

Lyth

F - term inflation

in

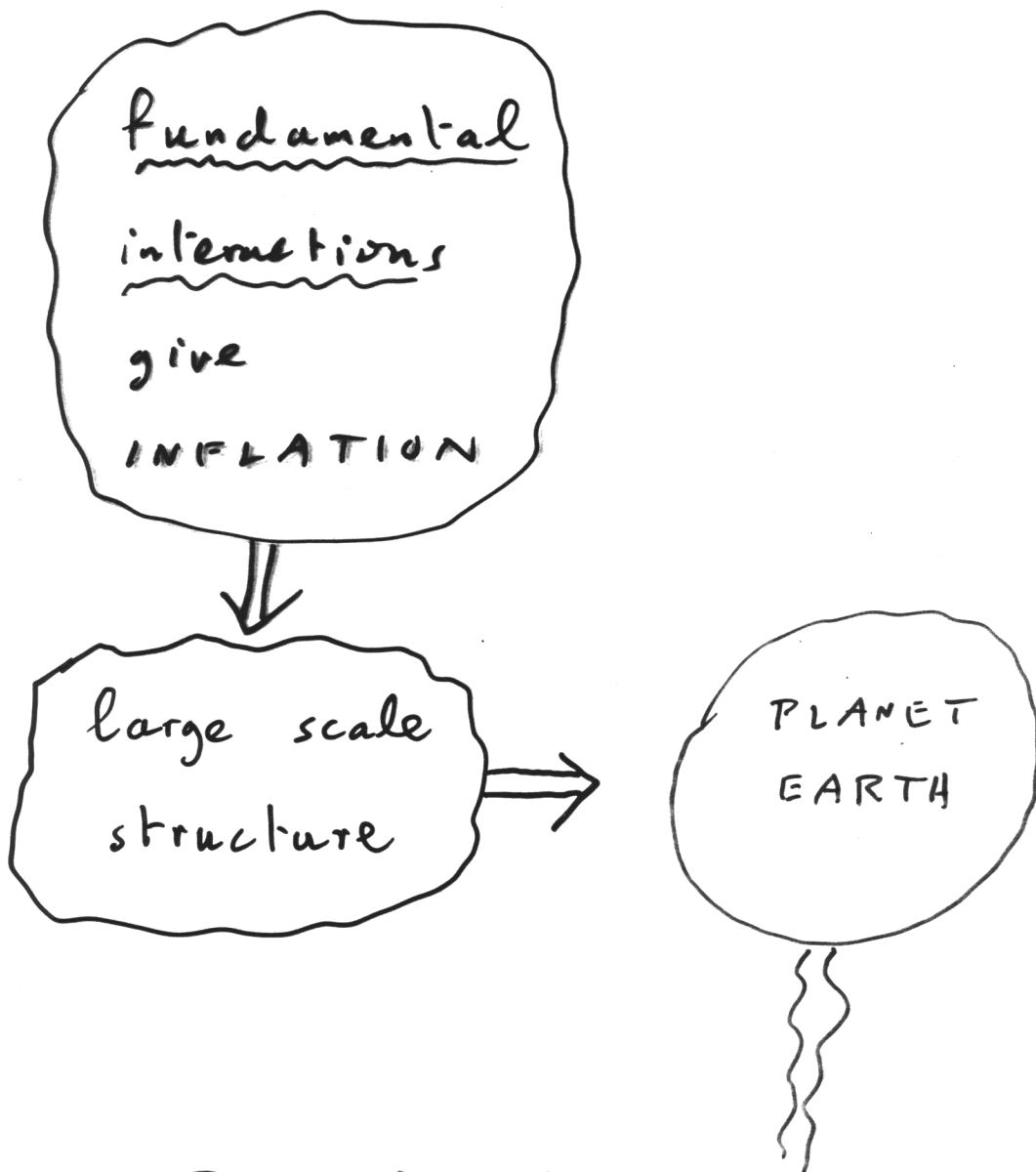
weakly coupled string theory

CLSW Copeland, Liddle, Lyth, Stewart, Wands  
S Stewart 1995  
1994

Gaillard, Lyth & Murayama hep-th/9806157

1. Models of inflation
2. Ways of keeping potential flat  
D-term inflation ☹️
3. Weakly coupled string theory potential
4. A D term drives F-term inflation





Particle theorists use astronomer's observation of large scale structure to probe inflation and hence the fundamental interactions

3/ What is a 'model of inflation'?

Model = OUTER SHELL ( $V(\phi)$ )  
+ INTERIOR (underlying  
supergravity theory)

complete  
model

eg. "D-term  
inflation"



just a  
shell eg.

"chaotic"  
inflation

$V \propto \phi^n$ ,  $\phi \sim 10M_p$



just an  
interior

THIS TALK:  
PRECISE  
POTENTIAL  
NOT  
SPECIFIED



# Keeping the inflation potential flat

Use a global susy flat direction, but  
also need during inflation

INFLATON  
MASS

$$\left| \frac{m^2 M_P^2}{V} \right| \lesssim 0.1$$

INFLATON  
POTENTIAL

$$\left( \frac{n-1}{2} \right) < 0.1$$

↑ from spectral  
index  $|n-1| < 0.2$

Supergravity with F term dominating

$$V = e^{K/M_P^2} [\dots]$$

$$K = |\phi|^2 + \dots$$

$$\frac{m^2 M_P^2}{V} = 1 + X$$

Generically  $|X| \gtrsim 10^{-1}$  or so


but we need  $X = -1.0 \pm 0.1$

HOW?

# Ways of keeping inflation mass small

- 1. Hybrid inflation with Fayet-Illiopoulos term:  
D-term dominates potential

[Stewart 95, Binetruy-Dvali 96 Halvo 96  
--- Uncle Tom Cobley and all ]

  $\phi \gtrsim M_p$  so non-renormalizable terms out of control [Kolda/March-Russel]  
 $V$  too big  
 Fields tend to drive  $D \rightarrow 0$

- 2. Kinetic term diverges [Stewart 95] ??

- 3. Inflation mass runs with scale 

[Stewart 96, Covi/Lyth/Roszkowski 97]

- 4. Inflation mass small by accident 

- 5. Inflation mass small by design, no-scale type theory

THIS TALK

 ??

## Weakly coupled string theory

Gives dilaton/axion, bulk moduli,  
matter fields. Assume 3 moduli

$$t_I \quad I = 1, 2, 3$$

matter fields

$$\begin{aligned} \phi_\alpha & \quad \alpha = AI \quad (\text{untwisted}) \\ & \quad \alpha = A \quad (\text{twisted}) \end{aligned}$$

(dilaton/axion later)

Invariance under modular transformations  
gives superpotential

$$W = \sum_m \lambda_m \prod_\alpha \phi^{n_m^\alpha} \prod_I \eta(t_I)^{2 \sum_\alpha n_m^\alpha q_I^\alpha - 2}$$

$$q_I^\alpha = \text{modular weight}, \quad q_I^{AJ} = \delta_J^I$$

$$K = - \sum_I \ln (t_I + t_I^* - \sum_A |\phi_{AI}|^2) \\ + \text{TWISTED}$$

## Recipe for successful inflation

During inflation require every term of  $W \approx 0$

$$\Rightarrow \frac{\partial W}{\partial t_I} \approx 0$$

twisted fields

$$\text{AND } W_\alpha \equiv \frac{\partial W}{\partial \phi_\alpha} = 0$$

$\ll M_P$

except for one untwisted sector

$$V = \frac{\sum_A |W_{A3}|^2}{x_1 x_2}$$

$$x_I \equiv t_I + t_I^* - \sum_A |\phi_{AI}|^2$$

This has no-scale form, but  $V \neq 0$ . Not obvious that masses small for flat directions or global susy. Need more detail to show this for at least one direction, to allow an inflation.

Using a Fayet - Iliopoulos D term

to generate the F term [GLM 98]

SIMPLEST MODEL

Assume only one nonzero  $W_\alpha$ ,  $\alpha = C3$   
coming from a term

$$W = \lambda \phi_{A1} \phi_{B2} \phi_{C3}$$

NO  
FI  
DEPENDENCE!

generate  $\phi_{A1}$ ,  $\phi_{B2}$  from FI D term

$$V_D = \frac{g^2}{2} \left( \xi - x_1^{-1} |\phi_{A1}|^2 - x_2^{-1} |\phi_{B2}|^2 + \dots \right)$$

let  $A1$ ,  $B2$  be F-flat

$V_D \rightarrow 0$  gives

$$|\phi_{A1}|^2 = C_1 x_1$$

$$|\phi_{B2}|^2 = C_2 x_2$$

$$V = \lambda^2 \xi^2 \quad \text{FI dependence has gone!}$$

flat directions preserved in all  
untwisted sectors, plenty of  
inflation candidates.

PROBLEMS  
OF D-TERM  
INFLATION  
AVOIDED

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# Including the dilaton

Assume  $V^{1/4} \gg 10^{10}$  GeV

so that gaugino condensation negligible (?)

But we must stabilize the dilaton.

Use non-perturbative  $K$ , and

linear multiplet formalism [BGW 97]

Simple scheme for inflation doesn't work.

Instead, allow more general form

$$W = \lambda \phi_{c3} [\eta(t_1) \eta(t_2)]^{-2} \prod_{\alpha} \phi_{\alpha} \prod_I \eta^{2g_{\alpha}}(t_I)$$

[ $M_P = 1$ ] and generalize <sup>SOME</sup>  $\phi_{\alpha}$  from  $\mathbb{D}$  term

and trigger the rest from other contributions to  $W$ .

CAN STABILIZE DILATON, AND

$$V \propto \prod_I \left[ |\eta(t_I)|^4 \propto_I \right]^{n_I}$$

$n_I = 0$  or  $\pm$  INTEGER

NEED AT LEAST ONE  $n_I = 0 \Rightarrow$  FLAT DIRECTIONS

OTHERS  $< 0 \Rightarrow$  MODULI STABILIZED

MAGNITUDE  $V \sim \lambda^2 \left( \frac{3}{M_P^2} \right)^{\frac{d-1}{4}} \}^2$

# CONCLUSION

Weakly coupled string  
theory may give viable  
inflation with F I D term  
generating an F term

Specific model ?

Connection with extensions  
of Standard Model ?

M - theory . . . . ?