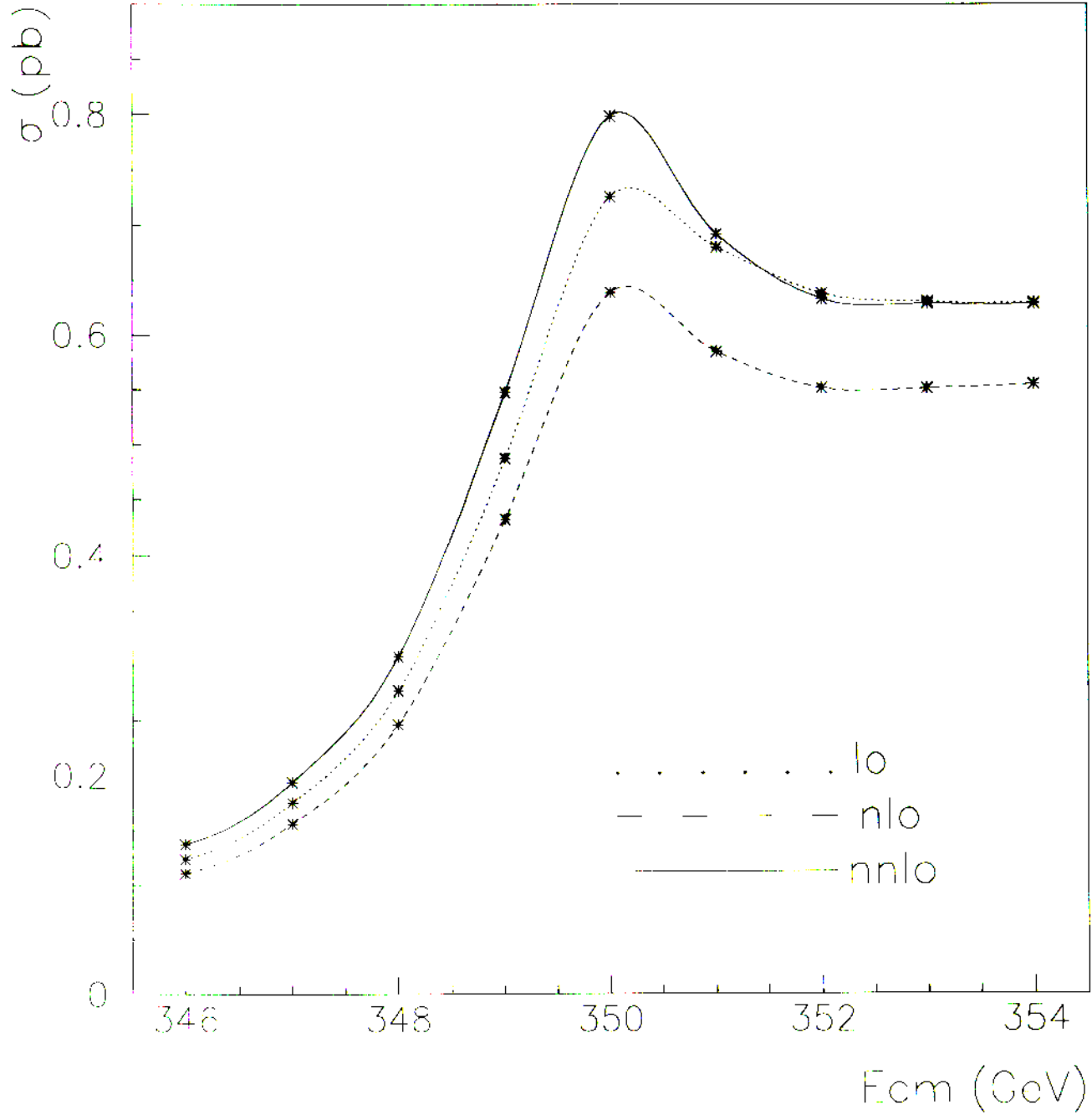
LO
NLO
NNLO

NNLO à la Hoang, TT

$m_t = 175 \text{ GeV}$

$\alpha_s = 0.920$

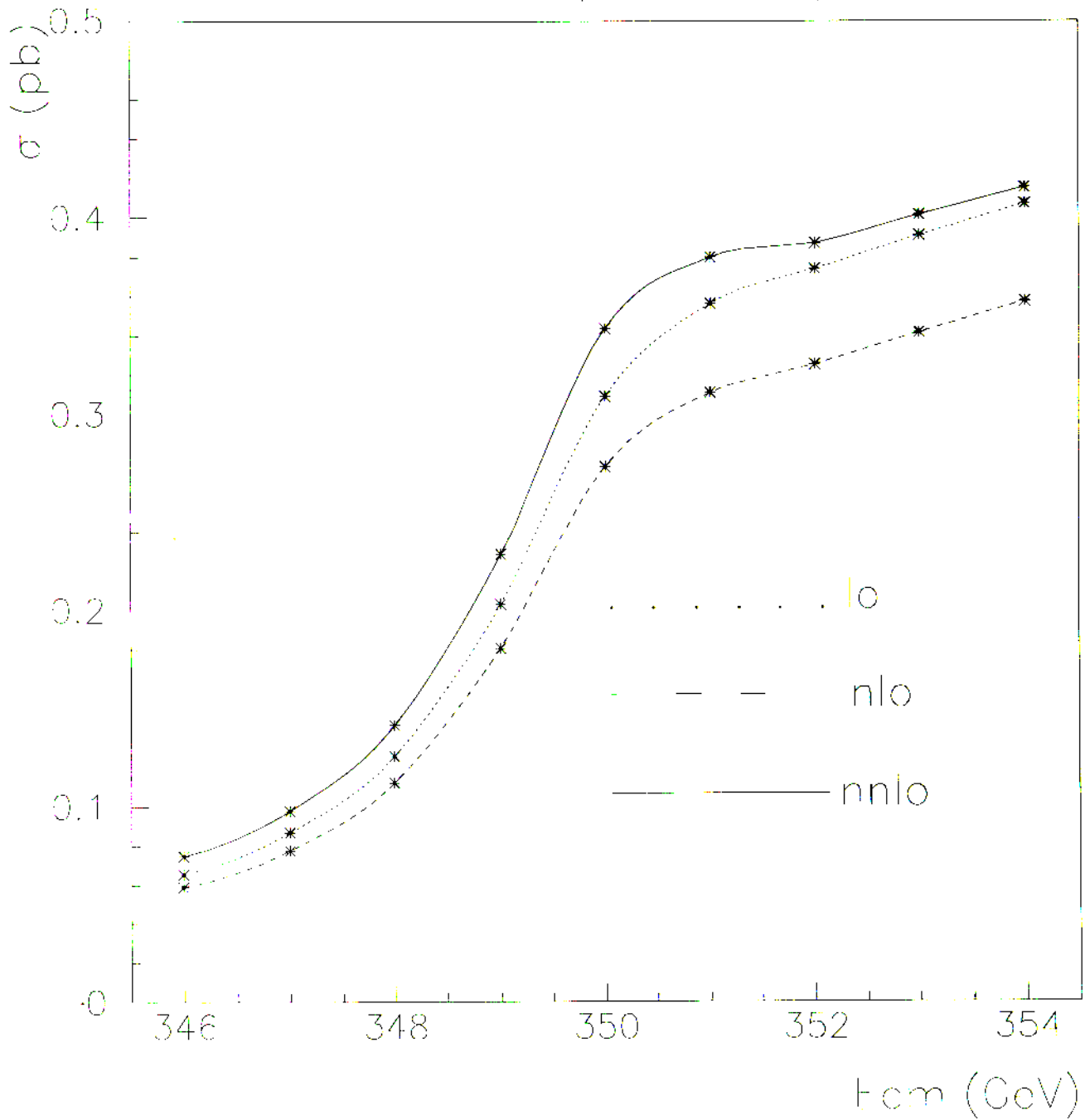
1S Mass (no ISR, no beam)



$m_t = 175 \text{ GeV}$

$\alpha_s = 0.120$

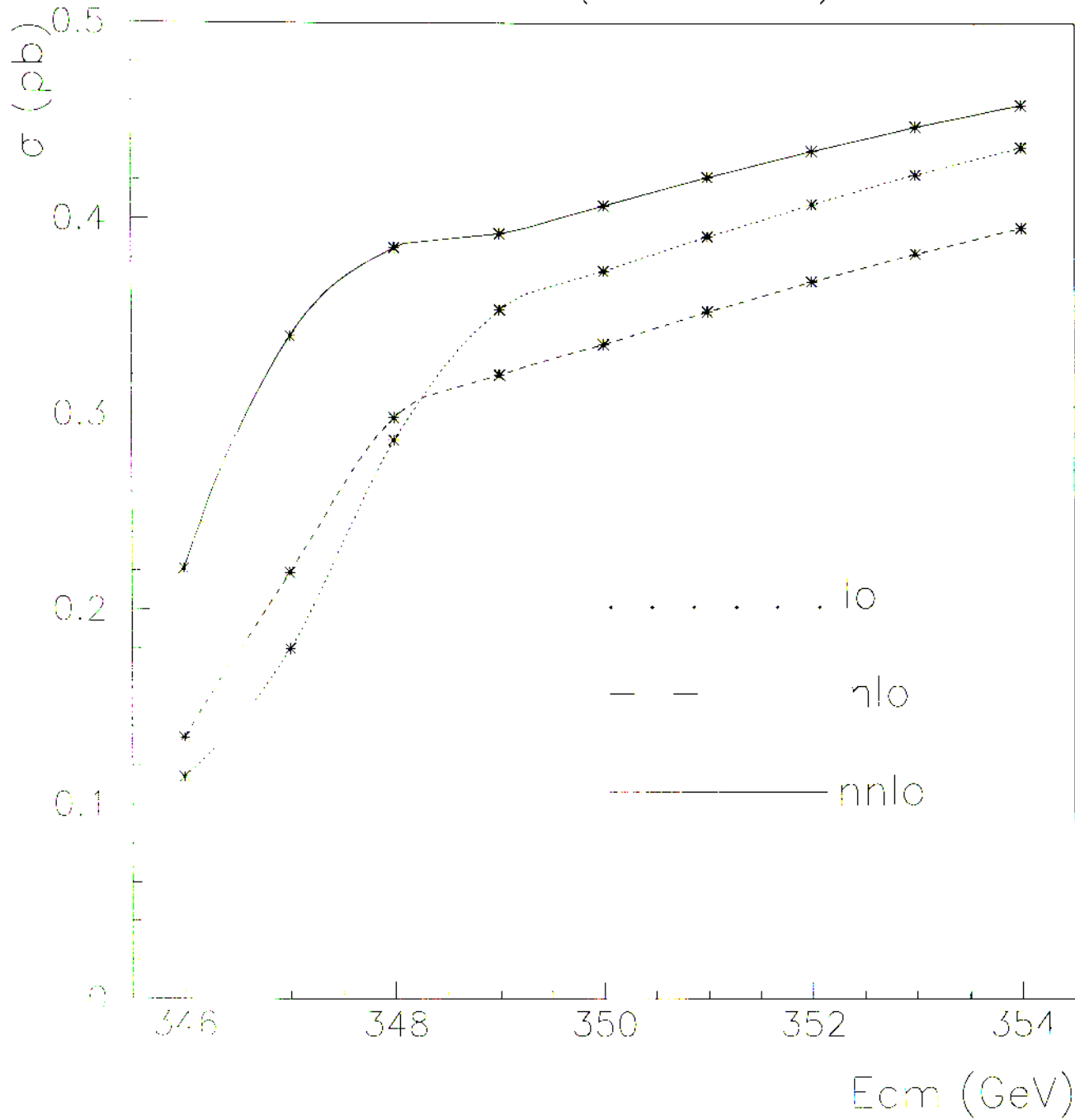
1S Mass (ISR + beam)



$m_{top} = 175 \text{ GeV}$

$\alpha_s = 0.120$

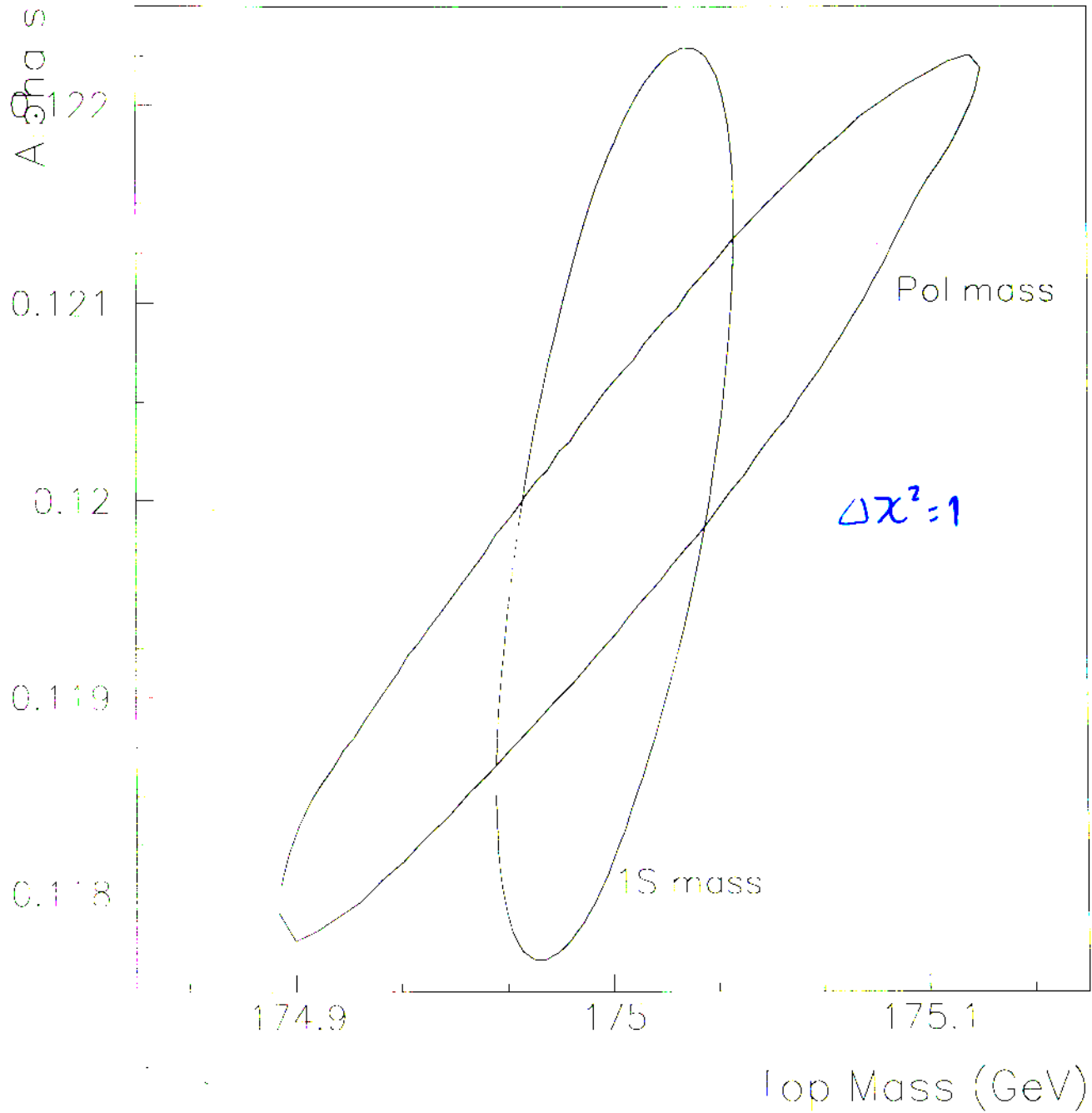
Pol Mass (ISR+beam)



$m_t = 175 \text{ GeV}$

$\alpha_s = 0.120$

Pol Mass and 1S Mass (ISR+beam). NNLO



$S_{POL} = 0.966 \rightarrow S_{1S} = 0.629$

Preliminary results of experimental analysis:

Martinez
Peralta

- $m_t \leftrightarrow \alpha_s$ correlation strongly reduced
- for $\int \mathcal{L} = 100 \text{ fb}^{-1}$ very small stat. errors for the m_t (α_s) fit ($\Delta m_t \sim 40 \text{ MeV}$) to NNLO.

Warning: This is **NOT** the total error!

- Compare different orders to estimate theoretical uncertainty:

$$\Rightarrow \Delta m_t^{\text{"theor."}} \sim 100 \text{ MeV} \quad (\text{prelim.!!})$$

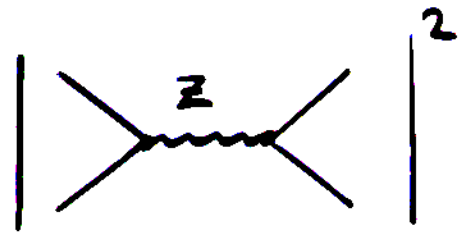
and no good α_s -error due to large corrections to the normalization (independent of mass scheme).

....> take α_s from elsewhere!

Different threshold topics:

- "Axial contributions at the top threshold"

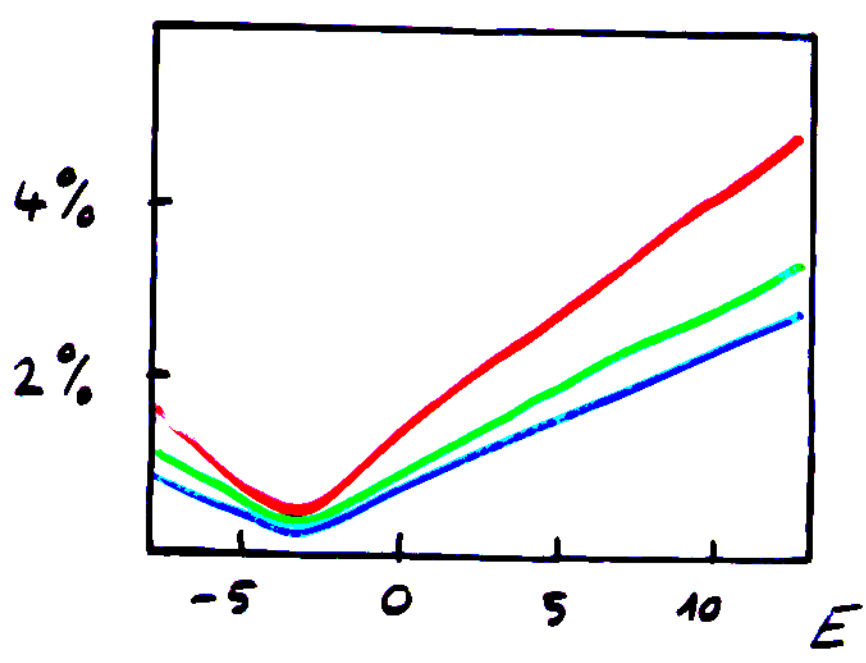
Kühn, TT



$\sim v^2$ relative to vector contributions.

Small correction, but completes the picture at NNLO and allows for an independent measurement due to e^- Polarization dependence:

$$\frac{\sigma_{AA}}{\sigma_{VV}}$$



$P_+ = 0$
 $P_- = 1$
 0
 -1

Can be included in future NNLO analyses.

● Polarization of t (\bar{t})

can be measured through energy -

angular distributions of decay L .

Harlander, Zezabek, Kühn, TT, Peter Sumino

Peter, Sumino: construction of observable sensitive only to the decay !

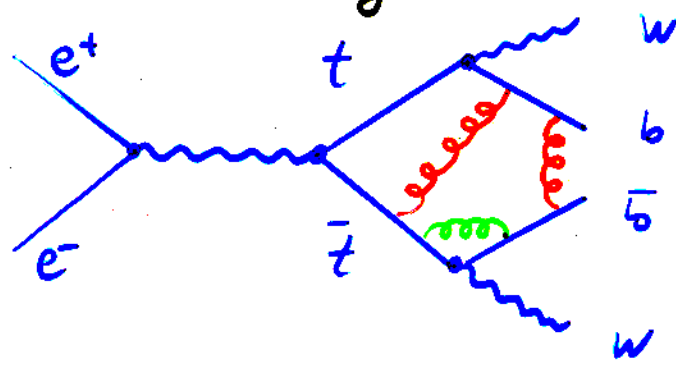
and note:

P_-	+80%	0	-20%	$(P_+ = 0)$
P_t	+60%	-40%	-90%	

But: need for experimental analysis ...

● $O(\alpha_s)$ Final state interactions

(~ rescattering ~ interconnection ~ non-factorizable)



Peter, Sumino
Yakovlev, Melnikov
Khoze, Sjostrand

Chapovskii, Beenakker, Berends

Cancel in σ_{tot} , but distort (invariant mass) distributions ! $\Delta M_{max} = -85 \text{ MeV}$

Corrections known at threshold for
 $\frac{d\sigma}{dp}$, A_{FB} , Polarization to $O(\alpha_s)$.

Peter, Sumino

3. top in the continuum

- these FSI might be important for the kinematic mass reconstruction (event by event), but

$$\Delta M_{\max} = -10 \text{ MeV} \quad \text{only}$$

at $\sqrt{s} \sim 500 \text{ GeV}$. Chapovshi et al.

- $O(\alpha_s)$ corrections to t spin-polar. and spin-correlations

Brandenburg, Flesch, Uwer
Groote, Körner, Leyva

corrections up to $\sim 5\%$:



Need for exp. analysis including hadronization and detector effects!

QCD corrections to top spin-polarization and spin-correlations*

$$e^-(\mathbf{p}, \lambda_+) e^+(-\mathbf{p}, \lambda_-) \rightarrow t(\mathbf{k}_t, \hat{\mathbf{s}}_t) \bar{t}(\mathbf{k}_{\bar{t}}, \hat{\mathbf{s}}_{\bar{t}}) X$$

$\hat{\mathbf{s}}_t(\hat{\mathbf{s}}_{\bar{t}})$ polarization vector of $t(\bar{t})$ quark, λ_{\pm} longitudinal polarization of e^{\pm} .

- In general, QCD corrections to expectation values of spin observables are small.

Examples: $m_t = 175 \text{ GeV}$, $\alpha_s \equiv 0.1$, $\lambda_+ \equiv 0$, $\lambda_- \equiv +1$,
 $\mathbf{S}_t = \frac{\boldsymbol{\sigma}}{2} \otimes \mathbb{1}$ ($\mathbf{S}_{\bar{t}} = \mathbb{1} \otimes \frac{\boldsymbol{\sigma}}{2}$) spin operator of $t(\bar{t})$.

$$\begin{aligned} 2\langle \hat{\mathbf{p}} \cdot \mathbf{S}_t \rangle |_{\sqrt{s}=500 \text{ GeV}} &= 0.8998 - 0.278 \frac{\alpha_s}{\pi} \\ &= 0.8910 \quad (\sim 1\%), \end{aligned}$$

$$\begin{aligned} 2\langle \hat{\mathbf{k}}_t \cdot \mathbf{S}_t \rangle |_{\sqrt{s}=400 \text{ GeV}} &= 0.4198 + 0.450 \frac{\alpha_s}{\pi} \\ &= 0.4341 \quad (\sim 3\%), \end{aligned}$$

$$\begin{aligned} \langle \mathbf{S}_t \cdot \mathbf{S}_{\bar{t}} \rangle |_{\sqrt{s}=1 \text{ TeV}} &= 1/4 - 0.405 \frac{\alpha_s}{\pi} \\ &= 0.2371 \quad (\sim 5\%). \end{aligned}$$

* A Brandenburg, M Flesch, P Uwer, Phys Rev D **59** (1999) 014001

● Formfactors

Bernreuther ¹² →

Also no recent exp. analysis.

Important: $\textcircled{P_{e^-}}$

● $e^+e^- \rightarrow t\bar{t} + \left\{ \begin{array}{l} g \\ Z \\ H \end{array} \right\} \rightarrow b\bar{b}$

Moretti
Corcella, Seymour →

$t\bar{t}g, t\bar{t}Z$ background for $t\bar{t}H$.

↑
radiation from b (\bar{b}) important!
M.E. correction soon in Herwig 6.1.

→ $\Delta M_{\max} = ?$ in progress.

● Complete $O(\alpha_s^2)$ + EW corrections
for $t\bar{t}$ above threshold available.

Kühn

→ large EW contributions
from box-diagrams.

→ α_s determination from
 σ_{tot} ?

Sensitivity to (non SM) form factors in $t\bar{t}$ prod. & decay:

only $t\bar{t} \rightarrow l^\pm \bar{\nu}_l + jets$ channels considered
 $l = e, \mu$

Cuts: $E_e > 30 \text{ GeV}$, $|\cos \Theta| < 0.95$

Breth = 16%, int. lumi 310 fb^{-1} (500 GeV), 500 fb^{-1} (800 GeV)

1σ stat. errors (68% CL)

$\sqrt{s} = 500 \text{ GeV}$

e^- polarization
 $p = 0$ $p = -0.8$

F_{1R}^W	0.030	0.012
$F_{2V}^{t\bar{t}}$	0.015	0.011
$\text{Re } F_{2A}^t$	0.035	0.007
$\text{Re } F_{2A}^{\bar{t}}$	0.012	0.008
$\text{Im } F_{2A}^t$	0.010	0.008
$\text{Im } F_{2A}^{\bar{t}}$	0.055	0.010
$\text{Im } F_{2R}^W$	0.025	0.010

$\leftarrow V+A$ in $t \rightarrow W b$
 \leftarrow anom. mag. "moment"

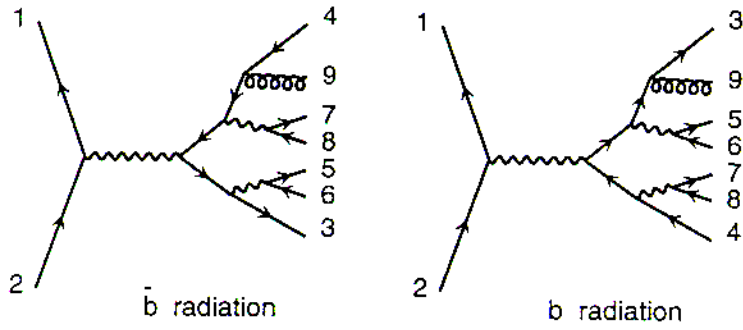
\leftarrow SF in $t\bar{t}$ production
 dipole "moment"
 $q_t^{t\bar{t}} = \frac{e}{2m_t} F_{2A}^{t\bar{t}}$

\leftarrow SF in $t \rightarrow W b$

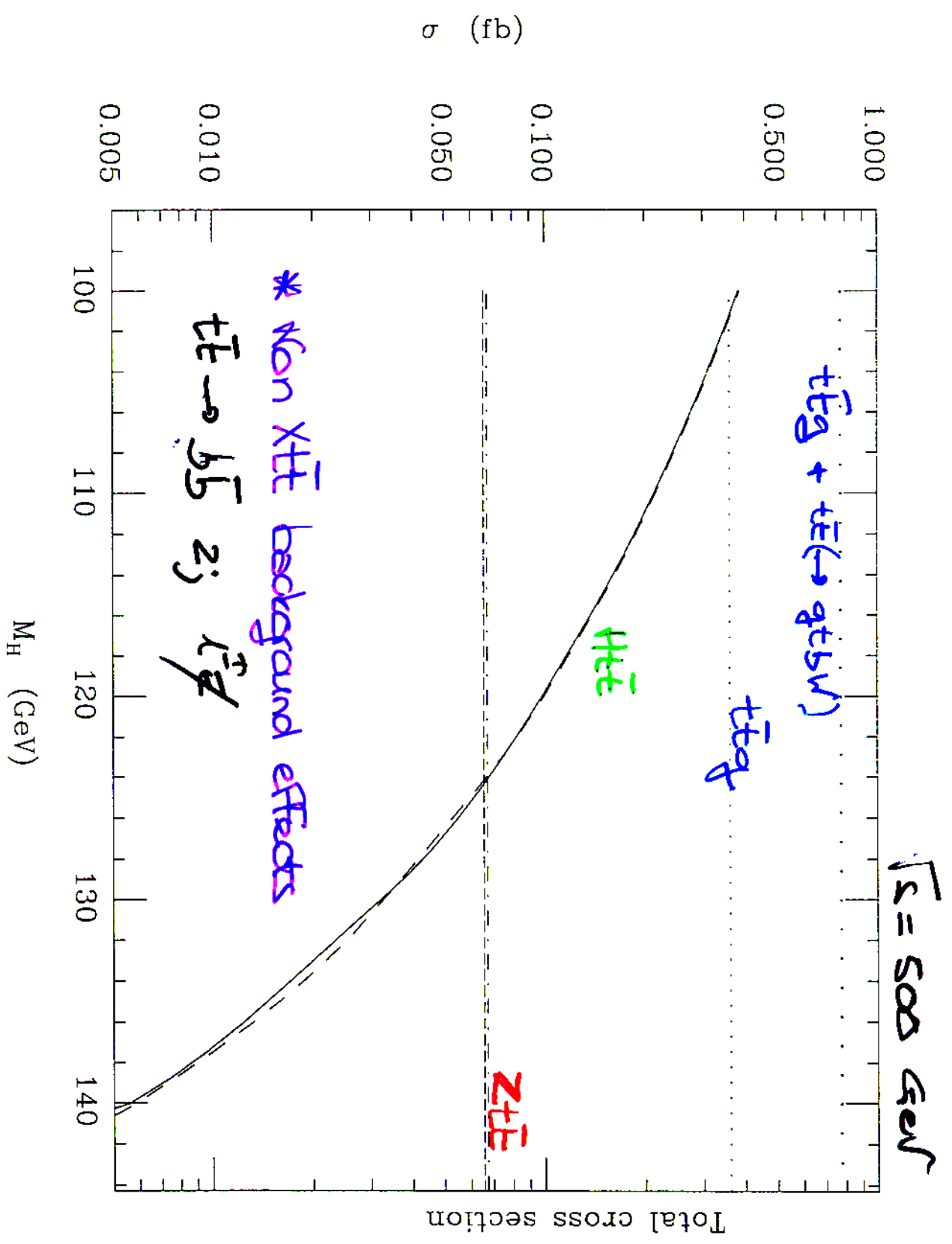
$\sqrt{s} = 800 \text{ GeV}$

$p = 0$ $p = -0.8$

$F_{2V}^{t\bar{t}}$	0.011	0.008
$\text{Re } F_{2A}^t$	0.015	0.004
$\text{Re } F_{2A}^{\bar{t}}$	0.008	0.007
$\text{Im } F_{2A}^t$	0.006	0.005
$\text{Im } F_{2A}^{\bar{t}}$	0.037	0.007



- b -radiation + \bar{b} -radiation \approx $t\bar{t}$ radiation...
(Stirling/Stelzer 1996)
- Soon in HERWIG 6.1 (ME corrections)



● Rare t decays :

Mele et al.

Guasch, Solà

Are FCNC top decays a door to SUSY physics ?

$$\text{SM: } \text{Br}(t \rightarrow c H) \approx 10^{-13}, \text{ few} \cdot 10^{-4}$$

$$\text{Br}(t \rightarrow c g) \approx 10^{-11}, \text{ few} \cdot 10^{-4}$$

in MSSM!

→ Redo exp. analysis to check for accessibility with 500 fb^{-1} .

4. Sitges and beyond

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Threshold:

- * More detailed studies of theoretical uncertainties needed:
sensitivity of the fitted m_t to order, scale in α_s , different mass definitions, different NNLO input...
- * Optimization of the scan-strategy.
- * Comparison of different calculations of nonfactorizable corrections.
Unified description for all energies?

Long term:

- * Exp. analysis of Polarization, axial contributions, formfactors, spin-correl.
- * Redo the studies for mass reconstruction above threshold.

⑤ $t\bar{t}H$...