

SUMMARY

● J. Kalinowski et al.,

Determining the SUSY parameters
in $e^+e^- \rightarrow \tilde{\chi}_i^+ \tilde{\chi}_j^-$

● G. Moortgat-Pick et al.,

$e^+e^- \rightarrow \tilde{\chi}_2^0 \tilde{\chi}_1^0$, $\tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0 + e^+ + e^-$
M' (or M₁) dependence

● S. Kraml et al.,

$e^+e^- \rightarrow \tilde{g}_i \tilde{g}_j$ $\tilde{g} = \tilde{t}, \tilde{b}$
Parameter determination

● M. Besançon

Experimental aspects of SUSY with \mathcal{R}

● G. Moedau

\mathcal{CP} and FNKN in SUSY with \mathcal{R}

2. DETERMINING THE STRUCTURE

Charginos

Tsukamoto et al.
Moortgat-Loh et al.
Feng et al.
Choi et al.
Lafaye et al.
⋮

$$W^\pm \Rightarrow \tilde{W}^\pm$$

gaugino

$$H_1, H_2 \Rightarrow \tilde{H}_1, \tilde{H}_2$$

Higgsino

$$\psi^\pm = \begin{pmatrix} -i\tilde{W}^\pm \\ \tilde{H}^\pm \end{pmatrix}$$

mass term $\psi^- M_c \psi^+ + \text{h.c.}$

$$M_c = \begin{pmatrix} M_2 & \sqrt{2} m_w \cos \beta \\ \sqrt{2} m_w \sin \beta & \mu \end{pmatrix}$$

$$\left\{ \begin{array}{l} M_2 = \text{SU}(2) \text{ gaugino mass} \\ \mu = \text{Higgs mixing parameter} \\ \tan \beta = \frac{v_2}{v_1} = \frac{\langle H_2^0 \rangle}{\langle H_1^0 \rangle} \end{array} \right. \quad \mu H_1, H_2$$

charginos $\tilde{\chi}_i^\pm$ mass eigenstates

$$m_{\tilde{\chi}_{1,2}^\pm} = \frac{1}{2} \left(M_2^2 + \mu^2 + 2m_w^2 \pm \sqrt{(M_2^2 + \mu^2 + 2m_w^2)^2 - 4(M_2\mu - m_w^2 \sin 2\beta)^2} \right)$$

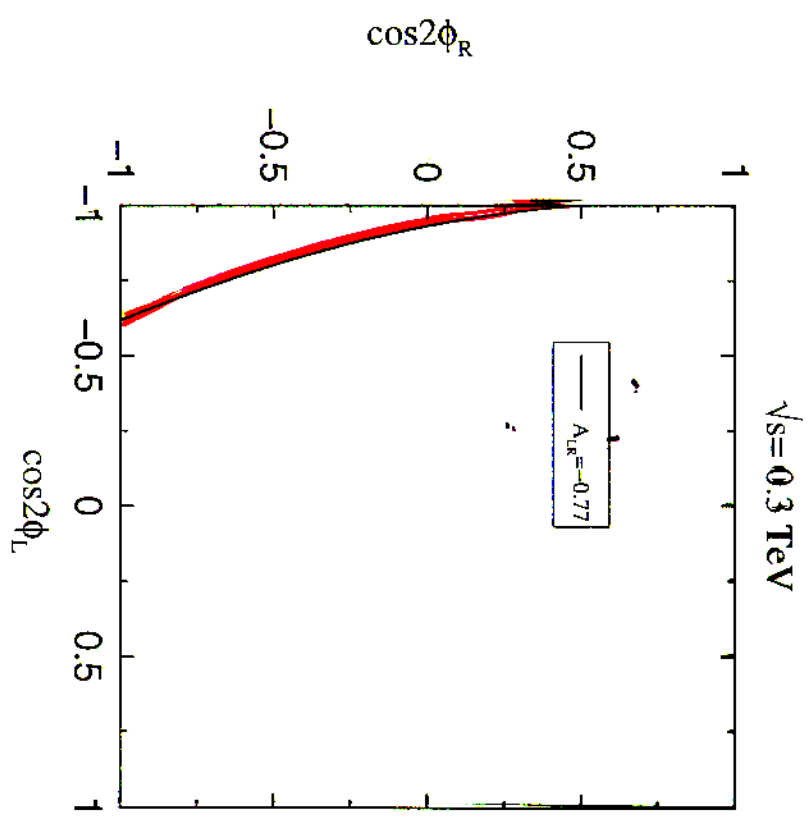
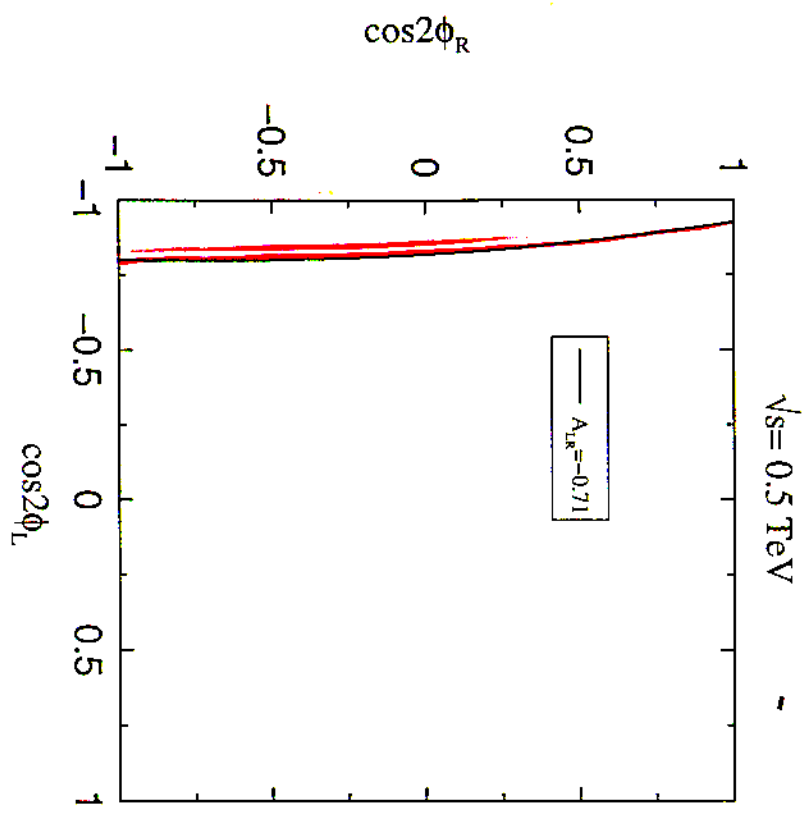
$$\tilde{\chi}_{1L}^- = \tilde{W}_L^- \cos \phi_L + \tilde{H}_1^- \sin \phi_L$$

$$\tilde{\chi}_{1R}^- = \tilde{W}_R^- \cos \phi_R + \tilde{H}_2^- \sin \phi_R$$

$$M_2, \mu, \tan \beta \Rightarrow m_{\tilde{\chi}_i^\pm}, \phi_L, \phi_R$$



add A_{LR} if available



unique solution \Rightarrow

$m_{\tilde{\chi}_1^+} = 95 \text{ GeV}$

$\cos 2\phi_L = -0.8$

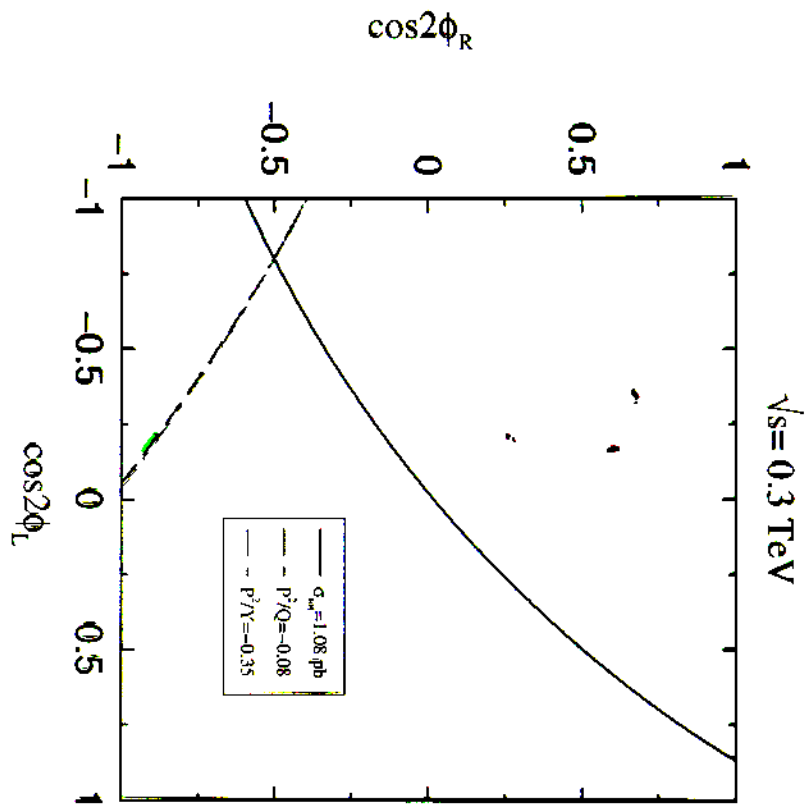
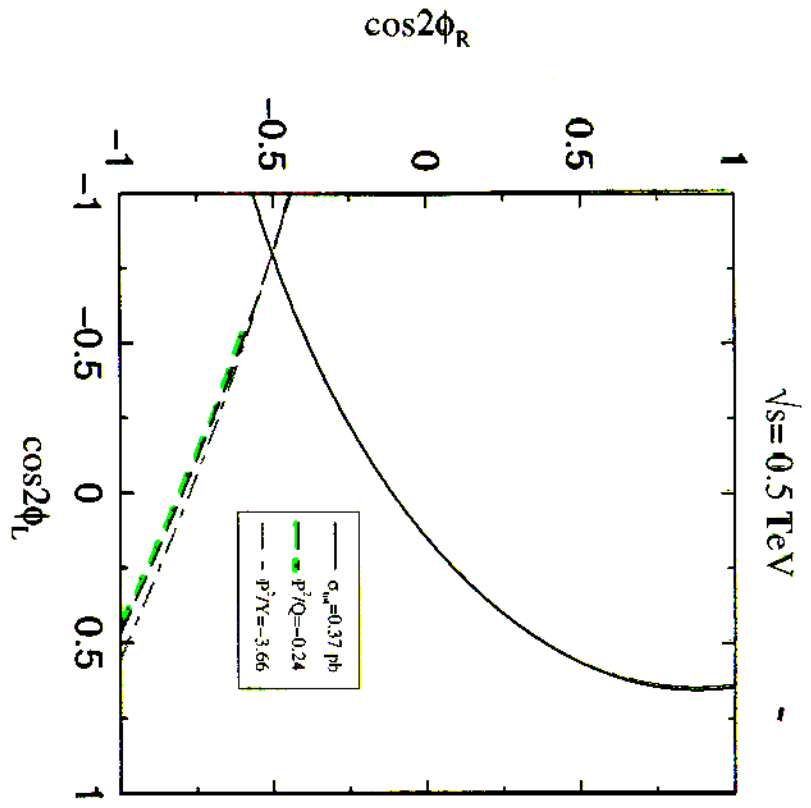
$\cos 2\phi_R = -0.5$

\rightarrow fundamental parameters

$\tan \beta$	1.06	3.33
M_2	83	248
μ	-59	123
		GeV

two-fold ambiguity

physical observables \rightarrow physical parameters (vary energy as well)



Errors

$\mathcal{L} = 50 \text{ fb}^{-1}$

$\mathcal{L} = 500 \text{ fb}^{-1}$

RR 2 ($\tan\beta = 30$)

$m_{\tilde{\chi}_{\pm}^0} = 132, 295 \text{ [GeV]}$

0.1

0.1

$\cos 2\phi_L = 0.49$

0.12

0.02

$\cos 2\phi_R = 0.86$

0.02

0.005

$M_2 = 150 \text{ [GeV]}$

7.03

1.20

$\mu = 263 \text{ [GeV]}$

4.0

0.68

$\cos 2\beta = -0.9978$

0.33

0.056

$\sin 2\beta = 0.0666$

0.19

0.033

$\tan\beta = 30$

(7.6 - ∞)

(2.2 - 59.6)

$M_1 = 75.4$

1.96

0.40

(-74)

1.46

0.32

large luminosity crucial for $\tan\beta$!

Contents

1. Investigated Process

- Feynman Diagrams
- Motivation for M' Range

2. Beam Polarization

- Polarization-Asymmetry
- Forward-Backward Asymmetry

3. Numerical Results

Constraining M'

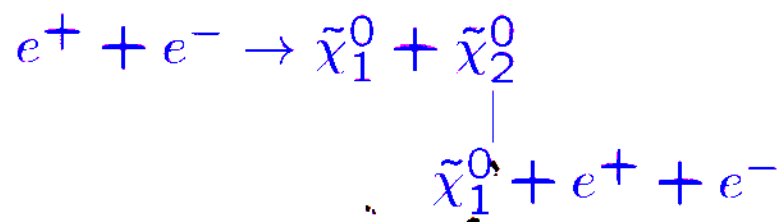
- $m_{\tilde{e}_L} \approx m_{\tilde{e}_R}$
- $m_{\tilde{e}_L} \ll m_{\tilde{e}_R}$
- $m_{\tilde{e}_L} \gg m_{\tilde{e}_R}$

4. Conclusions

5. Outlook

1. Investigated process (MSSM)

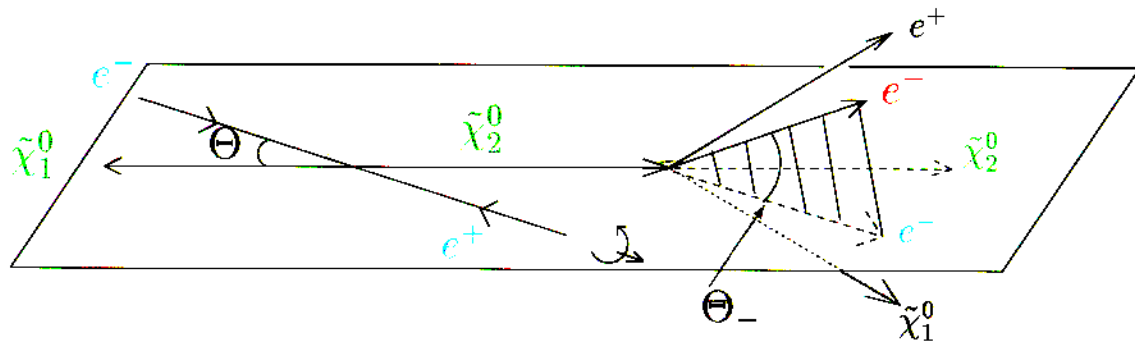
Neutralino production with leptonic decay:



⇒ Including the complete **spin correlations** between production and decay!

Kawasaki '73
 Dicus '85
 Feng '97
 M.-P. '97, '99 } *et al.*

Decay Angular Distribution of e^- in the Laboratory System



- Production:

No forward-backward asymmetry!
(Majorana character!)

- Production \times Decay:

Angular distribution of e^- depends on polarization of $\tilde{\chi}_2^0$ ($P_{\tilde{\chi}_2^0}^3 \sim \cos \Theta$!)

\Rightarrow Large **forward-backward-asymmetry** of decay e^- possible:

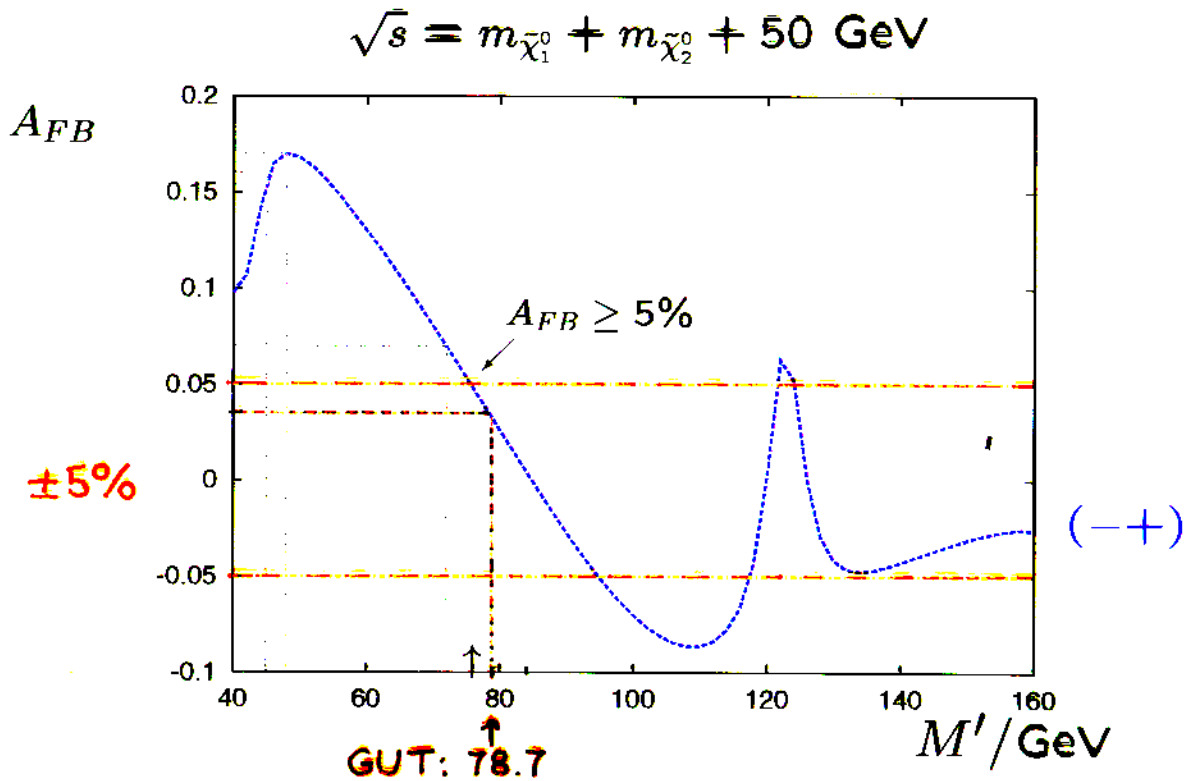
$$A_{FB} = \frac{\sigma(\cos \Theta_- > 0) - \sigma(\cos \Theta_- < 0)}{\sigma(\cos \Theta_- > 0) + \sigma(\cos \Theta_- < 0)}$$

- Cross Section:

$$\sigma_e = \sigma \times BR = \int \frac{d\sigma}{d \cos \Theta_-} d \cos \Theta_-$$

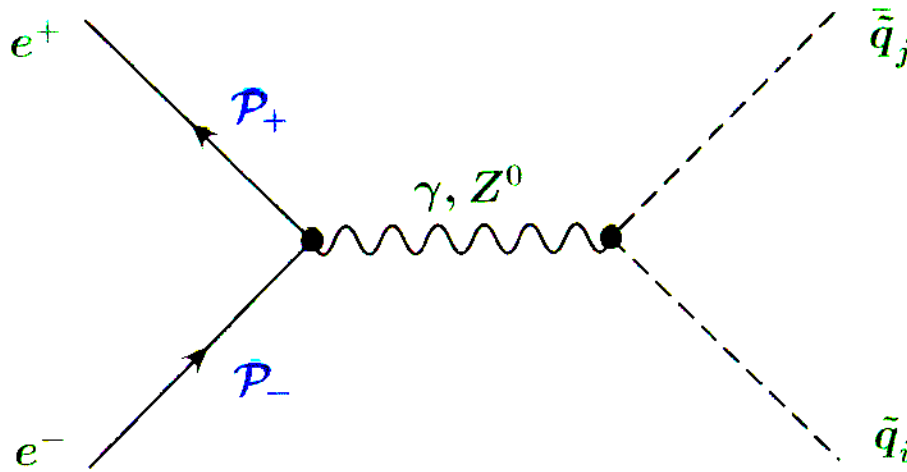
a) Small slepton mass splitting, $m_{\tilde{e}_L} \approx m_{\tilde{e}_R}$

Forward-backward asymmetry of decay lepton with beam polarization:



- complex interplay between production and decay (\rightarrow 'spin correlations')
- strong dependence on M'
- $|A_{FB}| > 5\%$: range of M' can be further constrained
- independent of $\Gamma_{\tilde{\chi}_2^0}$

Squark production in e^+e^-

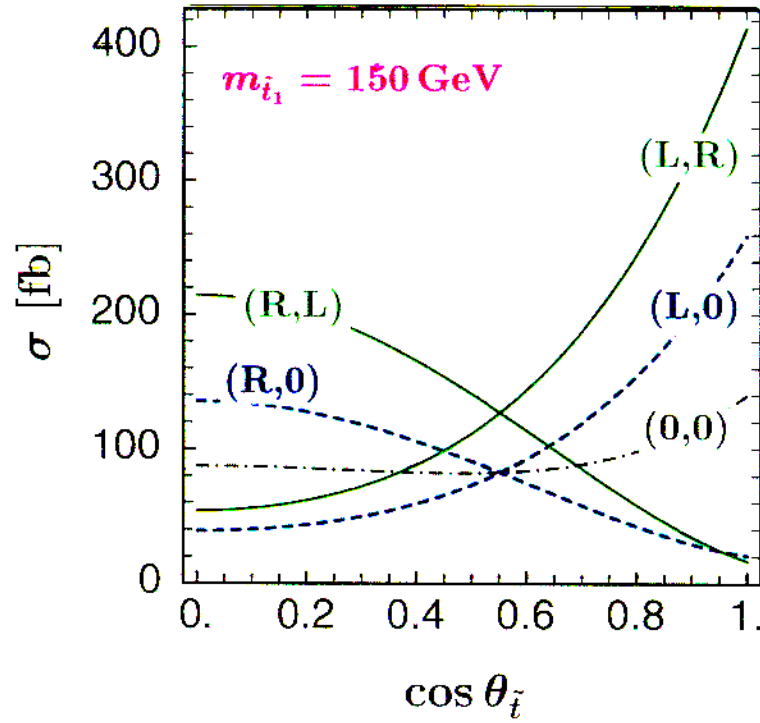


\mathcal{P}_- is the degree of polarization of the e^- beam and \mathcal{P}_+ that of the e^+ beam. $\mathcal{P}_\pm \in [-1, 1]$ with

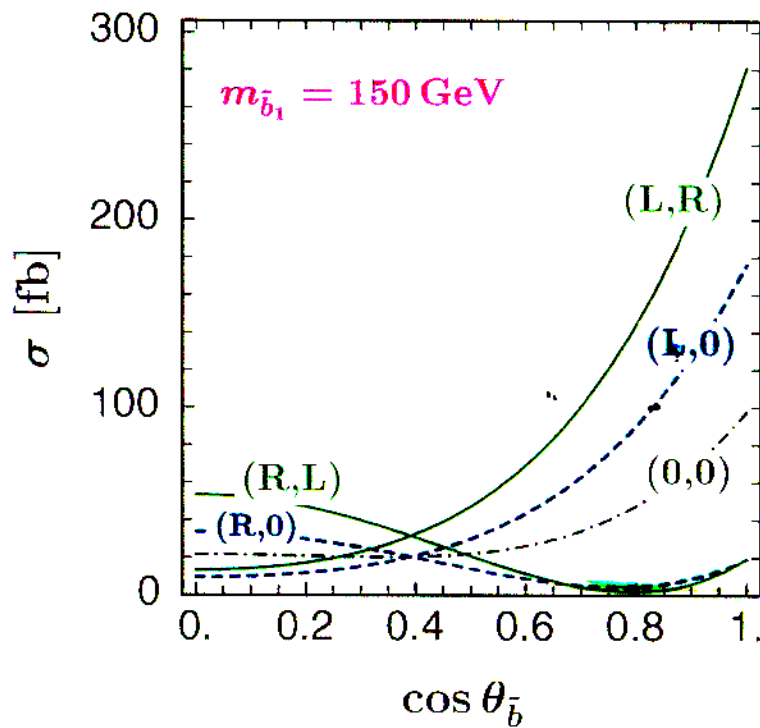
$$\mathcal{P}_\pm = \begin{cases} -1 & \text{if } e^\pm \text{ is left-polarized,} \\ 0 & \text{if } e^\pm \text{ is unpolarized,} \\ +1 & \text{if } e^\pm \text{ is right-polarized.} \end{cases}$$

cross sections
incl. SUSY-QCD and ISR corrections

$$e^+e^- \rightarrow \tilde{t}_1\tilde{t}_1$$



$$e^+e^- \rightarrow \tilde{b}_1\tilde{b}_1$$



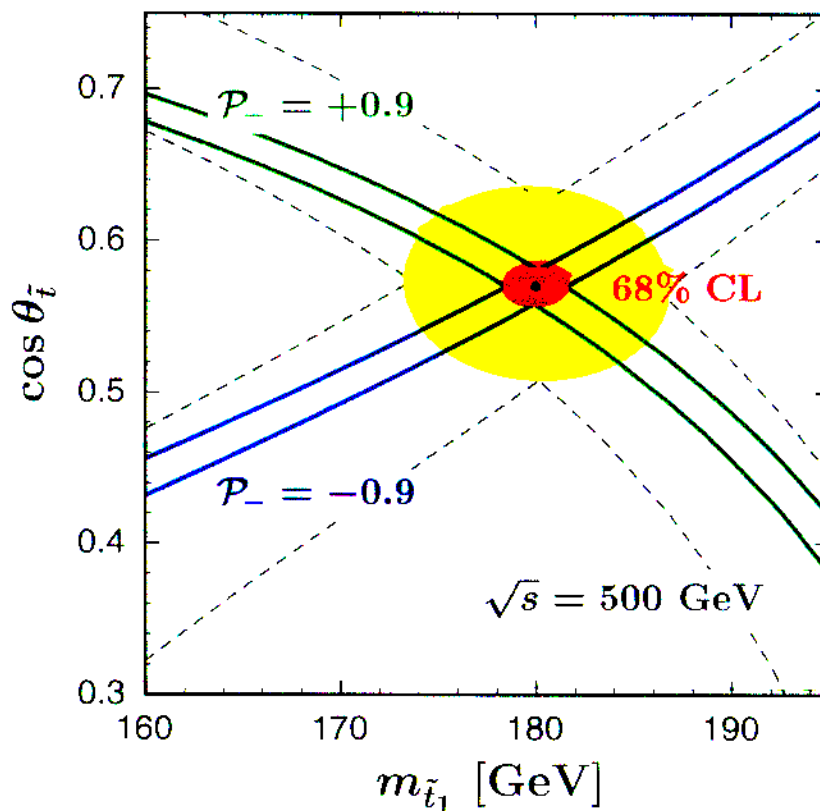
(L, R) \equiv ($\mathcal{P}_- = -0.9$, $\mathcal{P}_+ = +0.6$), etc. ...

$$m_{\tilde{t}_2} = m_{\tilde{b}_2} = m_{\tilde{g}} = 600 \text{ GeV}, \quad \sqrt{s} = 500 \text{ GeV}.$$

Determination of MSSM parameters with polarized e^- beams

— high lumi —

$$m_{\tilde{t}_1} = 180 \text{ GeV}, \quad \cos \theta_{\tilde{t}} = 0.57$$



$\mathcal{L} = 300 \text{ fb}^{-1}$:

we ESTIMATE errors

$$\mathcal{P}_- = -0.9 \quad \dots \quad \sigma(\tilde{t}_1 \tilde{t}_1) = 61.2 \pm 1.5 \text{ fb}$$

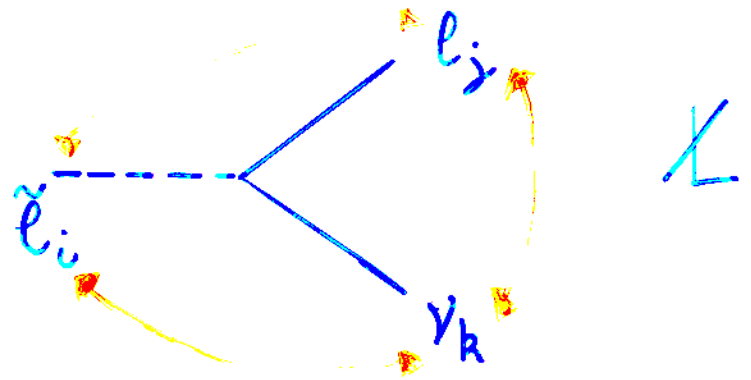
$$\mathcal{P}_- = +0.9 \quad \dots \quad \sigma(\tilde{t}_1 \tilde{t}_1) = 57.1 \pm 1.4 \text{ fb}$$

SUSY-QCD corrections taken into account

$$\Rightarrow m_{\tilde{t}_1} = 180 \pm 1.65 \text{ GeV}, \quad \cos \theta_{\tilde{t}} = 0.57 \pm 0.0012$$

$$\lambda_{ijk} \quad L_i L_j E_k$$

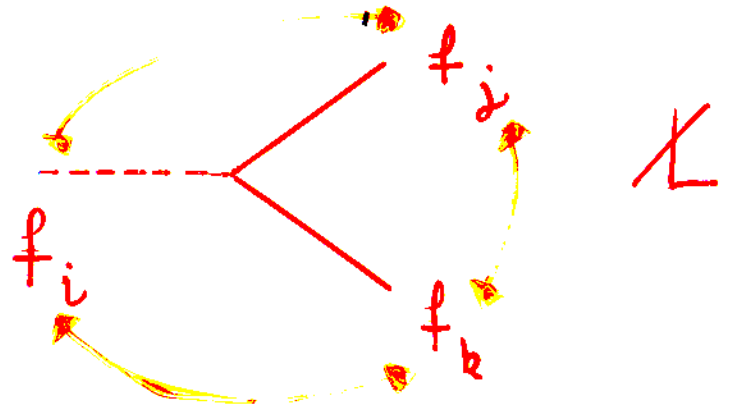
$i \neq j$ (9 termes)



+

$$\lambda'_{ijk} \quad L_i Q_j \overline{D}_k$$

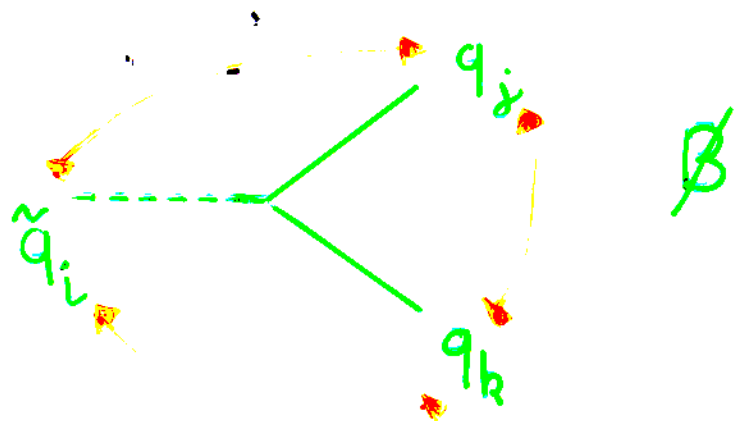
(27 termes)



+

$$\lambda''_{ijk} \quad \overline{U}_i \overline{D}_j \overline{D}_k$$

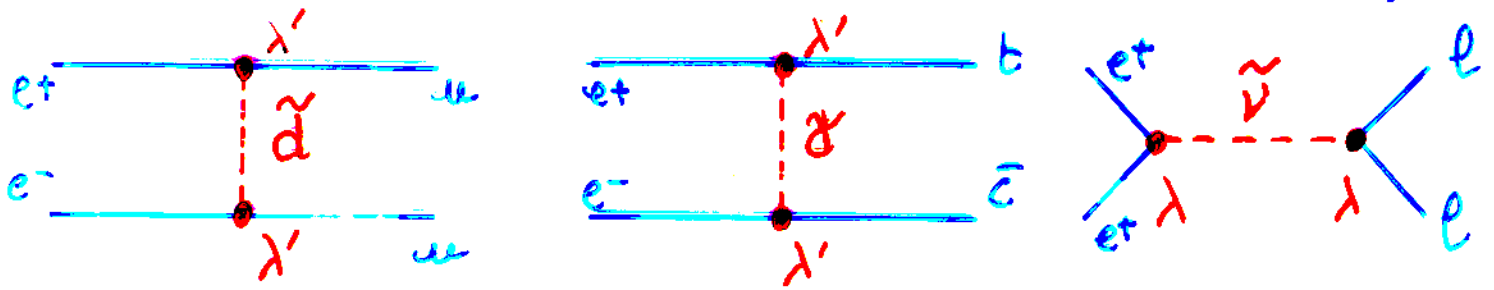
$j \neq k$ (9 termes)



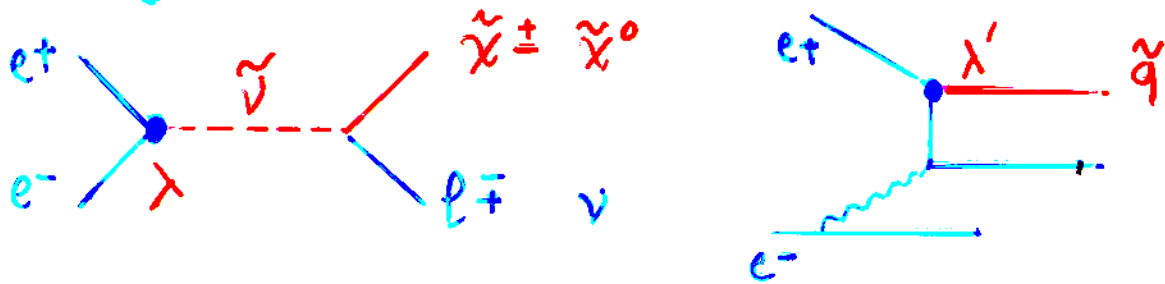
$$R_p = (-1)^{3B + L + 2S}$$

Phenomenology at e^+e^- colliders

- indirect effects $e^+e^- \rightarrow f\bar{f}$ (resonant also)



- single production of SUSY particles



See G. Moreau talk at this workshop

- effects in decays

"ordinary" pair production of susy particles

followed by either direct decay $\tilde{f}_i \rightarrow f_j f_k$

or indirect decay $\tilde{f}_i \rightarrow f_i \tilde{\chi}_1^0 \rightarrow f_i f_j f_k$

- For decay to happen inside detector

$$\lambda \gtrsim 10^{-5} \text{--} 10^{-6} \quad (\text{Gauginos})$$

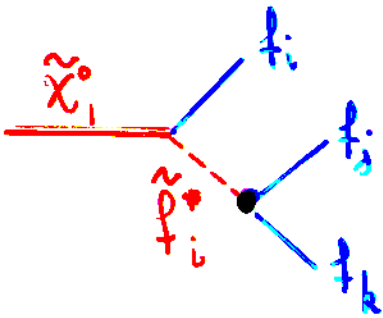
$$\lambda \gtrsim 10^{-7} \text{--} 10^{-8} \quad (\text{Sfermions})$$

Signature : multi lepton - multi jets

λ_{ijk}

λ'_{ijk}

λ''_{ijk}

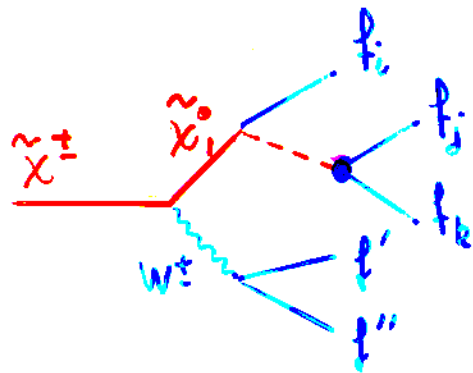


$2\nu 4\ell$

$2\ell + 4q$

$2\nu + 4q$

$6q$



$4\ell + 2\nu + 4q$

$8q + 2\ell$

$4\ell + 2\nu + 2q + \ell\nu$

$6q + 2\ell + 2\nu + 2\ell$

$4\ell + 2\nu + 2\ell + 2\nu$

$4q + 2\ell + 2\ell + 2\nu$

$10q$

$8q + \ell\nu$

$6q + 2\ell + 2\nu$

$N_{jet} \stackrel{?}{=} N_q$

Search for $\tilde{\chi}_1^0$ with a λ'' coupling

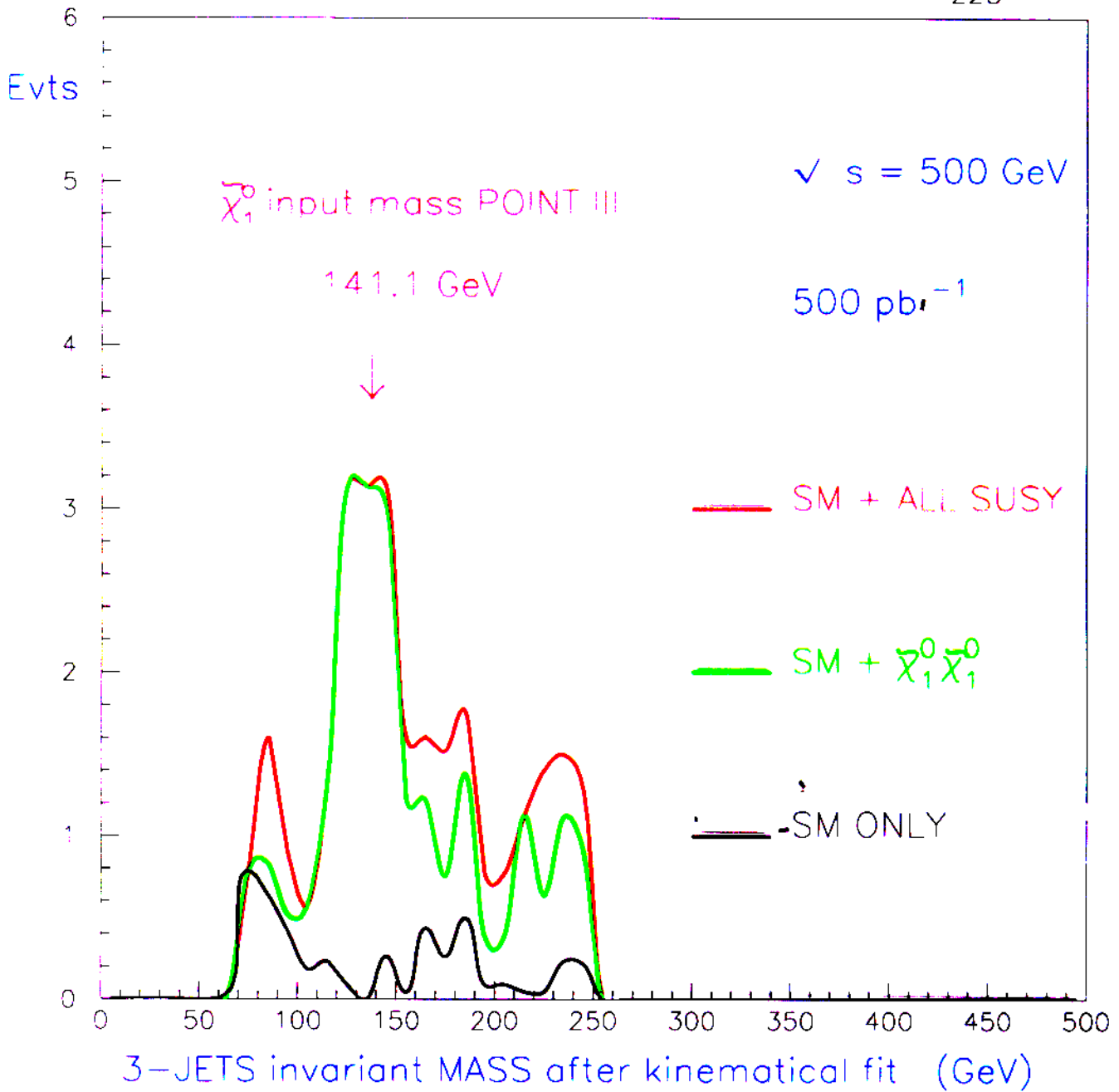
- Pair production of $\tilde{\chi}_1^0$ (LSP)
cross-section high
- assume λ''_{223} coupling
one of the less constrained $\lambda''_{223} < 1.25$
- leads to 6 jets signature including 2 b-jets
- opportunity vs LHC ?
QCD background at LHC ?
- assume so called mSUGRA
several points in the parameter space

SELECTION

- $N_{tot} > 12$ and $N_{charged} > 6$
- $N_{jet} = 6$
- $E_{tot} > 300$ GeV and $E_{\gamma}^{max} < 80$ GeV
- θ_{jets} in $[10^{\circ}, 170^{\circ}]$
- apply b-tagging
- apply 5 Constraints kinematical fit on jets
 - 4C: 4-momentum conservation
 - 1C: 2 objects with equal mass
- $D_{min} < 15$ GeV and $\chi_{5C}^2 < 90$
 D_{min} is the difference of the two 3-jets invariant masses with the combination of 3-jets which minimizes this difference

Look at 3-jets invariant mass = mass of $\tilde{\chi}_1^0$

SUSY with R-parity violating coupling λ''_{223}



Broken R parity contributions to
 Flavour Changing Neutral Currents
 & CP Violation: $P^+ P^- \rightarrow \bar{f}_J f_{J'}, \tilde{f}_J^* \tilde{f}_{J'}$

G. Moore

FCNC rates

$$\sigma(\bar{f}_J f_{J'}) \approx \left(\frac{\lambda}{0,1}\right)^4 \left(\frac{100 \text{ GeV}}{\tilde{m}}\right)^{2,5} 10 \text{ fb}$$

$$\mathcal{B}(Z \rightarrow \bar{f}_J f_{J'}) \approx \left(\frac{\lambda}{0,1}\right)^4 \left(\frac{100 \text{ GeV}}{\tilde{m}}\right)^{2,5} 10^{-9} \sim \mathcal{B}(\text{S.M.})$$

$$\sigma(\tilde{f}_J^* \tilde{f}_{J'}) \approx \left(\frac{\lambda}{0,1}\right)^4 10 \text{ fb} \lesssim \sigma'(\text{M.S.S.M.})$$

CP Asymmetries

$$\mathcal{A}(\bar{f}_J f_{J'}) \approx (10^{-2} - 10^{-3}) \sin \psi$$

$$\mathcal{A}(Z \rightarrow \bar{f}_J f_{J'}) \approx (10^{-1} - 10^{-3}) \sin \psi \gtrsim \mathcal{A}(\text{S.M.})$$

$$\mathcal{A}(\tilde{f}_J^* \tilde{f}_{J'}) \approx (10^{-2} - 10^{-3}) \sin \psi \gtrsim \mathcal{A}(\text{M.S.S.M.})$$

$\psi \equiv$ CP odd complex phase

involving the λ, λ', R_p couplings

Conclusions

- There are different methods to determine the SUSY parameters $M', M, \mu, \tan\beta$
- High \mathcal{L} + polarisation of e^- (and e^+) crucial for a precise determination of the SUSY parameters
- $\tilde{\chi}$ leads to a rich phenomenology, multilepton and multijet events (difficult at LHC!)

Talks at Sitzes

S Ambrosanio	GMSB studies
H-U Marty	mSUGRA studies
A Sopczak	$\tilde{e}\tilde{e}$ production
M Besançon	R_p violating SUSY
S Choi	$\chi^+\chi^-$ analysis
G Moortgat-Pick	$\chi^0\chi^0$ analysis
H Eberl	$\tilde{q}\tilde{q}$ production
G Moreau	CP violation and FCNC in R_p violating SUSY

Task list

expt:

- include more difficult models
- update, improve, refine analysis
 - mass measurements, esp. multi-jets
 - more decay channels, Br determination
 - explicit polarisation $e_L e_R$ & $e_R e_L$

theo:

- determine errors on SUSY parameters given the achievable expt. resolutions
- map out accessible parameter space
 - SUGRA, non-SUGRA, CP phases, ...
- use polarisation of both beams
- radiative corrections

all:

- quantitative comparison with LHC potential